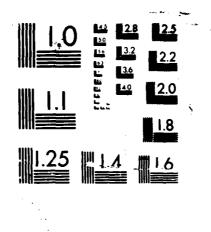
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NAVAL POSTGRADUATE SCHOOL

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THESIS

FURTHER DEVELOPMENT OF A ONE-DIMENSIONAL UNSTEADY EULER CODE FOR WAVE ROTOR APPLICATIONS

by

David T. Johnston

March 1987

Thesis Advisor:

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Further Development of a One-Dimensional Unsteady Euler Code for Wave Rotor Applications

by

David T. Johnston Lieutenant, United States Navy B.S., Cornell University, 1979

Submitted in partial fulfillment of the requirements for the degree of

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ABSTRACT

The EULER1 Fortran program for computing one-dimensional unsteady flow based on the QAZ1D method of Verhoff was extended to provide tracking and correcting of discontinuities, flow to right or left and open and closed end boundary conditions. The program was run on four shock tube test cases to verify accuracy and range of capability of the revised E1DV2 code. Further extensions and test verifications are recommended so that the code is suitable for wave rotor applications.



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TABLE OF CONTENTS

I.	INT	RODU	CTION	18
II.	ANAI	LYTI	CAL AND COMPUTATIONAL APPROACH	20
	A.	QAZ	1D DESCRIPTION	20
	в.	CHA	RACTERISTIC SOLUTION	23
	c.	DIS	CONTINUITIES	28
	D.	BOU	NDARY CONDITIONS	44
III.	FOR	TRAN	PROGRAM E1DV2	51
	A.	GEN	ERAL DESCRIPTION	51
	в.	THE	MAIN PROGRAM	52
	c.	THE	SUBROUTINE PROGRAMS	56
IV.	RESU	ULTS		76
	Α.	TES	T CASE 1	77
	В.	TES	T CASE 2	83
	c.	TES	T CASE 3	36
	D.	TES	T CASE 4	86
v.	DISC	cuss	ION	92
	A.	RES	ULTS OF TEST CASES	92
	в.	CUR	RENT LIMITATIONS OF THE E1DV2 CODE	96
VI.	соис	CLUS	IONS	99
APPENI	X XIC	A:	DERIVATION OF EQUATIONS	101
APPENI	OIX E		OPERATION OF ED1V2 ON THE NPS VM/CMS SYSTEM	115
APPENI	oix (c:	FLOWCHARTS	122
ADDENI	TY T	D •	FIDUS FORTEN LISTING	142

LIST	of	REFERENCES		 200
INIT	[AL	DISTRIBUTIO	N LIST	 201

| 100mm | 10

LIST OF TABLES

I	SUMMARY OF THE EULER EQUATIONS	21
II	SHOCK EQUATIONS FOR HIGH PRESSURE ON LEFT	31
III	SHOCK EQUATIONS FOR HIGH PRESSURE ON RIGHT	35
IV	SUBROUTINES	53
V	VALUES OF PARAMETERS SHOCK AND CNTACT	61
B.I	TERMINAL AND OUTPUT	115
B.II	EDITABLE VARIABLES	117

LIST OF FIGURES

2.1	The Natural Coordinate System	22
2.2	Characteristic Curve within Computational Mesh	26
2.3	Computational Grid for the QAZ1D Method	27
2.4	Shock Wave with High Pressure on Left	29
2.5	Q Extended Riemann Variable Change with Mach Number	33
2.6	Shock Wave with High Pressure on Right	34
2.7	Extended Riemann Variable Change with Mach Number, High Pressure on Right	37
2.8	Behavior of Physical Properties through a Contact Surface	40
2.9	Modified Entropy Distribution for Shock and Contact Surface Traveling Right	42
2.10	Modified Entropy Distribution for Shock and Contact Surface Traveling Left	44
2.11	Left Boundary Computational Grid	45
2.12	Right Boundary Computational Grid	47
2.13	Shock Reflecting at Solid Boundary	49
3.1	Overall Algorithm for QAZ1D Method	58
3.2	Incerval and Node Description used in "SWEEP"	60
3.3	Schematic of SHOCK = 331 and CNTACT = 232	60
3.4	Schematic of SHOCK = 100 and CNTACT = 321	62
3.5	Schematic of SHOCK = 221 and CNTACT = 222	62
3.6	Schematic of SHOCK = 231 and CNTACT = 322	63
3.7	Computational Method for "COND1" Routine	65
3.8	Computational Method for "COND2" Routine	66

3.9	Computational Method for "COND3" Routine	67
3.10	Example Condition for "COND5" Routine	68
3.11	Example of "COND4" Routine Situation	69
3.12	Example of "COND6" Situation	70
3.13	Discontinuity Location within an Interval	73
4.1	Shock Tube at t = 0 and t = t	76
4.2	Test Case 1 (J = 1 to J = 55)	78
4.3	Test Case 1 (J = 56 to J = 109)	79
4.4	Exact and Computed Density Distributions (Test Case 1)	80
4.5	Location of Discontinuities versus Time (Test Case 1)	81
4.6	Test Case 1, High Pressure on Right	82
4.7	Test Case 2, High Pressure on Left	84
4.8	Test Case 2, High Pressure on Right	85
4.9	Test Case 3, High Pressure on Left	87
4.10	Test Case 3, High Pressure on Right	88
4.11	Test Case 4, High Pressure on Left	90
4.12	Test Case 4, High Pressure on Right	91
A.1	Shock Wave with High Pressure on Right	102
A.2	Contact Surface Traveling Right, Subscript Notation	110
A.3	Contact Surface Traveling Left, Subscript Notation	112
C.1	Main Program Flowchart	123
C.2	"DBURST" Subroutine Flowchart	125
C.3	"TRAK" Subroutine Flowchart	127
C.4	"SWEEP" Subroutine Flowchart	131

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C.5	General "COND1,2,3 and 5" Subroutine Flowchart	134
C.6	"COND4" Subroutine Flowchart	135
C.7	"CORRCT" Subroutine Flowchart	136
C.8	"BONDRY" Subroutine Flowchart	139
C.9	"SRFLCT" Subroutine Flowchart	142

TABLE OF SYMBOLS

TEXT	E1DV2	DEFINITION
A	A	Speed of Sound
	*A	Denotes the value of a variable at the node to the left of a discontinuity, * can be any variable name
^A i/ ^A j	AR	The ratio of sound speed across a shock. A/B (shock moving right), B/A (shock moving left)
	*B	Denotes the value of a variable at the node to the right of a discontinuity
	BDRY	3 denotes left boundary, 2 the right boundary
	*BD	Variable at phantom node
	CNTACT	3 digit variable denoting contact sur- face location, direction of travel, and if it crosses a node
	COUNT	Counter for graphics routines
	CSDIR	Contact surface direction, 2 to the right, 3 to the left
	CSRMN	Riemann variable change across a contact surface
	D2	Density ratio at first node inside boundary
	DARRAY	Array of density for plotting
	DELAH	Change in A from I to I+1
	DELAL	Change in A from I-1 to I
	DELQQH	Change in QQ from I to I+1
	DELQQL	Change in QQ from I-1 to I
	DELRRH	Change in RR from I to I+1

	DELRRL	Change in RR from I-1 to I
	DELSH	Change in S from I to I+1
	DELSL	Change in S from I-1 to I
δt	DELT	Time step
δt _{ex}	DELTEX	The excess time in a time step when the shock is exactly at the solid wall
ðt _{wl}	DELTWL	The time for the shock to reach the wall
	DELQH	Change in Q from I to I+1
	DELQL	Change in Q from I-1 to I
Δs	DELX	Interpolation distance (LMD+DELT)
ρ	DENS	Density
	DLCD	Density to the left of the contact discontinuity in the exact solution
	DLSH	Density to the left of the shock in the exact solution
	DLTA**	Prefix which indicates the spatial change in ** for one time step
	DQ	The jump in velocity across the shock divided by the sound speed at B (right) or A (left)
	DR	The ratio of the density across a shock, B/A (right), B/A (left)
	DRI	Initial density ratio across the diaphragm
	EE	Desired precision for characteristic calculations
	E(K)	Actual error in characteristic slope calculation
	EREIMN	The jump in QQ across the shock calcu- lated analytically as a function of w
Υ	G	Gamma (ratio of specific heats)

GRAPHS	For graphical output, 0 = none (tabular), 1 = plots all variables, 2 = compares density with exact solution
G1	1/(G-1)
G2	2/(G-1)
Н	1/(N-1)
HALT	Terminates program if 1, set by conditions not coded
INTEG(K)	Result of integrating Z(K)
**INT	Value of ** interpolated between nodes on the current time level
12	Number of the node to the right of a discontinuity
JSTOP	Number of time levels to be calculated
LBDDR	Left boundary density ratio
LBDDRI	Left boundary density ratio at time zero
LBDPR	Left boundary pressure ratio
LBDPRI,	Left boundary pressure ratio at time zero
LBDPRS	Value of 0 denotes constant pressure at left boundary, 1 denotes adjustable pressure at the left boundary
LBDTR	Left boundary temperature ratio
LBDTRI	Left boundary temperature ratio at time zero
LBNDRY	Denotes left boundary condition, open or closed
LMD(K)	The characteristic trajectories in the space-time plane (q+A, q-A, q)
LNODE	Array of left most node to be corrected in CORRCT
	Denotes which side of diaphragm has low pressure

λ

	LXX	Node defining the left interval
	MREIMN	The measured jump in QQ across the shock, from A to B
	·N	Number of Spacial Nodes (odd number)
	ND	Double precision value of N
	NEW**(I)	Stored values of ** for the next time level
	PARRAY	Array of pressures for plotting
P _i /P _j	PR	The ratio of the pressure across a shock, A/B (right), B/A (left)
P	PRESS	Pressure
	PRI	Initial pressure ratio across the diaphragm
	PLTCNT	Counter for graphics routines
<u>8*</u>	*PRIM(K)	Suffix which indicates the spatial derivative of * at the current time level
	P2	Pressure ratio at first node inside boundary
đ	Q	Absolute fluid velocity
	QARRAY	Array of velocities for plotting
	QLBD	Initial velocity at left boundary
	QLI	Initial velocity left of the diaphragm
	QRBD	Initial velocity at right boundary
	QRI	Initial velocity right of the diaphragm
Q	QQ	Q+A*S (extended Riemann variable)
	RBDDR	Right boundary density ratio
	RBDDRI	Initial right boundary density ratio
	RBDPR	Right boundary pressure ratio
	RBDPRI	Initial right boundary pressure ratio

RBDPRS Value of 0 denotes a constant pressure at right boundary, while 1 is for adjustable pressure Right boundary temperature ratio RBDTR RBDTRI Initial right boundary temperature ratio Denotes right boundary open or closed RBNDRY Array for right most node to be corrected RNODE in CORRCT Q-A*S (extended Riemann variable) R RR Node defining the right interval **RXX** S S Entropy SAP Entropy to the left of the shock for flows right or entropy to the right of the C.S. for flows left SARRAY Array of entropy for plotting SAVG Average entropy Entropy to the right of the C.S. for SBP flows right or entropy to the left of the shock for flows left Shock direction of travel, 3 to the left, SHKDIR 2 to the right SHOCK 3 digit variable denoting shock location, direction of travel, and if it crosses a node Spatial location of discontinuities SIGMA Sigma(L,J) where L indicates the type of discontinuity and J indicates the time level: 1--current level, 2--level being calculated Integer that denotes relative location of SK shock near boundaries Variable which indicates how many time SKIP steps between calls to output routines **STEP The change in time of ** at a node used to step up to the next time level

t	T	Time since initial conditions
T	TEMP	Temperature
	TRI	Initial temp, ratio across the diaphragm
	TS	Time for shock to travel one interval
	T2	Temperature ratio at first node inside boundary
u_{A}	UA	Velocity relative to the shock, left side
$\mathtt{u}_\mathtt{B}$	UB	Velocity relative to the shock, right side
	VHEAD	Velocity of the head of the expansion wave for the exact solution
	VCDE	Velocity of the contact discontinuity for the exact solution
v_s	vs	The shock speed (positive right, negative left)
	VSE	Velocity of the shock for the exact solution
	VTAIL	Velocity of the tail of the expansion wave for the exact solution
W	W	Mach no. relative to a standard shock
w		Vector of the principle variables, Q,R,S
X	x	Location in spacial plane (I-1)*H
	XARRAY	Array of spatial positions for plotting
	XEXACT	Array of six X values for the exact solution
	XINIT	Initial position of discontinuity for exact solution plotting
	X2	Location of node to right of discont. along the spacial axis
	Y	(N+1)/2
	YEXACT	Array of six density values for the exact solution

z	Z (K)	Vector of the right hand sides of the governing equations
Δ		Small spatial change
δ		Small change with respect to time
θ, φ		Flow angles with respect to reference coordinate planes

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The work is dedicated in memory of my grandparents, Ray Litton Johnston and Anna Elizabeth Weech.

I. INTRODUCTION

The investigation of wave rotors¹ and their possible application in gas turbine engines at the Naval Postgraduate School's (NPS) Turbopropulsion Laboratory prompted the development of a one-dimensional unsteady flow computer code. The QAZ1D method developed by Verhoff [Ref. 1] was chosen over other methods [Ref. 2] for reasons which included the following:

- 1. The method is based on the use of characteristics. Such methods can model wave propagation accurately.
- 2. The use of a natural streamline coordinate system eases the difficult task of computing with two and three dimensional grids.
- 3. The equations are written in a form which allows a straightforward extension to viscous flows.

Salacka [Ref. 2] verified the development of the equations and implemented a one-dimensional Euler solution of the

The wave rotor consists of simple tube-like passages along and around the periphery of a drum which rotates between end walls containing inlet and outlet (partial admission) gas ports. Compression and expansion processes are arranged to occur in a cyclically periodic unsteady process within the rotor such that a high pressure driver gas is used to compress a low pressure driven gas. compressed driven gas is led from the outlet port to the combustor and brought back into the rotor as the driver. The expanded driver gas exits an outlet port. Thus the rotor functions as both turbine and compressor with direct gas-gas energy exchange through unsteady wave processes. The technology of such devices requires the design of appropriate cycles using one-dimensional calculations, and analysis of the multi-dimensional unsteady flows such as occur during port opening and closing.

shock tube problem in the EULER1 code. The EULER1 code was limited to high pressure set on the left, with flow and shock velocities to the right. The shock wave was tracked and corrected for in the flow, but the contact discontinuity was not, and the expansion wave was not tracked. The code also did not treat end boundary conditions.

The present work extended the EULER1 code of Salacka to become the "Euler 1D Version 2" or E1DV2 code which:

- 1) can handle both right and left traveling flow and discontinuities
- 2) implements tracking and correction of the contact discontinuity
- 3) implements tracking of the expansion wave
- 4) models closed wall and open end boundary conditions
- 5) models shock and contact surfaces within a grid interval.

Section II and Appendix A describe the analysis underlying the revisions. The Fortran code, E1DV2, is detailed in Section III and Appendix C and graphical results of four test cases to demonstrate the new features of the code are given in Section IV. A discussion of these results and limitations of the present code follow in Section V. Conclusions and recommendations are made in Section VI. Appendix B contains instructions to operate the code on the NPS computer and the FORTRAN listing is included as Appendix D.

II. ANALYTICAL AND COMPUTATIONAL APPROACH

A. QAZID DESCRIPTION

The QAZID analysis and numerical solution scheme is an explicit, non-conservative method that uses extended Riemann variables to model the multi-dimensional Euler equations in a natural streamline coordinate system. Table I lists a summary of the applicable equations which are derived in detail in [Ref. 2].

1. The Coordinate System

Figure 2.1 shows the natural streamline coordinate system (s,n,m) relative to a fixed rectangular cartesian system (x,y,z). The right-hand orthogonal system moves in curvilinear translation along a streamline. The "s" direction is measured in the direction of the flow, tangent to the streamline. The "n" direction is perpendicular to the s direction in a plane perpendicular to the x-z plane. The "m" direction is normal to the plane containing the n and s directions. The angle φ is the angle between the x-n and x-y planes, and the angle φ is the angle between the velocity vector and the x-z plane in the s-n plane. In the one-dimensional problem treated here, the s direction is such that velocity to the right is positive, and to the left is negative. [Ref. 1:p. 2]

TABLE I

SUMMARY OF THE EULER EQUATIONS

Definitions

Speed of sound
$$A = \sqrt{P/\rho}$$
 (I.1)

Modified entropy change
$$dS = -\frac{dQ_R}{\gamma T}$$
 (I.2)

so that

$$\frac{\overline{S}}{R_G} = S = \frac{1}{\gamma(\gamma-1)} [2\gamma - \ln(P/\rho^{\gamma})] \qquad (I.3)$$

Extended Riemann variables

$$Q = q + As (I.4)$$

$$R = q - AS (I.5)$$

Euler Equations

$$\frac{\partial Q}{\partial t} + (q+A)\frac{\partial Q}{\partial s} = -\frac{\gamma-1}{2}A(s - \frac{2}{\gamma-1})\left[\frac{\partial}{\partial s}(q - \frac{2}{\gamma-1}A)\right] - \frac{\gamma-1}{2}qAs\left[\frac{\partial\theta}{\partial n} + \cos\theta \frac{\partial\phi}{\partial m}\right]$$
 (I.6)

$$\frac{\partial R}{\partial t} + (q-A)\frac{\partial R}{\partial s} = \frac{\gamma-1}{2}A(s - \frac{2}{\gamma-1})\left[\frac{\partial}{\partial s}(q + \frac{2}{\gamma-1}A)\right]$$

$$+ \frac{\gamma - 1}{2} qA S \left[\frac{\partial \theta}{\partial n} + \cos \theta \frac{\partial \phi}{\partial m} \right]$$
 (I.7)

$$\frac{\partial S}{\partial t} + q \frac{\partial S}{\partial s} = \phi \tag{I.8}$$

$$\frac{\partial \theta}{\partial t} + q \frac{\partial \theta}{\partial s} = -\frac{A^2}{\gamma q} \frac{\partial \ln P}{\partial n}$$
 (I.9)

$$\frac{\partial \phi}{\partial t} + q \frac{\partial \phi}{\partial s} = -\frac{A^2}{\gamma q \cos \theta} \frac{\partial \ln P}{\partial m}$$
 (I.10)

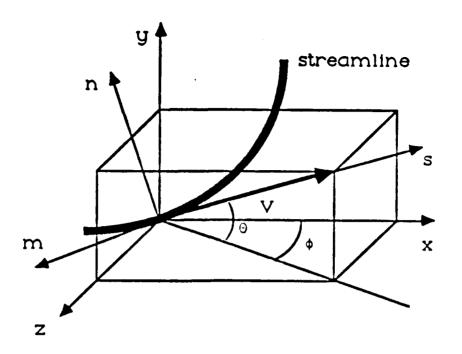


Figure 2.1 The Natural Coordinate System

2. Extended Riemann Variables

The "Riemann Variables" in most publications are defined as

$$R_1 = q - (\frac{2}{\gamma + 1}) A$$

and

(2.1)

$$R_2 = q + (\frac{2}{\gamma + 1}) A$$

where q is the velocity magnitude, A is the speed of sound, and γ is the ratio of the specific heat at constant pressure to the specific heat at constant volume for a particular gas

[Ref. 3:p. 5]. Verhoff modified the definition to obtain "Extended Riemann Variables," defined as

$$Q = q + AS (I.4)$$

$$R = q - AS \tag{I.5}$$

where S is the modified entropy given in Table I [Ref. 1:p. 2].

3. The Governing Equations

The Euler equations in Table I were developed in detail [Ref. 2:Appendix A] from the equations for conservation of mass, momentum, and energy for a control volume. The underlying assumptions comprise inviscid flow, negligible body forces, no heat transfer, and a perfect gas. These assumptions and the definition of modified entropy were used in transforming the equations into a form suitable for solution using the method of characteristics.

B. CHARACTERISTIC SOLUTION

Equations (I.6), (I.7), (I.8), (I.9) and (I.10) are a system of slightly coupled quasi-one-dimensional partial differential equations (PDE) with eigenvalues q+4, q, and q-A. These equations can be rewritten along the characteristics in the time-space domain to become ordinary differential equations (ODE) which are solved by quadrature and interpolation. The propagation of each characteristic

curve along its particular trajectory is expressed by the respective ODE. [Ref. 1:p. 1]

Each in the system of equations is in the form

$$\frac{\partial \mathbf{w}}{\partial \mathbf{t}} + \lambda \frac{\partial \mathbf{w}}{\partial \mathbf{s}} = \mathbf{z} \tag{2.2}$$

If w = w(s,t) it is shown by Salacka [Ref. 2:pp. 20-23] that

$$\lambda = \frac{ds}{dt} \tag{2.3}$$

and

$$\frac{\mathrm{d}\mathbf{w}}{\mathrm{d}\mathbf{t}} = \mathbf{z} \tag{2.4}$$

where λ describes the characteristic curve along which w changes.

In this section the solution of the 3D Euler equations given in Table I is described. The computer code developed in the present work, however, was for the 1D case wherein equations (I.9) and (I.10) are not required, and only the three remaining equations (I.6), (I.7), and (I.8) are considered.

Equations (I.6) to (I.8) for one-dimensional flow may be expressed in matrix form by setting

$$\vec{w} = \begin{bmatrix} Q \\ R \\ S \end{bmatrix} = \begin{bmatrix} q+A & 0 & 0 \\ 0 & q-A & 0 \\ 0 & 0 & q \end{bmatrix}$$

and

$$\overline{z} = \begin{bmatrix} -\frac{\gamma-1}{2}A(S-\frac{2}{\gamma-1})[q-\frac{2}{\gamma-1}A]_{S} \\ \frac{\gamma-1}{2}A(S-\frac{2}{\gamma-1})[q+\frac{2}{\gamma-1}A]_{S} \\ 0 \end{bmatrix}$$

Then equation (2.2) becomes, for the equation set,

$$\frac{\partial \overline{w}}{\partial t} + [\lambda] \frac{\partial \overline{w}}{\partial s} = \overline{z}$$
.

Figure 2.2 shows the characteristic curve in the spacetime domain between two nodes within the computational mesh. Equation (2.2) has a solution

$$\delta \overline{w} = -\Delta \overline{w} + \int_{t}^{t+dt} \overline{z} dt \qquad (2.5)$$

where $\delta \mathbf{w}$ is the change due to time at a fixed location, and $\Delta \mathbf{w}$ is the change due to displacement at a fixed location, along the characteristic curve. The value of $\Delta \mathbf{w}$ is calculated by interpolation through an iterative scheme

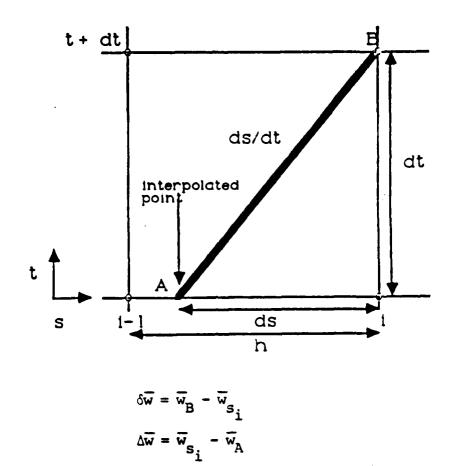


Figure 2.2 Characteristic Curve Within Computational Mesh

using initial guesses for the characteristic slope, λ , from values at time level t. The line integral is approximated by

$$\int_{t}^{t+dt} \overline{z} dt = \int_{A}^{B} \frac{\overline{z}}{\lambda} dS = \int_{S_{i}^{-}\Delta S}^{S_{i}} \frac{\overline{z}}{\lambda} dS = \frac{\overline{z}}{\lambda} (S_{i}^{-}(S_{i}^{-}\Delta S))$$

$$= \overline{z} (\Delta S/\lambda)$$

$$= \overline{z} (\delta t)$$
(2.6)

The spatial derivatives of q and A in \overline{z} are estimated from values at A and s_i . Finally, ∂w is calculated, and each node is updated to the next time level.

The Courant-Friedrichs-Lewy (CFL) convergence condition requires the domain of dependence of the numerical approximation to include the domain of dependence of the differential equation [Ref. 4:pp. 336-337]. Figure 2.3 shows that

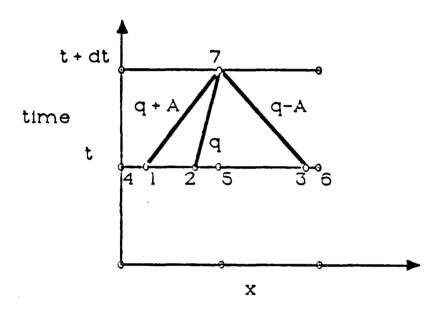


Figure 2.3 Computational Grid for the QAZ1D Method

the computational grid for the QAZ1D method satisfies this condition by having interpolated initial data points (points 1, 2, and 3) in between previous solution nodes (points 4, 5, 6). The q+A characteristic is estimated from values at point 4, q characteristic from values at point 5, and q-A characteristic from values at point 6. The use of a maximum

time step keeps the domain of dependence of the numerical scheme just outside that of the actual equations, aiding convergence. Unlike finite difference schemes that are conservative and require a numerical diffusion or viscosity to handle oscillations or smearing, this method is stable without numerical smoothing or artificial dissipation [Ref. 5:pp. 562-583]. However, the equations do not account for the discontinuities across shocks and contact surfaces properly. Thus after each time step a one-point correction technique is used to correct for shocks and contact surfaces.

C. DISCONTINUITIES

1. Expansion/Rarefaction Waves

The head and tail of the expansion wave travel along the characteristic as gradient discontinuities. Flow velocity, speed of sound, pressure, and density are continuous across a gradient discontinuity but the spatial derivatives are discontinuous. Entropy remains constant through the rarefaction wave. The head of an expansion wave moves into undisturbed flow with a speed q+A, while the tail of the expansion wave has a velocity q-A. No special treatment of these waves is required; the characteristics method accurately tracks and models their influence. Expansion waves are generated when two shocks collide, a diaphragm is burst, a contact surface and shock intersect, a shock leaves

an open boundary, or an open boundary has a pressure lower than the pressure inside the tube. [Ref. 3:pp. 13-15]

2. Shocks

Shocks are created when a diaphragm is burst, compression waves generated at an open boundary coalesce into a wavefront with sufficient strength, or when a shock and contact surface collide. Pressure, velocity, density, and entropy are discontinuous across a shock [Ref. 6:pp. 30-31]. The equations of motion (I.6)-(I.10) are not correct for calculating changes through shocks. A method to correct for a shock is to use the ratio of the jump in the extended Riemann variable across the shock to the speed of sound downstream of the shock to find the incoming Mach Number relative to the shock (w) [Ref. 1:p. 3]. Figure 2.4 shows the case of a shock headed to the right. The shock velocity

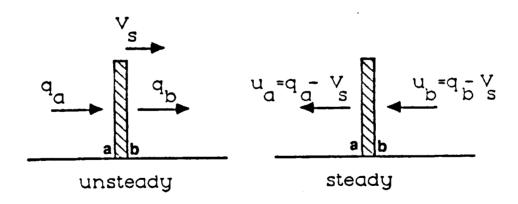


Figure 2.4 Shock Wave with High Pressure on Left

 (V_S) is imposed on the flow to produce a stationary shock condition. Flow variables are then corrected using normal shock relations. Figure 2.4 applies to a condition where high pressure is on the left. The shock is moving to the right at V_S into flow with velocity q_B . Table II lists the equations developed by Salacka [Ref. 2] for relating the extended Riemann variable change to Mach Number. Velocities are non-dimensionalized by the speed of sound downstream of the shock direction, A_B , and pressures and densities by the respective values downstream.

Figure 2.5 depicts equation (II.2) over a range of Mach Numbers from 1.0 to 4.0. The curve is approximated by the quadratic equation

$$\frac{Q_A - Q_B}{A_B} = -2.7574 + 3.1573w - 0.2863w^2$$
 (2.7)

If the high pressure is to the right the shock moves as Fig. 2.6 illustrates, and the governing equations are as listed in Table III. Again, downstream conditions are used to non-dimensionalize velocity, pressure, density, and the Riemann variable change. The development of the equations in Table III is given in Appendix A. A plot of equation (III.2) over a range of w from 1.0 to 4.0 is shown in Fig. 2.7. The curve is approximated by the quadratic equation

$$\frac{{}^{2}B^{-}{}^{2}A}{A} = 2.7574 - 3.15732w + 0.2863w^{2}$$
 (2.8)

TABLE II

SHOCK EQUATIONS FOR HIGH PRESSURE ON LEFT

Definitions

Relative Incoming Mach Number:
$$w = -\frac{u_B}{A_B} = -\frac{(q_B - V_S)}{A_B}$$
 (II.1)

Equations

Q Riemann Variable Change:

$$\frac{Q_{A}^{-Q}B}{A_{B}} = \frac{2(w^{2}-1)}{(\gamma+1)w} + (\frac{2}{\gamma-1}) \left[\frac{A_{A}}{A_{B}}-1\right] - \frac{A_{A}}{A_{B}} \left[\frac{1}{\gamma(\gamma-1)}\right] \ln\left[(\frac{2\gamma}{\gamma+1})w^{2}\right] - (\frac{\gamma-1}{\gamma+1}) \left[(\frac{(\gamma-1)w^{2}+2}{(\gamma+1)w^{2}})^{\gamma}\right]$$
(II.2)

Speed of Sound Ratio:

$$\frac{A_{A}}{A_{B}} = \frac{1}{(\gamma+1)w} [2(\gamma-1)[1+\frac{\gamma-1}{2}w^{2}][\frac{2\gamma}{\gamma-1}w^{2}-1]]$$
 (II.3)

Pressure Ratio:

$$\frac{P_{A}}{P_{B}} = \frac{2\gamma}{\gamma + 1} w^{2} - \frac{\gamma - 1}{\gamma + 1}$$
 (II.4)

Density Ratio:

$$\frac{\rho_{A}}{\rho_{B}} = \frac{(\gamma+1)w^{2}}{(\gamma-1)w^{2}+2} \tag{II.5}$$

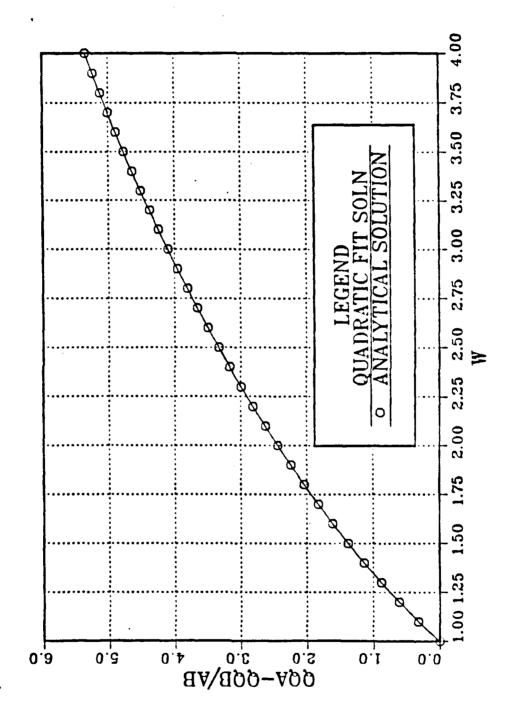
TABLE II (CONTINUED)

Velocity Change:

$$\frac{q_{A}^{-q_{B}}}{A_{B}} = \frac{2(w^{2}-1)}{(\gamma+1)w}$$
 (II.6)

Entropy Change:

$$S_{A} - S_{B} = -\left(\frac{1}{\gamma(\gamma - 1)}\right) \ln\left[\frac{2\gamma w^{2} - \gamma + 1}{\gamma + 1}\right] - \left(\frac{1}{\gamma - 1}\right) \ln\left[\frac{(\gamma - 1)w^{2} + 2}{(\gamma + 1)w^{2}}\right]$$
 (II.7)



Q, Extended Ricmann Variable Change with Mach Number Figure 2.5

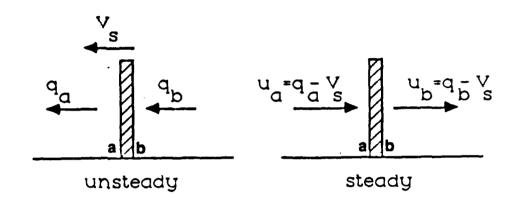


Figure 2.6 Shock Wave with High Pressure on Right

TABLE III

SHOCK EQUATIONS FOR HIGH PRESSURE ON RIGHT

Definitions

Relative Incoming Mach Number:

$$w = \frac{u_A}{A_A} = \frac{q_A - V_S}{A_A}$$
 (III.1)

Equations

R Riemann Variable Change:

$$\frac{R_{B}-R_{A}}{A_{A}} = \frac{2(1-w^{2})}{(\gamma+1)w} + (\frac{2}{\gamma-1})\left[1 - \frac{A_{B}}{A_{A}}\right] + \frac{A_{B}}{A_{A}}\left[\frac{1}{\gamma(\gamma-1)}\right] \ln\left[(\frac{2\gamma}{\gamma+1}, w^{2} - (\frac{\gamma-1}{\gamma+1})) \cdot (\frac{(\gamma-1)w^{2}+2}{(\gamma+1)w^{2}})^{\gamma}\right]$$
(III.2)

Speed of Sound Ratio:

$$\frac{A_{B}}{A_{A}} = \frac{1}{(\gamma+1)w} [2(\gamma-1)[1+\frac{\gamma-1}{2}w^{2}][\frac{2\gamma}{\gamma-1}w^{2}-1]]$$
 (III.3)

Pressure Ratio:

$$\frac{P_B}{P_A} = \frac{2\gamma}{\gamma + 1} w^2 - \frac{\gamma - 1}{\gamma + 1}$$
 (III.4)

Density Ratio:

$$\frac{\partial_{A}}{\rho_{B}} = \frac{(\gamma + 1)w^{2}}{(\gamma - 1)w^{2} + 2}$$
 (III.5)

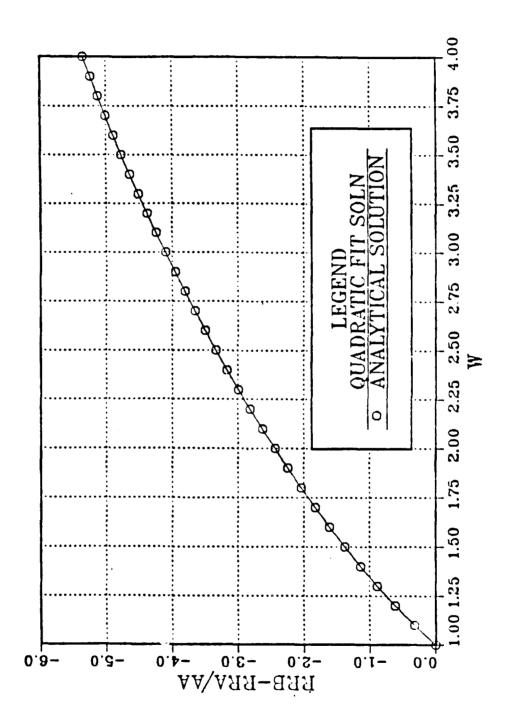
TABLE III (CONTINUED)

Velocity Change:

$$\frac{q_{B} - q_{A}}{A_{A}} = \frac{2(1 - w^{2})}{(\gamma + 1)w}$$
 (III.6)

Entropy Change:

$$S_{B}-S_{A} = -(\frac{1}{\gamma(\gamma-1)}) \ln \left[\frac{2\gamma w^{2}-\gamma+1}{\gamma+1}\right] - (\frac{1}{\gamma-1}) \ln \left[\frac{(\gamma-1)w^{2}+2}{(\gamma+1)w^{2}}\right]$$
 (III.7)



Extended Riemann Variable Change with Mach Number, High Pressure on Left Figure 2.7

An examination of equations (II.2) and (III.2) reveals that

$$\frac{R_B - R_A}{A_A} = - \left[\frac{Q_A - Q_B}{A_B} \right]$$

This is expected since in flow to the right, the Q extended Riemann variable is associated with the q+A characteristic. Also, since velocity is defined as positive to the right, q is positive. But for flow to the left, velocity is defined as negative, thus q is negative. Moretti [Ref. 3] showed that the downstream running Riemann variable (q+A characteristic) has a lower magnitude of discontinuity across a normal shock than the upstream running Riemann variable (q-A) characteristic), and is thus preferable. flow to the left, the Riemann variable associated with downstream is the R Riemann variable, though the characteristic associated with the R Riemann variable is q-4, in flow to the left q is negative and thus

$$q-A = -(|q| + A)$$
 (2.9)

Therefore, in fluid traveling left the R Riemann variable is used to find Mach Number, and in fluid traveling right the Q Riemann variable is used.

If the shock is between two nodes with no contact surface within the same interval, the method to calculate the Mach Number, w, is as follows:

- 1) The change in the appropriate extended Riemann variable across the interval is measured; R variable for flow left, and Q variable for flow right. Call this change, \(\Delta m\).
- 2) Use Δm in equation (2.7) or equation (2.8) for the appropriate flow to calculate w.
- 3) With equation (II.2) or equation (II.3), for flow right or left respectively, use w to calculate the analytical Riemann variable change, Δe .
- 4) If this exact value of Δe is not equal to Δm then calculate a new guess, Δg from

$$\Delta g_{i+1} = \Delta g_i + (\Delta m - \Delta e) \qquad (2.10)$$

and then repeat steps 2 to 4 until & equals &m.

Thus the correct value of w is determined, and shock corrections from the normal shock relations are valid. v_s is determined from equation (II.1) or equation (III.1) depending on flow direction. Flow direction will be initially determined by the side with high pressure. High pressure on the left means flow will travel to the right. Likewise, high pressure on the right means flow will travel to the left.

3. Contact Surface

A contact surface is a boundary between regions of flow which are different in composition or which have undergone different thermodynamic histories. Thus a contact surface is formed when the diaphragm is burst in a shock tube separating the gas initially in the driver from the gas initially in the driven tube [Ref. 6:pp. 23-29]. In a wave rotor, a contact surface would separate the combustor gases from the cooler inlet air. Contact surfaces are also caused by two shocks of opposite families colliding or a shock over taking a shock of the same family [Ref. 3:pp. 15-18].

Figure 2.8 illustrates the changes in physical properties through the contact surface in the shock tube problem. The gas to the right has been compressed and heated by the shock wave, with that to the left cooled and

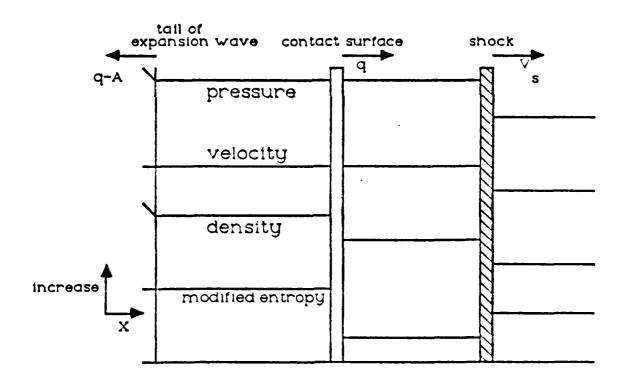


Figure 2.8 Behavior of Physical Properties Through a Contact Surface

expanded. The density, speed of sound, and modified entropy are discontinuous across the contact surface.

Since pressure is constant across the contact surface, using the perfect gas equation of state and the first law of thermodynamics it is shown in Appendix A for the shock tube problem that

$$A_{A}/A_{B} = \exp^{(\frac{(\gamma-1)}{2}(S_{B}-S_{A}))}$$
 (2.11)

Since the flow behind the contact surface to the tail of the rarefaction wave is isentropic, the value of S_B will be known. The value of S_A is the value of entropy behind the shock. Subtracting equations (I.4) and (I.5) from each other and dividing by entropy S_B , A_B can be determined. Thus the unknown speed of sound A_A is obtained from equation (2.11). With q_B equal to q_A , and S_A the Riemann variables just behind the contact surface are calculated from equations (I.4) and (I.5). For a contact surface traveling to the left it is only necessary to interchange the subscripts. The velocity of the contact surface is easily determined since it moves at velocity q along the q characteristic line associated with S. [Ref. 3:p. 16]

4. Contact Surface/Shock Interaction

When the shock and contact surface are within the same interval the calculation of the shock incoming Mach. Number, w, must be modified. Figure 2.9 shows a plot of the

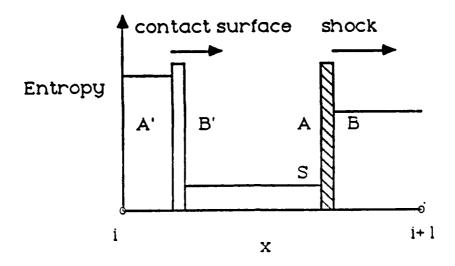


Figure 2.9 Modified Entropy Distribution for Shock and Contact Surface Traveling Right

modified entropy change across the interval. The use of the Riemann values at the nodes to estimate the Riemann variable change across the shock would be incorrect. The correct Riemann variable change would be, for flow to the right,

$$\Delta SK = \frac{Q_S - Q_B}{A_B}$$
 (2.12)

The correct Mach Number, w, is determined using the technique of Moretti modified for QAZ1D [Ref. 3:pp. 23-24].

Referring to Fig. 2.9, the technique for flow to the right is as follows:

- 1) Calculate w as if no contact surface were in the interval. With values at node i+1 known, determine S_B . Then use w and S_B in equation (II.7) to solve for S_A . This is the initial estimate of S_S . Let $S_{B'} = S_S$.
- 2) The Q Riemann Variable change across a contact surface is shown in Appendix A to be given by

$$A_{CS} = \frac{Q_{A'} - Q_{B'}}{A_{B}} = [e^{[(S_{B'} - S_{A'})(\frac{\gamma - 1}{2})]} S_{A'} - S_{B'}] \frac{A_{A}}{A_{B}}$$
 (2.13)

3) Define

$$\Delta m = \frac{Q_{A} \cdot Q_{B}}{A_{B}}$$
 (2.14)

then

$$\Delta m = \Delta SK + \Delta CS \tag{2.15}$$

can be solved to obtain Δ SK.

- 4) Using ΔSK as Δm in the shock iteration scheme given in Section II.C.2 calculate a new w.
- 5) With this new w and S_B use equation (II.7) to obtain a new S_A .
- 6) Compare S_A with S_S . If they are not equal to within an acceptable error, calculate a new estimate for S_S using

$$S_{i+1} = S_{i} + (S_{i} - S_{i})$$
 (2.16)

Iterate until convergence is achieved.

This will result in the proper w for a condition with shock and contact surface interacting.

For flow to the left, it is only necessary to interchange the subscripts A and B, and use

$$\frac{R_{B^{*}}-R_{A^{*}}}{A_{A}} = \left[\exp^{\left(\frac{(\gamma-1)}{2}(S_{A^{*}}-S_{B^{*}})}S_{B^{*}}-S_{A^{*}}\right]\left(\frac{A_{B}}{A_{A}}\right)}$$
(2.17)

for the extended Riemann Variable change. Figure 2.10 illustrates the left traveling condition.

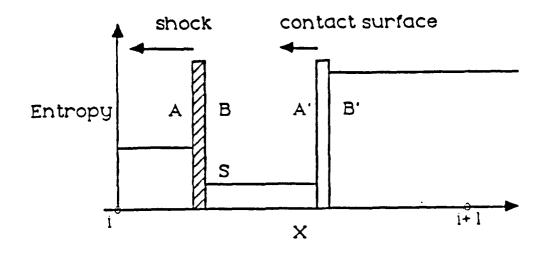


Figure 2.10 Modified Entropy Distribution for Shock and Contact Surface Traveling Left

D. BOUNDARY CONDITIONS

1. Open Boundary

At the open boundary, a reference pressure ratio, $P_{\text{ref}} = P_{\infty}/P_A \text{ is specified, where } P_{\infty} \text{ is the pressure to be}$ held at the boundary, and P_A is the pressure just inside the tube. Only the case where $P_{\infty} \leq P_A$ is considered. This means that an outflow condition at the boundary will result when $P_{\infty} < P_A$, with an expansion wave traveling in from the boundary. Thus locally at the boundary, conditions are isentropic.

The computational grid for the left boundary is shown in Fig. 2.11. A phantom node, L, is used outside the

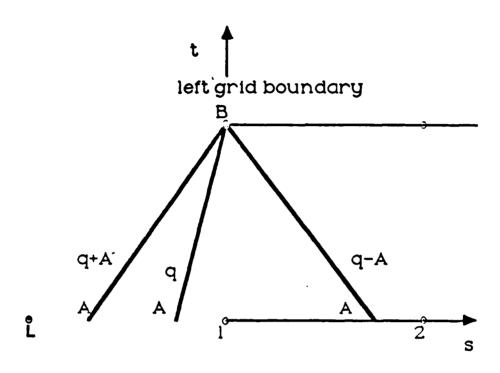


Figure 2.11 Left Boundary Computational Grid

computational mesh to enable simple enforcement of constant pressure and entropy at the mesh boundary node, 1.

The approach is to determine the required variables at node L, then transfer these values onto node 1, and vary q at the boundary to meet the required boundary conditions. First, using P_{ref} at node L and S at node 2 in equation (I.3) rewritten in the form

$$\rho_{R} = ((1/P_{ref}) (exp (y-1)) -1/y$$
(2.18)

 ρ_R , the density ratio at the boundary, is calculated. Using the perfect gas equation of state in equation (2.18) the temperature ratio, T_R is given by

$$T_{R} = (\rho_{R}^{(\gamma-1)}) (\exp^{(\gamma(1-\gamma)(S-\frac{2}{\gamma-1})})$$
 (2.19)

and can be calculated once ρ_R is known. With an initial velocity at the boundary, q_b , assumed the Riemann variables R and Q are determined for node L using

$$R = q_b - \sqrt{T_R} S \qquad (2.20)$$

and

$$Q = q_b + \sqrt{T_R} S \qquad (2.21)$$

Subtracting equation (2.20) from (2.21), and dividing by twice S yields A at node L, where $A = \sqrt{r_{RG}T}$. The values of R, Q, A, q_b , and S are now known at node L. These values are assigned to node 1, and the QAZ1D algorithm is applied to the boundary node as if it were an interior node. The result is an estimate of the new values for R, Q, and S at node 1. These are used to obtain a new estimate of the pressure ratio at node 1, call it P_{RN} . P_{RN} is compared with P_{ref} , and the new value of S with the old value of S at node 1. A new q_b is calculated by solving equations (2.20)

and (2.21) simultaneously. The process is repeated until entropy and pressure remain constant at the boundary. For the right-hand boundary, Fig. 2.12 shows the computational

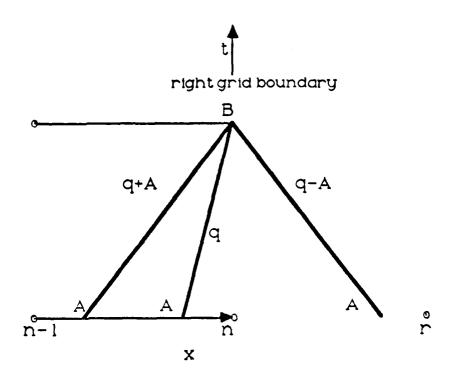


Figure 2.12 Right Boundary Computational Grid

grid with the phantom node, r, to the right of the mesh boundary node, n. The procedure for the right boundary is the same as for the left boundary.

When a shock travels across the open boundary, the boundary is first corrected using the method described in Section II.C.2. Subsequently, the pressure is returned to give the constant value specified for P_{ref} , using the above

procedure. The result will be an expansion wave traveling inward.

For supersonic flow, all of the variables are determined from values at the interior nodes [Ref. 1:p. 3].

2. Closed Boundary

The solid boundary is imposed by setting the velocity at the boundary, q, equal to zero. The same computational grid is used as that for an open boundary, but a different technique is used in assigning values to the phantom node. Referring to Fig. 2.11, the velocity at node 2, q_2 , is known. By setting

$$q_L = -q_2 \tag{2.22}$$

the wave impacting the boundary will be met by a wave of equal velocity but opposite in direction and will result in node 1 appearing as a solid boundary. Further, to facilitate the QAZ1D method, set

$$R_{L} = -Q_{2} \tag{2.23}$$

$$Q_{L} = |R_2| \qquad (2.24)$$

$$S_{L} = S_{2} \tag{2.25}$$

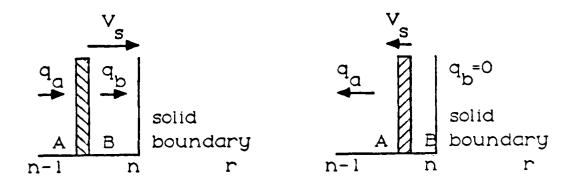
$$^{A}\mathbf{L} = _{2}A \qquad (2.26)$$

This will enable the computation of the new boundary node 1 values as an interior point with

$$q_1 = 0$$

The right boundary is handled in the same way.

Figure 2.13 illustrates the sequence of events when a shock reflects off a solid boundary on the right [Ref. 7:



- A) Shock Approaches Solid Boundary
- B) Shock Reflects Off Solid Boundary

Figure 2.13 Shock Reflecting at Solid Boundary

pp. 172-195]. Since the velocity behind the reflected shock, q_B , is zero, and the velocity in front of the shock, q_A , is known, the velocity gradient, Δq , over the shock is, in non-dimensionalized form, given by

$$\Delta q = (q_B - q_A)/A_A \qquad (2.27)$$

Rearranging equation (III.6), and using Y = 1.4 it can be shown that

$$w = \sqrt{1 + 0.36(\Delta q)^2} - 0.6\Delta q \qquad (2.28)$$

This is an exact analytical value for w based on stationary normal shock relations. The speed of sound ratio, ${}^A_B/{}^A_A$, is calculated from equation (III.3) and

$$A_{\mathbf{B}} = A_{\mathbf{A}} (A_{\mathbf{B}}/A_{\mathbf{A}}) \tag{2.29}$$

Entropy behind the shock, S_B , is determined from equation (III.7) since S_A is known. Then the extended Riemann variables, R and Q, behind the reflected shock are calculated from equations (I.4) and (I.5) respectively.

For a shock reflected from the left boundary, the subscripts A and B are interchanged and using equation (II.6) the Mach Number is given by

$$w = \sqrt{1 + 0.36(\Delta q)^2} + 0.6\Delta q \qquad (2.30)$$

The equations from Table II are used instead of those from Table III (used in the case of reflection from the right boundary), since the shock is now traveling from left to right.

III. FORTRAN PROGRAM E1DV2

A. GENERAL DESCRIPTION

Program E1DV2 is a Fortran computer program which calculates 1-dimensional unsteady flow based on the QAZ1D formulation and method of solution of the Euler equations of motion. The program has provisions for tracking in time the location of shock waves, contact surfaces and head and tail of the expansion waves. Its intended application to wave-roter design and analysis explains the present definition of node points and boundary conditions. In its current form, the code describes flow in a tube initiated by a diaphragm bursting. The location of the diaphragm, whether the flow is to the left or the right, and whether the ends of the tube are closed or open, can be varied.

The E1DV2 program is written in FORTRAN 77, and was developed using the IBM 3033 System 370 computer. The use of DISSPLA subroutines in plotting results requires compiling and executing using VS FORTRAN procedures. Appendix B describes the procedures for running the E1DV2 program on the Naval Postgraduate School IBM computer A listing of the code, which contains its own system. description in comment statements, is given in Appendix D.

The code incorporates:

- 1) first order accuracy
- 2) double precision numerics, except for single precision in graphical output
- 3) linear interpolation and extrapolation algorithms
- 4) quadratic polynomial approximations for curve fitting
- 5) non-dimensional variable input and output
- 6) structured subroutine format.

Table IV lists all the subroutines called from the main program and brief descriptions of their purposes. The extensive use of subroutines was intended to allow modifications and extensions of the code without major restructuring.

B. THE MAIN PROGRAM

The main program flowchart is illustrated in Appendix C, Fig. C.1. The conventions and a comprehensive list of variables are listed in the beginning of the program. The number of grid nodes is set by the user, and must be an odd number. Arrays are dimensioned to the number of nodes in the main program prior to compiling and executing.

Initial values for temperature, pressure, and density ratios at the diaphragm and boundaries are entered by editing. Also, the initial velocity distribution on each side of the diaphragm is set, and as well as the ratio of specific heats. The side with the high pressure is identified. Boundaries are set either closed or open. In the

TABLE IV

SUBROUTINES

TIME	Calculates minimum time step
TRAK	Tracks discontinuities, calculates shock mach number, w
SWEEP	Advances node values to next time step
COND1	Calculates interpolated values of Riemann variables, $\partial q/\partial s$, and $\partial A/\partial s$ when no shock or contact surface within an interval
COND2	Calculates interpolated values of Riemann variable, $\partial q/\partial s$, and $\partial A/\partial s$ when discontinuity within interval to right of node or flow is supersonic to the right
COND3	Calculates interpolated values of Riemann variable, $\Re/\Im s$, and $\Im A/\Im s$ when discontinuity within interval to left of node or flow is supersonic to the left
COND4	Called when node is jumped by discontinuity to load node information into array for use in subroutine CORRCT
COND5	Calculates interpolated values of Riemann variable, $\frac{\partial q}{\partial s}$, and $\frac{\partial A}{\partial s}$ when discontinuity on either side of node and flow is supersonic
COND6	Would contain subroutine to advance node when contact surface is in front of shock after intersecting and traveling in same direction. Not currently in use
COND7	Would contain subroutine to solve precisely when and where shock and contact surface would intersect within an interval. Not currently in use
COND7N	Would contain subroutine to solve precisely when and where shock and contact surface would intersect if either were jumping a node simultaneously. Not currently in use

TABLE IV (CONTINUED)

COND7S	Would contain the subroutine to solve the Riemann problem of shock and contact surface intersecting. Not currently in use
COND8	Would contain subroutine to advance node after shock and contact surface have crossed and are moving apart. Not currently in use
CORRCT	Advances nodes jumped by discontinuity to next time step
DELTAX	Determines relative location of discontinuity within an interval
SKJUMP	Calculates variable change across a normal stationary shock
CSJUMP	Calculates variable change across a contact surface
EXTRAP	Extrapolates entered values
INTERP	Interpolates entered values
DBURST	Calculates initial Riemann values at node where diaphragm is located
BONDRY	Calculates values to update left and right boundary
SRFLCT	Calculates new shock parameters when shock reflects off solid boundary
BBDRY	Alternate interpolating scheme near boundary
BORDER	Sets graphical borders
PLOT	Plots q, S, P, and ρ
EXACT	Plots exact p versus calculated p
LIST	Lists calculated values in files 8, 9, 10

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open case, either constant pressure, or an adjustable pressure is specified. The latter case in effect extends the tube, and allows discontinuities to disappear out of the tube without creating expansion or compression waves. Exact values for velocities of expansion wave, shock, and contact surface, and density ratio are specified by the user in the input section.

Output is controlled by setting the variable GRAPHS to either 0, 1, or 2. A zero creates three files which contain data calculated at the time the call to subroutine LIST is made. A value of 1 causes plots of pressure, density, velocity, and entropy distributions to be created. When GRAPHS equals 2 a plot of the exact density distribution along with the calculated density distribution is made. Calls to output routines are determined by the parameter, SKIP, the number of time steps between calls, which is specified by the user.

Program termination can occur for several reasons. First, the program terminates when a maximum number of time steps, JSTOP, is reached. JSTOP is specified by the user. Second, the program terminates if, during execution, any of the following conditions are met:

- 1) The shock intersects with the contact surface
- 2) The pressure at any open boundary is higher than the pressure at the first node inside the boundary
- The shock exits an open boundary.

In these cases a message is displayed on the terminal describing the reason for termination.

C. THE SUBROUTINE PROGRAMS

1. The "DBURST" Routine

Figure C.2 in Appendix C shows the flowchart for "DBURST". The assumption that a shock and contact surface are formed immediately causes oscillating numerical solutions that dampen within five to ten time steps. By mathematically "bursting" the diaphragm prior to time zero, a solution at the node where the diaphragm is located can be determined at time zero. The result is a more accurate representation of the wave structure and a dampening of a reduced transient solution within three time steps. "DBURST" calculates the Riemann variables that would exist behind a shock and contact surface that have moved an infinitesimal amount after the diaphragm burst, and assigns them to the node where the diaphragm was situated.

2. The "TIME" Routine

The "TIME" subroutine was not changed from that developed by Salacka [Ref. 2:p. 35]. The purpose is to compute the maximum allowable time step but ensuring that all characteristic trajectories over the time step are within one interval between nodes. The time step is determined from

at every node, and the minimum time step is used.

3. The "TRAK" Routine

This routine computes the new locations of shock, contact surface, and head and tail of the expansion wave after the time step, DELT, calculated in "TIME." Appendix C, Fig. C.3 shows the flowchart for the "TRAK" subroutine. The shock velocity, Vs, incoming Mach Number, w, and pressure, density, and sonic velocity ratios PR, DR, and AR respectively are determined. The equations for flow left and right are the same, except for DQ, the velocity gradient, which is different only by sign. Thus by proper bookkeeping the same equations are coded once and used in either direction. The initial direction of the shock and contact surface are set from code that interprets which side has the high pressure at time zero. The contact surface speed is determined after the shock speed is established. The situation at time zero is handled as in "DBURST" to ensure that the shock/contact surface interaction properly modeled. Since there is a certain transient solution that decays after three time steps, tracking of the expansion wave is not initiated until then.

The head of the expansion wave travels at a velocity corresponding to q+A, and the tail with speed q-A. In the case of flow traveling to the left, this is reversed.

4. The "SWEEP" Routine

The "SWEEP" subroutine solves equation (2.5) and updates the values of variables at the nodes, including the boundary nodes. Appendix C, Fig. C.4 shows the "SWEEP" flowchart. Only those nodes which have been crossed by a discontinuity during the time step are updated by the "CORRCT" subroutine. Section II.B describes the theory coded into "SWEEP". The routine begins at the left boundary node and progresses to the right boundary node, one node at a time. Figure 3.1 illustrates the overall algorithm applying the QAZID method. At the boundary nodes, the

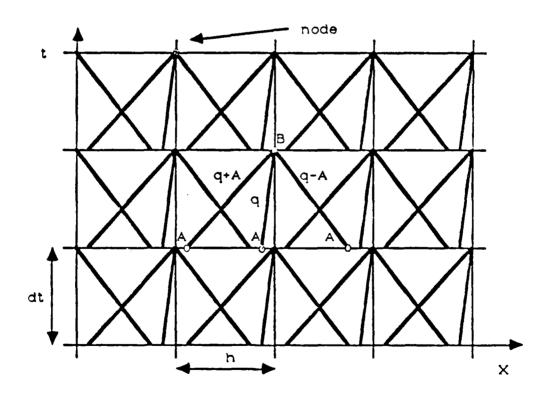


Figure 3.1 Overall Algorithm for QAZ1D Method

"BONDRY" subroutine is called and returns the updated values at those nodes. In between, the correct and most effective algorithm to update the node is determined. These algorithms are coded into eight different condition subroutines. These routines calculate the interpolated Riemann variables associated with the three characteristics (q+A, q, and q+A), plus the spatial derivatives at $\partial q/\partial s$ and $\partial A/\partial s$. This allows "SWEEP" to calculate Δw and \overline{z} . The integral of \overline{z} is then determined, and the update for the variables of that node in ∂w are computed. ∂w is stored until the entire mesh has been swept. Then the variable arrays (\overline{w}) are updated to the next time interval.

To choose the proper condition routine, the following information about conditions in the interval on either side of the node are expressed in two 3 digit integer variables, SHOCK and CNTACT. The value of these variables provide a code for the following information:

- SHOCK--The existence of a shock within an interval, and, if so, the direction of travel, and if the shock will cross the node in front of it within the current time step.
- CNTACT-The existence of a contact surface within an interval, and, if so, the direction of travel, and if the contact surface will cross the node in front of it within the current time step.

Figure 3.2 illustrates the regions around a node. Table V lists the values that SHOCK and CNTACT may have, and their meaning. Figures 3.3, 3.4, and 3.5 illustrate examples of what different SHOCK and CNTACT values mean. At each node

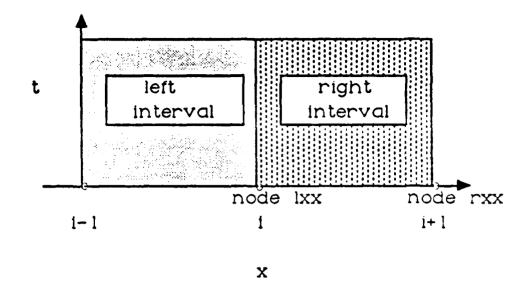


Figure 3.2 Interval and Node Description used in "SWEEP"

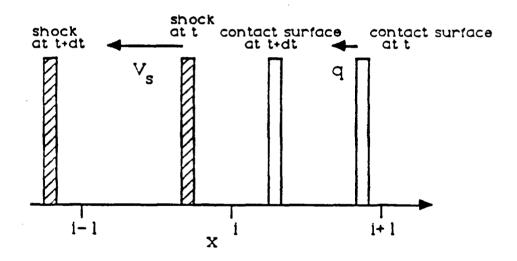


Figure 3.3 Schematic of SHOCK = 331 and CNTACT = 232

TABLE V VALUES OF PARAMETERS SHOCK AND CNTACT

SHOCK

<u>Value</u>	Located in interval on	Direction of travel	
100	No Shock	N/A	N/A
321	Left	Right	Yes
322	Left	Right	No
331	Left	Left	Yes
332	Left	Left	No
221	Right	Right	Yes
222	Right	Right	No
231	Right	Left	Yes
232	Right	Left	No
		CNTACT	
100	No contact surface	N/A	N/A
321	Left	Right	Yes
322	Left	Right	No
331	Left	Left	Yes
332	Left	Left	No
221	Right	Right	Yes
222	Right	Right	No
231	Right	Left	Yes
232	Right	Left	No

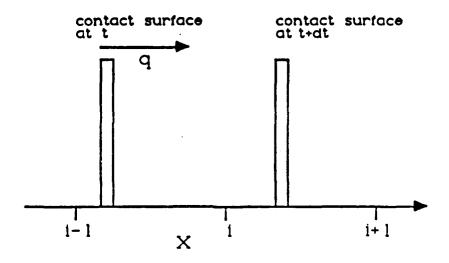


Figure 3.4 Schematic of SHOCK = 100 and CONTACT = 321

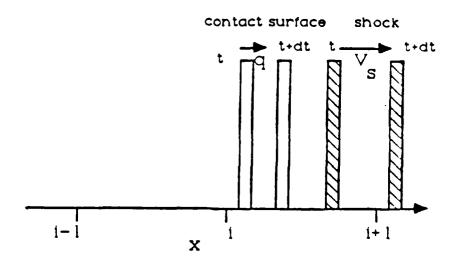


Figure 3.5 Schematic of SHOCK = 221 and CNTACT = 222

the code examines the shock and contact surface condition, along with relative location of the shock to a contact surface if both exist near the node, if the flow is supersonic or subsonic at the node, and the direction the flow is traveling. The appropriate algorithm is determined and called in the form of a condition subroutine.

The "SWEEP" routine is designed to handle all possible shock and contact surface combinations. Because the code does not solve the situation where the shock and contact surface intersect, as illustrated in Fig. 3.6, then any combinations after the shock and contact surface have crossed call condition routines that currently contain only messages. The code was intentionally prepared to be easily extended to treat the intersection of the shock and the contact surface, and beyond.

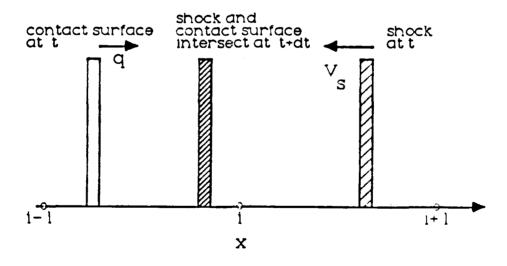


Figure 3.6 Schematic of SHOCK = 231 and CNTACT = 322

5. The "Condition" Subroutines

The ten subroutines that are called by "SWEEP" to calculate the interpolated values of the extended Riemann variables, R and Q, plus S, $\partial q/\partial s$, and $\partial A/\partial s$ are COND1, COND2, COND3, COND4, COND5, COND6, COND7, COND7S, COND7N, and COND8. The procedure used in COND1, COND2, COND3, and COND5 is that of Salacka [Ref. 2:pp. 36-37] modified to account for contact surfaces. Appendix C, Fig. C.5 is a general flowchart for these four routines. Essentially, an initial estimate is made of the characteristic slopes, \(\cdot\), by enforcing the principle of domain of dependence. The assumption is made that the slopes are linear, and that the characteristics pass through point B, as defined in Fig. 3.7. Then q and A are computed at point A, which in turn yields a second estimate of the characteristic slope, \(\lambda\).

The two slopes for each characteristic are compared. If they are not equal to within an acceptable error, the new estimate of \(\cdot\) is used to repeat the process until convergence is achieved. All three characteristics are handled simultaneously. The value of

$$\Delta s = \lambda \cdot \vartheta t \tag{3.2}$$

is then determined for each characteristic q+4, q, and q-4. This allows linear interpolation of Q, R, and S at point A. The spatial derivatives, $\partial Q/\partial S$ and $\partial A/\partial S$ are computed from

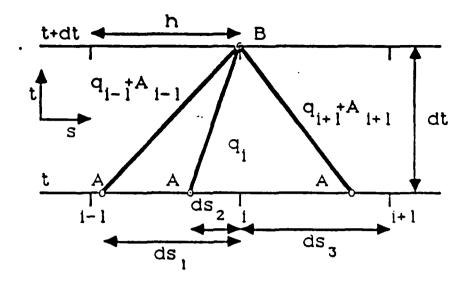


Figure 3.7 Computational Method for COND1 Routine

the values of q and A used in the estimate of the initial characteristic slopes.

The "COND1" subroutine is used when there are no contact surfaces or shocks within the interval on either side of the node, and flow is subsonic. The q+A characteristic uses forward differencing, while the q-A characteristic uses a backward differencing scheme to keep the initial domain of dependence of the numerical scheme outside the physical domain of dependence.

The "COND2" subroutine is a backward differencing algorithm used in situations when one or more discontinuities are in the right interval, or if flow is supersonic to the right. Fig. 3.8 illustrates the computational method

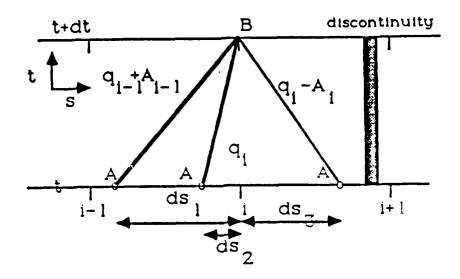


Figure 3.8 Computational Method for COND2 Routine

for "COND2". The characteristic slopes of q+A and q are handled as in "COND1", but the q-A characteristic slope is determined by a backward rather than a forward scheme. To interpolate between node i and i+1 would be incorrect because of the discontinuity in the values between them. The value of parameters in the right interval are interpolated from values in the left interval by assuming the derivatives do not change between the intervals up to the discontinuities (i.e., a shock and/or a contact surface).

The "COND3" subroutine is a forward differencing algorithm used in situations when one or more discontinuities are in the left interval, or if flow is supersonic traveling to the left. Figure 3.9 shows the computational

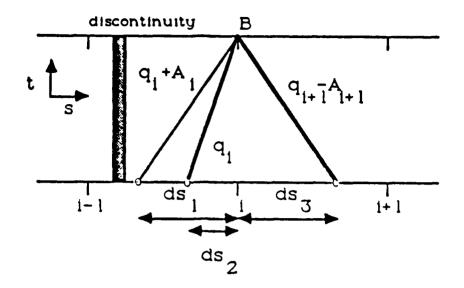


Figure 3.9 Computational Method for COND3 Routine

method for "COND3". The method is similar to that in COND2 but the q+A characteristic slope has to be interpolated from values of node i instead of node i-1 using a forward difference scheme. The characteristic slope for q-A and q are estimated by forward difference schemes using values of node i+1 and i respectively.

For conditions, such as that illustrated in Fig. 3.10, where a discontinuity is in the interval opposite the direction of supersonic flow then COND5 subroutine is called. A mix of COND2 and COND3 is used. For flow to the right the method of COND2 is implemented, while flow to the left is the same as for COND3.

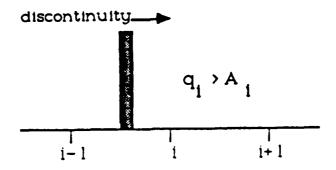


Figure 3.10 Example Condition for "COND5" Routine

Subroutine "COND4" is called whenever a node is to be crossed by a discontinuity from either direction. The flowchart for "COND4" is shown in Appendix C, Fig. C.6. Two integer vector arrays, LNODE and RNODE, are used to store the following information on the node being crossed.

- A) the node number, I
- B) the value of SHOCK
- C) the value of CNTACT
- D) the current value of the integer time step, J The information is used in "CORRCT" to update the node to the next time level. In the current code the maximum number of nodes that can be crossed during any time step is two. Figure 3.11 shows an example of this situation, and defines the assignment of values. Because the nodes are swept from left to right, the left-most node is assigned to LNODE, while RNODE applies to any node crossed to the right of the LNODE node. The values of \hat{W} are set to zero, so

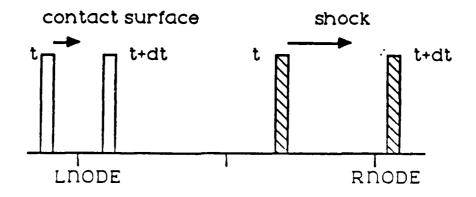


Figure 3.11 Example of "COND4" Routine Situation

that these nodes are skipped when updating occurs in "SWEEP". The main program interprets the value of J in LNODE and RNODE to determine if zero, one, or two nodes need to be corrected in "CORRCT". If zero nodes are crossed during a time step then "CORRCT" is not called.

The "COND6" and "COND8" subroutines are designed for future extensions of the entire code. Until the Rieman's problem illustrated in Fig. 3.6 is coded, then any situation after the shock and contact surface intersect cannot be computed. However, "SWEEP" is already coded to call "COND6" for the situation illustrated in Fig. 3.12, or its mirror image. "COND8" would be called for all the other situations after the shock and contact surface interaction has taken place. Currently, both subroutines output messages on the screen describing the situation, and set HALT equal to 1 to terminate the program.

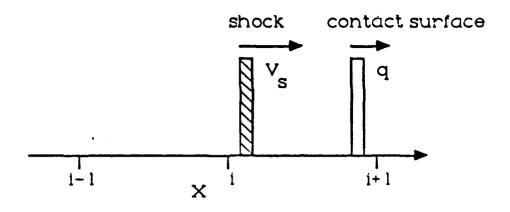


Figure 3.12 Example of "COND6" Situation

The "COND7", "COND7N", and "COND7S" subroutines are all related to each other. They are intended to contain code that would facilitate the shock and contact surface intersection and solve the resulting Riemann problem. "COND7" routine is called when the contact surface and shock moving in opposite directions would cross in a time step within an interval. The routine would calculate when and where within the time and space domain the intersection would occur based on the known velocity of each discontinuity and their current locations. This new time could then be used to rerun "SWEEP" with the shock and contact surface exactly on top of each other at the end of the new time step. The "COND7N" routine is for the same situation, but when a node is crossed by either discontinuity during the same time step. The same procedure is done, with the requirement to ensure the node crossed is properly updated

by "CORRCT" during the new time step. The "COND7S" routine is called when a shock and contact surface are located at the same point at a time other than zero. The subroutine would contain the code to solve the Riemann problem set up by "COND7N" or "COND7" routines.

6. The "CORRCT" Routing

Appendix C, Fig. C.7 shows the flowchart for "CORRCT". The "CORRCT" routine corrects nodes that have been crossed by a discontinuity (i.e., a shock or a contact surface) or are straddled by both. The routine takes the information from LNODE and RNODE arrays to determine which node or nodes are to be updated, and if there is any shock and contact surface interaction at the nodes. Then, using subroutines "DELTAX", "SKJUMP", "CSJUMP", "EXTRAP", "INTERP", and "BBDRY" the concepts from Section II are imposed to calculate the jump in the parameters R, Q, S, A and q at the node in question to the new time level.

7. The "BONDRY" Routine

The "BONDRY" routine computes the new values of the parameters Q, R, and S at the boundary nodes for time step t. The concepts of Section II for an open or closed boundary are coded as shown in the flowchart of "BONDRY" given in Appendix C, Fig. C.8. The routine uses the "COND1", "COND2", or "COND3" routines to calculate the correct w, and then solves for w the same as in "SWEEP". If a shock crosses an open boundary node during a time step,

then "SKJUMP" routine is used to calculate the values behind the shock at the node.

8. The "SRFLCT" Routine

The "SRFLCT" subroutine is called to calculate the values of Q, R, S, q and A at the boundary node when a shock reflects from a solid boundary. Appendix C, Fig. C.9 shows the flowchart of "SRFLCT" which codes the analysis in Section II.D.2 for closed boundary shock reflection. The time for the shock to reach the solid boundary, ∂t_W , is computed. Then the excess time in the time step, ∂t_N is given by

$$\partial t_{ex} = \partial t - \partial t_{w}$$
 (3.3)

After the new shock velocity, V_s , is calculated, then the new location of the reflected shock is known from multiplying V_s by $\Im\, t_{ex}$ and adding or subtracting from the boundary location.

9. The "DELTAX" Routine

The "DELTAX" subroutine is used in "CORRCT" and "BONDRY" to calculate the location within an interval of a discontinuity in terms of x. Figure 3.13 defines the various displacements which are calculated.

10. The "SKJUMP" Routine

The "SKJUMP" subroutine computes the conditions downstream of a stationary normal shock as described in

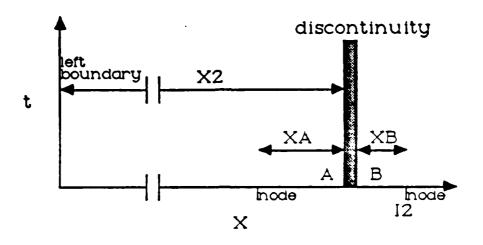


Figure 3.13 Discontinuity Location within an Interval

Section II.D.2. The "CORRCT", "TRAK", and "BONDRY" subroutines call "SKJUMP" when required, to obtain the speed of sound (A), entropy (S), and velocity (q) behind the shock.

11. The "CSJUMP" Routine

The "CSJUMP" subroutine computes the velocity and speed of sound change across a contract surface as described in Section II.D.3. The "CORRCT" and "TRAK" routines call "CSJUMP".

12. Numerical Support Routines

The "EXTRAP", "INTERP", and "BBDRY" routines are used by "CORRCT", "BONDRY", "TRAK", and "DBURST" to extrapolate or interpolate data to the face of a discontinuity or point. In particular, "BBDRY" is an interpolation routine used within an interval near a boundary.

13. The Output Routines

The four output subroutines used are those developed by Salacka [Ref. 2:pp. 39-40]. The "BORDER" and "PLOT" routines output plots of pressure, velocity, density, and modified entropy distributions versus a non-dimensionalized tube length at preset time intervals. "EXACT" creates a plot of the exact density distribution at selected points and compares it with the computed density distribution for a selected time step. The "LIST" routine outputs to files 8, 9, and 10 tabular listing of computed data. The files are sent to the user's permanent storage disk.

A value of GRAPHS equal to one causes "BORDER" to be called in the main program. This defines plot axis, labels, and headings. "PLOT" is then called once at time zero, and at every time step set by SKIP.

If GRAPHS is set equal to two, then "EXACT" is called every SKIP time steps to plot six exact density values and the computed density distribution. The six exact points are:

- A) The two boundary points
- B) The head and tail of the rarefaction wave
- C) . A point just behind the contact surface
- D) A point just behind the shock.

The location of the exact values is based on elapsed time and known exact values for wave velocities entered with the initial conditions for the problem.

"LIST" routine is called every SKIP time steps when GRAPHS is equal to zero. File 9 contains a tabular listing of the Riemann variables, modified entropy, pressure, density and velocity distributions, elapsed time, discontinuity velocity and location. File 10 is a tabular listing of the location of the shock, contact surface, and the head and tail of the expansion wave computed at every SKIP time steps. File 8 contains the exact values of the location of the shock, contact surface, and the head and tail of the expansion wave.

IV. RESULTS

Four test cases were run using the E1DV2 code. The purpose was to verify the ability of the code to determine the unsteady flow process and correctly simulate varying boundary conditions and flow directions in the Riemann shock tube problem. The shock tube is illustrated in Fig. 4.1 with the high pressure on the left. The tube is divided into two sections by a diaphragm. When the diaphragm is burst, the pressure equalizes through a shock wave traveling into the expansion chamber, and an expansion or rarefaction

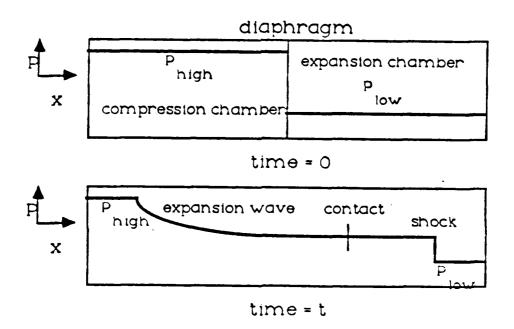


Figure 4.1 Shock Tube at t = 0 and t = t

wave traveling into the compression chamber. A contact discontinuity is behind the shock wave, traveling at the particle velocity [Ref. 6:p. 30].

A. TEST CASE 1

Test Case 1 was designed to demonstrate shock reflection and expansion wave reflection at solid boundaries. Test Case 1 had the following initial and boundary conditions:

- Pressure and density ratios equal to five, with high pressure on the left
- 2) Temperature ratio equal to unity
- 3) Both boundaries were closed
- 4) Diaphragm was located at x = 0.5
- 5) Computational mesh had 101 nodes
- 6) Maximum time step, JSTOP, = 109, with SKIP = 18.

Plots of the results obtained for the pressure, density, velocity, and modified entropy distributions are shown in Fig. 4.2 and Fig. 4.3. Fig. 4.2 shows the computation up to time step 55, while Fig. 4.3 takes the computation from time step 56 to termination. The output of "EXACT", a plot of the exact density compared with the computed density distribution is shown in Fig. 4.4. Fig. 4.5 illustrates the spatial location versus time for exact and computed shock, contact surface, and head and tail of the expansion wave. Data for Fig. 4.5 were taken from file 10 and file 8. Fig. 4.6 shows plots of pressure, density, modified entropy, and velocity distributions for the same initial and boundary

SHOCK TUBE RESULTS
FIRST ORDER N -101
DENSITY RATIO - 5.0 TEMP RATIO - 1
PRESSURE RATIO - 5.0

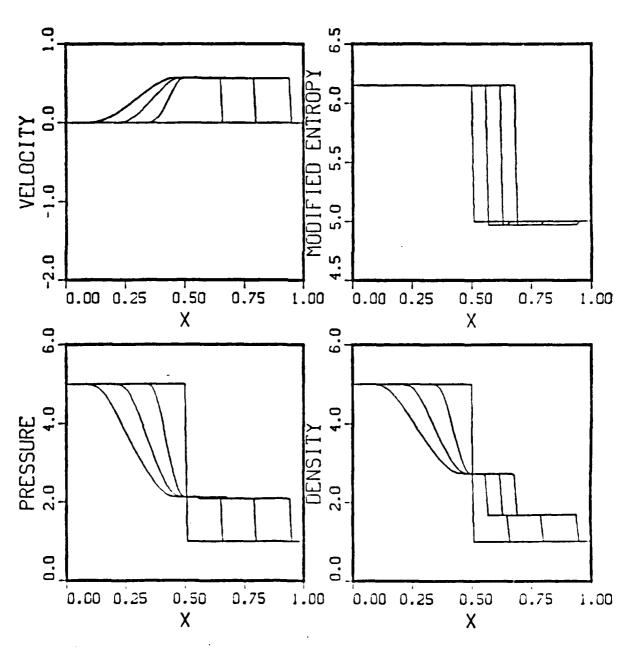


Figure 4.2 Test Case 1 (J = 1 to J = 55)

SHOCK TUBE RESULTS FIRST ORDER N -101 DENSITY RATIO - 5.0 TEMP RATIO - 1 PRESSURE RATIO - 5.0

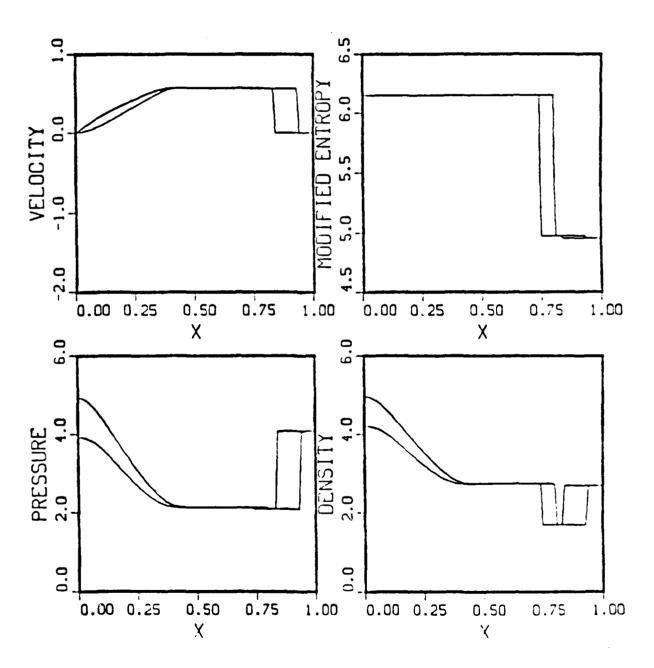


Figure 4.3 Test Case 1 (J = 56 to J = 109)

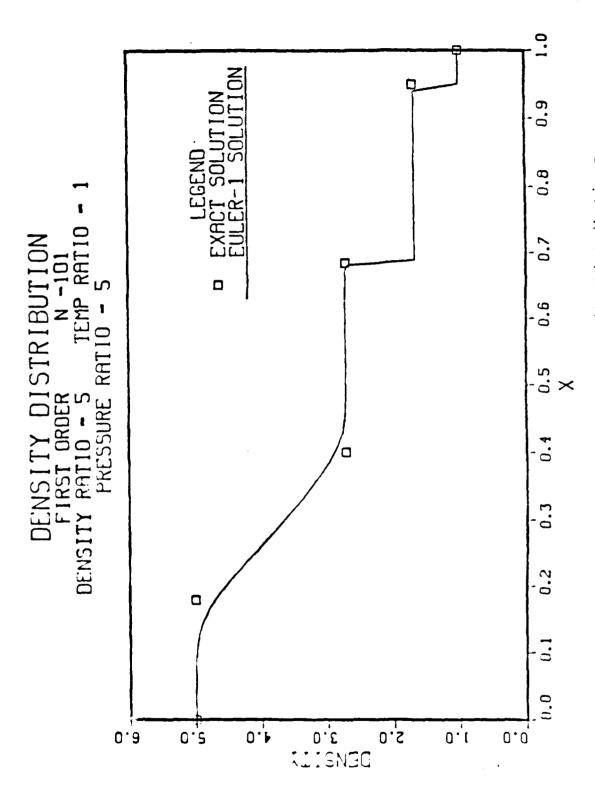
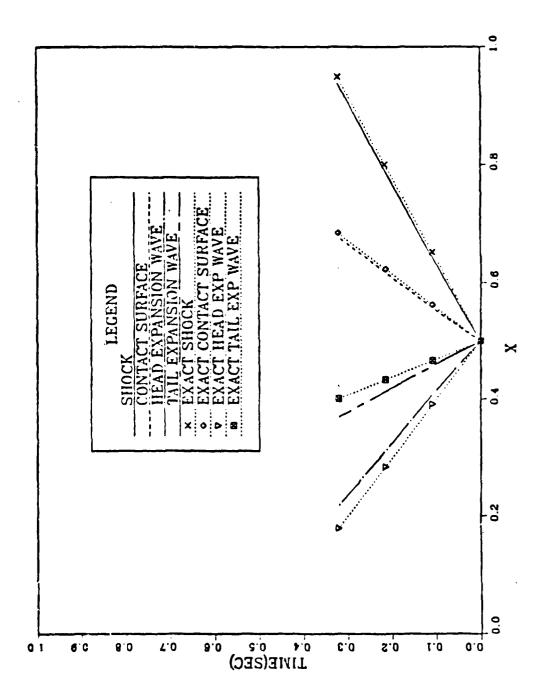


Figure 4.4 Exact and Computed Density Distributions



Location of Discontinuities versus Time (Test Case 1)

SHOCK TUBE RESULTS

FIRST ORDER N -101

DENSITY RATIO - 5.0 TEMP RATIO - 1

PRESSURE RATIO - 5.0

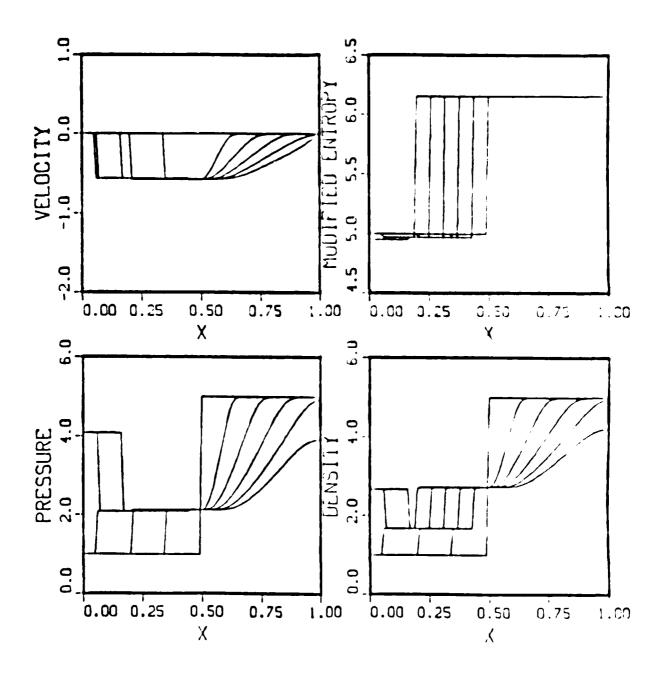


Figure 4.6 Test Case 1, High Pressure on Right

conditions but with high pressure on the right. Figure 4.6 includes data corresponding to those in both Fig. 4.2 and Fig. 4.3 for the high pressure initially on the left.

B. TEST CASE 2

Test Case 2 was to demonstrate an open boundary, constant pressure, expansion wave interaction. The test case was run with the following initial and boundary conditions:

- Pressure and density ratios equal to 5.), with high pressure on the left
- 2) Temperature ratio equal to unity
- The left boundary was open, with a constant pressure ratio across the boundary of 4,5
- The right boundary was open, with an adjustable pressure ratio that in effect extended the length of the tube
- 5 The diaphragm was located at x = 0.74
- 5 Computational mesh had 51 nodes
- Maximum time step, JSTOP, = 07, 3KIP = 9.

Plots of the results for the pressure, density, velocity, and modified antropy distributions are shown in Fig. 4.7. The test case was rerun with high pressure on the right. Figure 4.3 shows the results for pressure, density, and temperature ratios the same. The diaphragm was then at κ = 0.26. Boundary conditions were reversed. The same computational mesh, and output control were used.

SHOCK TUBE RESULTS

FIRST ORDER N - 51

DENSITY RATIO - 5.0 TEMP RATIO - 1

PRESSURE RATIO - 5.0

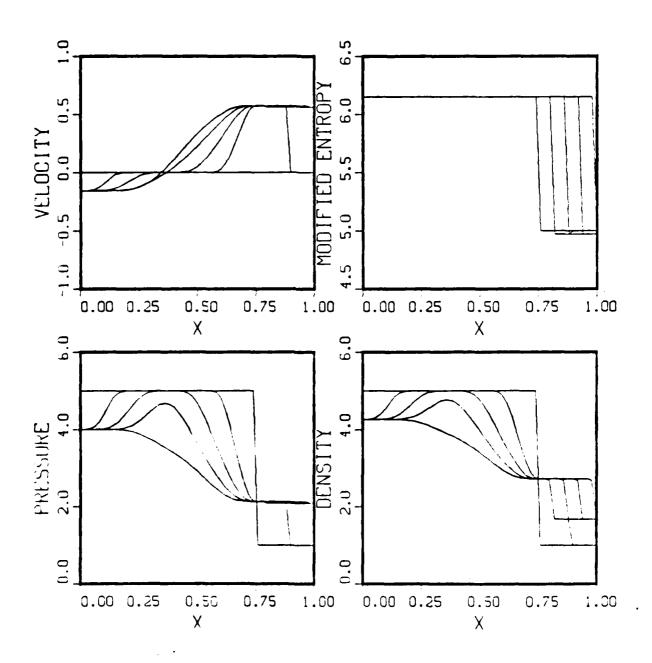


Figure 4.7 Test Case 2, High Pressure on Left

SHOCK TUBE RESULTS

FIRST ORDER N - 51

DENSITY RATIO - 5.0 TEMP RATIO - 1

PRESSURE RATIO - 5.0

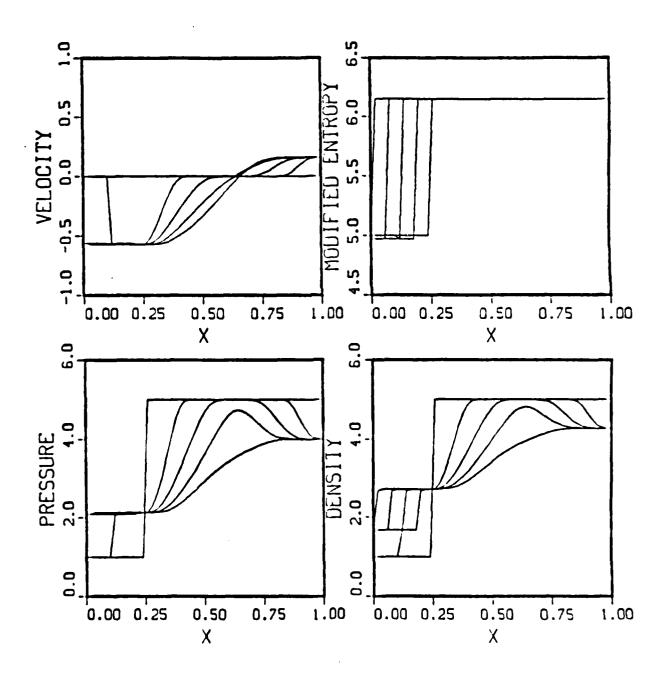


Figure 4.8 Test Case 2, High Pressure on Right

C. TEST CASE 3

Test Case 3 was designed to demonstrate a shock exiting an open boundary with constant pressure maintained at the boundary itself. The following initial and boundary conditions were set:

- 1) Pressure and density ratios equal to 5.5, with high pressure on the left
- 2) Temperature ratio equal to unity
- 3) Left boundary was closed
- 4) Right boundary was open with a constant pressure ratio across the boundary of unity
- 5) Diaphragm was located at x = 0.5
- 6) Computational mesh had 101 nodes
- 7) Maximum time step, JSTOP, = 73, with SKIP = 18.

Figure 4.9 shows plots of the results obtained for pressure, density, modified entropy, and velocity distributions. Similarly, Fig. 4.10 shows results obtained by putting the high pressure on the right, reversing the boundary conditions, and holding everything else the same.

D. TEST CASE 4

Test Case 4 was designed to demonstrate a lower pressure ratio, with shock wave reflection. The initial and boundary conditions were set as follows:

- 1) Pressure and density ratios equal to 3.2, with high pressure on the left
- 2) Temperature ratio equal to unity
- 3) Both boundaries were closed

SHOCK TUBE RESULTS
FIRST ORDER N -101
DENSITY RATIO - 5.5 TEMP RATIO - 1
PRESSURE RATIO - 5.5

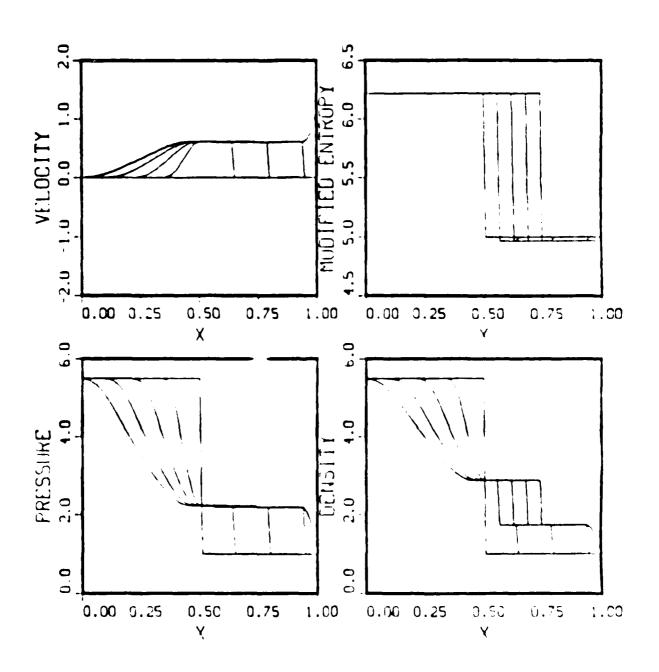


Figure 4.9 Test Case 3, High Pressure on Left

SHOCK TUBE RESULTS
FIRST ORDER N -101
DENSITY RATIO - 5.5 TEMP RATIO - 1
PRESSURE RATIO - 5.5

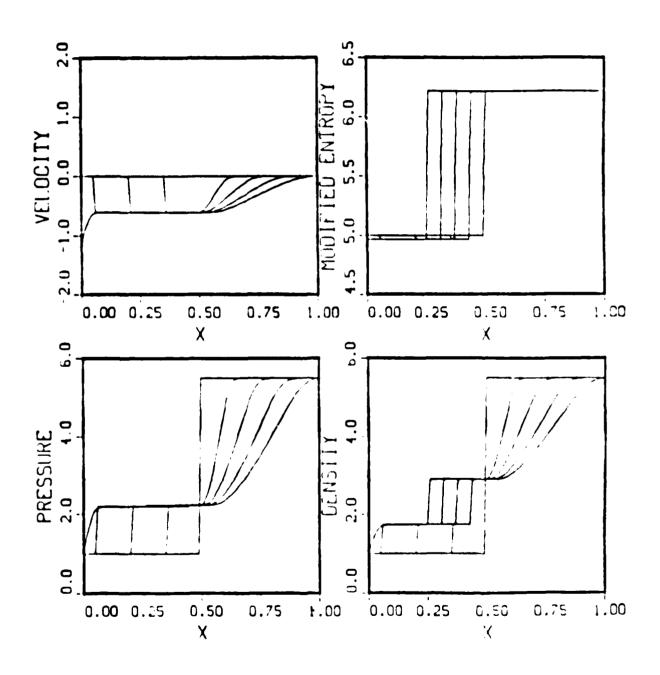


Figure 4.10 Test Case 3, High Pressure on Right

- 4) Diaphragm was located at x = 0.5
- 5) Computational mesh had 901 nodes
- 6) Maximum time step, JSTOP, = 601, with SKIP = 150.

 Plots of the results obtained for the pressure, density, modified entropy, and velocity distributions are given in Fig. 4.11. Figure 4.12 shows the results obtained with the high pressure to the right, SKIP = 200, and holding all other parameters constant.

SHOCK TUBE RESULTS

FIRST ORDER N -901

DENSITY RATIO - 3.2 TEMP RATIO - 1

PRESSURE RATIO - 3.2

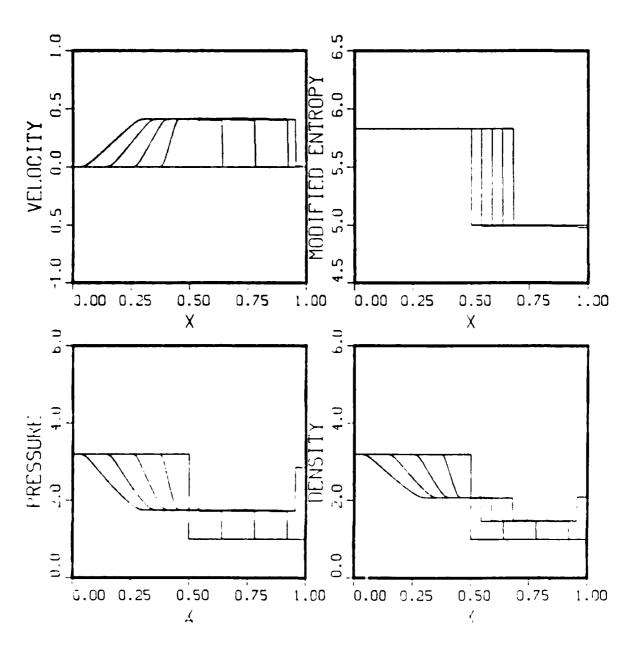


Figure 4.11 Test Case 4, High Pressure on Left

SHOCK TUBE RESULTS

FIRST ORDER N -901

DENSITY RATIO - 3.2 TEMP RATIO - 1

PRESSURE RATIO - 3.2

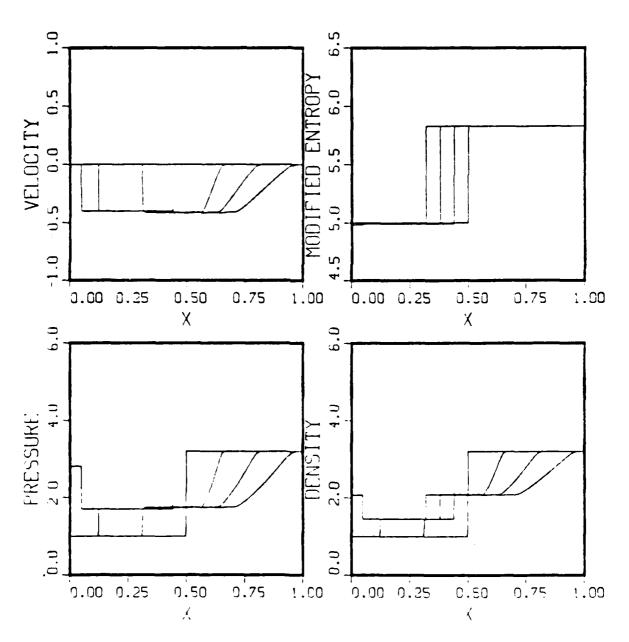


Figure 4.12 Test Case 4, High Pressure on Right

V. <u>DISCUSSION</u>

A. RESULTS OF TEST CASES

Overall, in the four specific test cases which were run, the expected qualitative flow behavior was produced by the code. Quantitatively, either experimental data or further exact solutions are needed to fully validate the computations. The results of each test case will be discussed separately.

Test Case 1 results in Fig. 4.2 show the formation of a well-defined shock wave traveling to the right, with the contact surface crisply defined following along behind. The entropy drops sharply across the shock and remains constant to the contact surface and then jumps to a steady, constant value to the left boundary as expected. Pressure and velocity remain constant through the contact surface. Velocity is positive since flow is to the right. expansion wave is smeared from head to tail over the correct range. Figure 4.3 is a continuation of the flow problem with a sequential display of the results. The entropy continues to drop as the reflected shock travels back toward the contact surface. Notice that the velocity behind the shock is zero. At the left boundary as the head of the expansion wave reflects, pressure and density continues to drop while velocity is zero at the boundary. The density

distribution shows that the contact surface and shock are about to cross. The program terminated and issued a message before the next output call was made, when the code determined that the contact surface and shock would cross. The exact density distribution compared with the compared density distribution in Fig. 4.4 clearly shows the shock and contact surface are modeled very accurately with a medium mesh. The expansion process, consisting of infinitesimal changes propagating along the characteristics is fairly well Figure 4.5 shows that tracking of the contact modeled. surface and shock wave, in comparison with exact locations at set times, is excellent. Using q+4 and q-4 based on conditions behind the burst diaphragm as estimates of velocities of the head and tail of the expansion wave respectively results in positions of the head and tail slightly different from those of an exact Riemann solver code Ref. 3%. The exact code is based on a method given in [Ref. 9:pp. 181-191]. However, an examination of the tabulated output showed that the solution method predicted changes in the gradients to occur at similar locations to those computed using the $q+\lambda$ and $q-\lambda$ estimates. Consequently, while there may be some inaccuracy in the numerical solution, the method of tracking the head and tail of the expansion wave is acceptable.

The ability to reproduce the same conditions but with flow to the left is demonstrated clearly in Fig. 4.6. The

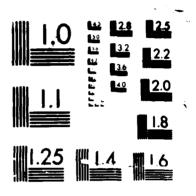
entropy, density, velocity, and pressure distributions are mirror-images of those for the case of high pressure on the left.

Test Case 2 results in Fig. 4.7 show that at time zero with a pressure ratio at the boundary of 4, which is lower than the preset value inside the tube of 5, an expansion wave traveling inwards is generated. Outflow is seen in the negative velocity distribution developing near the left boundary, where negative velocity implies flow traveling to the left. The contact surface and shock are clearly formed to the right of the off-center diaphragm, and travel to the The expansion wave generated at the diaphragm right. travels to the left and intersects with the expansion wave generated at the left boundary. The pressure distribution shows the propagation of these waves as the pressure drops behind the head of each wave. With conditions reversed, so that the high pressure is to the right of the diaphragm, the results in Fig. 4.8 are a mirror-image with velocity negative for flow to the left, and positive for the outflow to the right.

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Test Case 3 results in Fig. 4.9 demonstrate that the shock wave meeting an open boundary where the pressure held constant, is correctly computed to exit the ture density distribution shows the jump increase are shock, then another jump increase across the surface. Then density plunges down as an expense.

FURTHER DEVELOPMENT OF A ONE-DIMENSIONAL UNSTEADY EULER CODE FOR MAYE ROTOR APPLICATIONS(U) NAVAL POSTGRADUATE SCHOOL MONTEREY CA D T JOHNSTON MAR 87 NPS67-87-882 F/G 28/4 AD-A181 750 UNCLASSIFIED NL



MICROCOPY RESOLUTION TEST CHART

travels back into the tube when the shock exits. The pressure ratio at the open right boundary was held at unity, as seen in the pressure distribution which, at the boundary behaves similarly to the density distribution. The pressure at the boundary would be required to increase as the shock passed by, however the enforcement of the constant pressure locally causes an expansion wave to form traveling to the left. The entropy remains constant, at the value behind the shock, from the boundary back to the contact surface. There is a jump in entropy across the contact surface. The velocity distribution shows that as the shock travels to the right, the velocity jumps up. When the expansion wave generated at the right boundary travels inward the velocity continues to increase in magnitude while flowing to the right. The expansion wave generated at the diaphragm can be seen traveling to the left in the plots of pressure, density, and velocity. Reversing the situation and computing conditions for flow to the left, in Fig. 4.10, results in a mirror-image in the pressure, density, and entropy distributions. The velocity becomes negative since flow is to the left.

Test Case 4 is a repeat of the first test case but with a pressure ratio of 3.2 and a fine computational mesh. In Fig. 4.11 the density steps up across the shock and contact surface as they travel to the right. When the shock reflects the density jumps again. The velocity distribution

shows that the velocity drops to zero behind the reflected shock, after it had jumped up across the shock when it was traveling to the right. The instability seen in the velocity and pressure distributions near the midpoint occurred during the first 100 time steps. A numerical instability appears to generate at the diaphragm at time zero for pressure ratios less than about 3.0 which can be severe. For the conditions in this test case the transient instability damped out after the first 100 time steps. The shock, contact surface, and expansion wave are nevertheless seen to be accurately modeled. Figure 4.12 demonstrates that reversed conditions result in mirror-images of the computed conditions.

B. CURRENT LIMITATIONS OF THE CODE E1DV2

The current limitations of the E1DV2 code for modeling quasi-one-dimensional inviscid flow are in two categories. First, there are numerical limitations in obtaining solutions with the present code for different initial and boundary conditions. Second, the present coding limits what flow situations can be treated.

The numerical instability which occurs at low pressure ratios during the first few time steps can be severe. The assumption in the current code is that the shock forms immediately, which at high pressure ratios does not pose any problems. The mathematical modeling of the bursting diaphragm in subroutine "DBURST" adequately reduces the

transient instability for high pressure ratios, but not for low pressure ratios.

A second rather different numerical limitation was identified in numerically detecting the location of the head and tail of the expansion process. Because the expansion process is not a sharply defined front, fixing the precise locations of the head and tail waves numerically at a given time is difficult. However, the method currently used does accurately track the computed propagation of the wave along the characteristics. The characteristics are modeled currently as straight lines. A higher order curve would describe them more accurately.

The current code is limited to tracking two discontinuities and the expansion wave (i.e., a shock and a contact surface). Thus any situation which would generate another discontinuity can not be computed. The code can determine when this will occur, and will issue a message explaining the situation before terminating. Thus the shock colliding with a contact surface will currently terminate the program. A boundary pressure that is higher than the pressure inside the tube would also create a compression wave or possibly a shock wave. This condition will also terminate the program. Simulation of the process of a shock forming over an extended distance and time as compression waves pile on top of each other and strengthen, would also require additional code.

Finally, the variation of gamma that occurs across the contact surface in a wave rotor cannot be handled currently since E1DV2 assumes a single constant gamma throughout.

VI. CONCLUSIONS

Towards the development of a one-dimensional code for wave rotor applications, methods for tracking and correcting conditions across a contact discontinuity, applying open and closed-end boundary conditions, accounting for shock wave and contact surface interaction were devised and were presented here in detail. The EULER1 Fortran Code [Ref. 2] was revised to become the E1DV2 code with the following additional capabilities:

- 1) tracking of the contact surface and expansion wave
- 2) imposing high pressure initially on the right side of the diaphragm
- 3) correct jump conditions across the contact surface
- 4) allow open boundary conditions with constant pressure specified and allow exiting of shock and expansion waves
- 5) allow closed boundary conditions and model shock and expansion wave reflections
- 6) improved numerical accuracy from time zero to the maximum time step.

The code was tested on the shock tube problem under four different initial and boundary conditions with excellent results.

The following extensions are recommended to make the code suitable for wave rotor applications:

1) Solve the Riemann problem at the moment when the shock and contact surface intersect

- 2) Add additional code to track more than two discontinuities and one expansion wave
- 3) Incorporate a variable value of gamma into the code
- 4) Update the characteristic curve approximation from linear to a higher order polynomial
- 5) Add code necessary to handle open boundary conditions with inflow
- 6) Improve on the numerical computation at time zero for low pressure ratios across the diaphragm
- 7) Enable boundary conditions to be variable during program execution to allow wave rotor cycle design
- 8) Compare computations using the code with experimental data where available
- 9) Extend the code to two dimensions.

These extensions may require various degrees of effort. However, the ability of the QAZ1D solution method to be extended rather simply to describe viscous multi-dimensional flow suggests that such efforts would be justified.

APPENDIX A

DERIVATIONS OF EQUATIONS

A.	LIST OF VARIABLES
A	Speed of sound
$c_{\mathbf{p}}$	Specific heat at constant pressure
c_v	Specific heat at constant volume
e	specific internal energy
h	Specific enthalpy
P	Static pressure
Q	Modified Riemann variable
q_R	Reversible heat transferred
đ	Velocity magnitude
R	Modified Riemann variable
R_{G}	Gas constant
S	Modified entropy (non-dimensional where $S = S \cdot R_G$)
T	Static temperature
t	Time
u	Velocity relative to a standing shock wave
v	Specific volume
W	Incoming Mach Number relative to a stationary shock wave
W	Work
ρ	Density
γ	Ratio of specific heats

B. DERIVATION OF SHOCK JUMP EQUATION FOR HIGH PRESSURE ON THE RIGHT

The analytical equation relating the non-dimensionalized extended Riemann variable, R, change through a normal shock is derived below similar to that for the Q variable change when high pressure is on the left [Ref. 2:Appendix A].

Figure A.1 shows a shock moving to the left with velocity $V_{\rm S}$. Subscript A is always associated with parameters to the left of any discontinuity, and B with those on the right. To enable normal shock relations to be used the system requires a velocity in the opposite direction but of equal magnitude be imposed upon it. The coordinate system was defined such that vectors, such as velocity, directed to the right are positive while those to the left are negative.

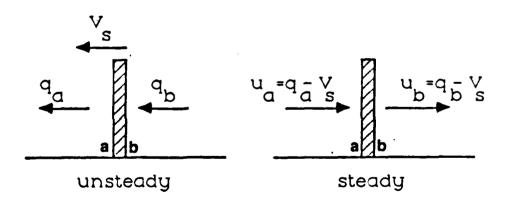


Figure A.1 Shock Wave with High Pressure on Right

Since relative incoming Mach Number, w, relates the velocity downstream, or that region into which the shock is traveling, to the speed of sound in that region [Ref. 10:pp. 114-154] then

$$\mathbf{w} = \frac{\mathbf{q}_{\mathbf{A}}^{-\mathbf{V}}\mathbf{s}}{A_{\mathbf{A}}} = \frac{\mathbf{u}_{\mathbf{A}}}{A_{\mathbf{A}}} \tag{A1}$$

w is a positive value because q_A , though negative, is smaller in magnitude than the equally negative shock velocity, V_S . The speed of sound, A, is positive by definition.

The appropriate extended Riemann variable in this case is R, defined as

$$R = q - AS \tag{A2}$$

Since q is negative, this can be rewritten as

$$R = -(|q| + AS)$$
 (A3)

to emphasize that R is the Riemann variable associated with the lesser change across the shock [Ref. 3:pp. 18-21]. We adopt the pattern of non-dimensionalizing velocity by the speed of sound, pressure and density by corresponding values downstream of the shock. Using the entropy S, defined by Verhoff [Ref. 1:p. 2] as

$$S = \frac{2}{\gamma - 1} - \frac{1}{\gamma(\gamma - 1)} \ln \left(\frac{P}{\rho \gamma} \right)$$
 (A4)

then

$$\frac{R_{B}^{-}R_{A}}{A_{A}} = \frac{q_{B}^{-}A_{B}S_{B}}{A_{A}} - \frac{q_{A}^{-}A_{A}S_{A}}{A_{A}}$$

$$= \frac{q_{B}^{-}q_{A}}{A_{A}} + S_{A}^{-} - \frac{A_{B}^{-}}{A_{A}^{-}} S_{B}$$

$$= \frac{q_{B}^{-}q_{A}}{A_{A}^{-}} + \left[\frac{2}{\gamma-1} - \frac{1}{\gamma(\gamma-1)} \ln \left(\frac{P_{A}^{-}}{P_{A}^{-}} \left(\frac{\rho_{A}^{-}}{\rho_{A}^{-}}\right)^{\gamma}\right)\right]$$

$$- \frac{A_{B}^{-}}{A_{A}^{-}} \left[\frac{2}{\gamma-1} - \frac{1}{\gamma(\gamma-1)} \ln \left(\frac{P_{B}^{-}}{P_{A}^{-}} \left(\frac{\rho_{A}^{-}}{\rho_{A}^{-}}\right)^{\gamma}\right)\right]$$

$$= \frac{q_{B}^{-}q_{A}^{-}}{A_{A}^{-}} + \left[1 - \frac{A_{B}^{-}}{A_{A}^{-}}\right] \left[\frac{2}{\gamma-1}\right] + \left(\frac{A_{B}^{-}}{A_{A}^{-}}\right) \frac{1}{\gamma(\gamma-1)} \left[\ln \left(\frac{P_{B}^{-}}{P_{A}^{-}} \left(\frac{\rho_{B}^{-}}{\rho_{A}^{-}}\right)^{\gamma}\right)\right] \tag{A5}$$

The ratios of pressure, density, and sonic velocity across a normal shock from Zucker [Ref. 7:p. 151] and Shapiro [Ref. 10:p. 118] in terms of Mach Number are

$$\frac{P_B}{P_A} = \frac{2\gamma}{\gamma + 1} w^2 - \frac{\gamma - 1}{\gamma + 1}$$
 (A6)

$$\frac{\rho_{\mathrm{B}}}{\rho_{\mathrm{A}}} = \frac{(\gamma+1)w^2}{(\gamma-1)w^2+2} \tag{A7}$$

$$\frac{A_{B}}{A_{A}} = \frac{1}{(\gamma+1)w} [2(\gamma-1)[1+\frac{\gamma-1}{2}w^{2}][\frac{2\gamma}{\gamma-1}w^{2}-1]]^{1/2}$$
(A8)

The first term on the right side of equation (A5) can be expressed in terms of w by applying simple continuity in mass.

$$\rho_{\mathbf{A}}\mathbf{u}_{\mathbf{A}}\mathbf{A}\mathbf{r}\mathbf{e}\mathbf{a}_{\mathbf{A}} = \rho_{\mathbf{B}}\mathbf{u}_{\mathbf{B}}\mathbf{A}\mathbf{r}\mathbf{e}\mathbf{a}_{\mathbf{B}} \tag{A9}$$

Taking the areas as equal, this becomes

$$\frac{\rho_{A}}{\rho_{B}} = \frac{u_{B}}{u_{A}} = \frac{(\gamma - 1)w^{2} + 2}{(\gamma + 1)w^{2}}$$
 (A10)

By subtracting one from each side

$$\frac{u_{B}}{u_{A}} - 1 = \frac{\gamma - 1}{(\gamma + 1)w^{2}} - 1$$

$$\frac{u_{B} - u_{A}}{u_{A}} = \frac{(\gamma - 1)w^{2} + 2 - (\gamma + 1)w^{2}}{(\gamma + 1)w^{2}}$$

$$\frac{u_{B} - u_{A}}{u_{A}} = \frac{2(1 - w^{2})}{(\gamma + 1)w^{2}}$$
(A11)

Substitute equation (A1) for u_A to get

$$\frac{u_{B}^{-u}A}{wA_{A}} = \frac{2(1-w^{2})}{(\gamma+1)w^{2}}$$

$$\frac{u_{B}^{-u}A}{A_{A}} = \frac{2(1-w^{2})}{(\gamma+1)w}$$
(A12)

thus

$$\frac{q_{B} - V_{S} - (q_{A} - V_{S})}{A_{A}} = \frac{2(1 - w^{2})}{(\gamma + 1)w}$$

$$\frac{q_{B} - q_{A}}{A_{A}} = \frac{2(1 - w^{2})}{(\gamma + 1)w}$$
(A13)

Combining equations (A6), (A7), (A8), and (A13) into equation (A'5) gives

$$\frac{R_{B}^{-R}A}{A_{A}} = \frac{2(1-w^{2})}{(\gamma+1)w} + (\frac{2}{\gamma-1})\{1 - (\frac{1}{(\gamma+1)w}(2(\gamma-1)[1+\frac{\gamma-1}{2}w^{2}][\frac{2\gamma}{\gamma-1}w^{2}-1]]^{\frac{2\gamma}{\gamma-1}}w^{2} - 1\}^{\frac{1}{\gamma-1}}$$

$$+ \{\frac{1}{(\gamma+1)w}(2(\gamma-1)[1+\frac{\gamma-1}{2}w^{2}][\frac{2\gamma}{\gamma-1}w^{2}-1]\}^{\frac{1}{\gamma-1}}$$

$$\times \{\frac{1}{\gamma(\gamma-1)}[\ln((\frac{2\gamma}{\gamma+1}w^{2}-\frac{\gamma-1}{\gamma+1})(\frac{(\gamma-1)w^{2}+2}{(\gamma+1)w^{2}})^{\frac{1}{\gamma-1}})\}\}$$
A.4

C. DERIVATION OF CONTACT SURFACE JUMP EQUATION

The analytical expression for the ratio of sor.

velocity across a constant surface is derived, as increase.

The first law of thermodynamics is stated as

or, in differential form

$$de = \partial q_R + \partial W$$
 (A15)

Internal energy is defined as

$$e = h - pv (A16)$$

then

$$de = dh - pdv - vdp$$
 (A17)

The incremental work is given by

$$\partial W = pdv$$
 (A18)

The heat addition is determined from the definition of modified entropy,

$$d\overline{s} = -\frac{1}{\gamma} \frac{dq_R}{T}$$

$$dq_R = -\gamma T d\overline{s}$$
(A19)

Substituting equations (A17), (A18), and (A19) into equation (A15) yields

$$dh - pdv - vdp = -\gamma TdS - pdv$$

Canceling like terms, and rearranging gives

$$dp = \frac{\gamma}{v} \overline{TdS} + (\frac{1}{v}) dh \qquad (A20)$$

Enthalpy, h, is defined as

$$h = C_p T \tag{A21}$$

For a perfect gas the sonic velocity is given by

$$A = (\gamma R_G T)^{1/2}$$

thus

$$dA = \frac{1}{2} (\gamma R_G T)^{1/2} (dT/T)$$
 (A22)

Substituting equation (A21) and then (A22) into equation (A20), equation (A20) becomes

$$dp = \frac{\gamma}{v} \overline{T} d\overline{S} + (\frac{1}{v}) d(C_p T)$$

$$= \frac{\gamma}{v} \overline{T} d\overline{S} + (\frac{1}{v}) C_p dT$$

$$= \frac{\gamma}{v} \overline{T} d\overline{S} + (\frac{1}{v}) C_p T (\frac{2dA}{A}) \qquad (A23)$$

For an ideal gas,

$$Y = C_p/C_v$$

and

$$C_p = C_v + R_G$$

Combining these two equations, and rearranging

$$c_{p} = R_{G} \left(\frac{\gamma}{\gamma - 1} \right) \tag{A24}$$

Substituting equation (A24) into equation (A23), and observing that pressure remains constant through the contact surface

$$\frac{T}{V}\gamma d\overline{S} + \frac{T}{V}(R_{G}(\frac{2\gamma}{\gamma - 1})) \frac{dA}{A} = 0$$
 (A25)

Eliminating T/v, equation (A25) becomes

$$\left(\frac{2}{\gamma-1}\right) d(\overline{S}/R_{G}) = -\frac{dA}{A}$$
 (A26)

Then \overline{S}/R_G becomes a non-dimensionalized entropy. Using the notation of $S=\overline{S}/R_G$ now for the non-dimensionalized form, so that by integrating both sides

$$\frac{2}{\gamma-1} \int_{A}^{B} ds = \int_{A}^{B} - \frac{dA}{A}$$

$$\frac{2}{\gamma-1}[S_B - S_A] = \ln A_A / A_B$$

which can be written as

$$A_{A}/A_{B} = \exp^{(\frac{(\gamma-1)}{2}(S_{B}-S_{A}))}$$
 (A27)

Definitions used in this development, excluding modified entropy were from [Ref. 11:pp. 87-125].

D. DERIVATION OF EXTENDED RIEMANN VARIABLE CHANGE ACROSS A CONTACT SURFACE

An analytical expression for the change in the non-dimensionalized extended Riemann variable, Q, across a contact surface traveling right is derived here. Figure A.2 depicts a contact surface moving right with velocity q.

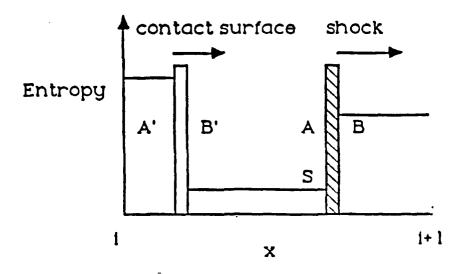


Figure A.2 Contact Surface Traveling Right Subscript Notation

Values of parameters to the left of the interface are denoted by subscript A', and those to the right with subscript B'. As illustrated, parameters to the left of the shock have subscript A, and to the right subscript B. All velocities are non-dimensionalized by sonic velocity immediately downstream of the discontinuity. Thus using the definition of the extended Riemann variable,

$$Q = q + AS (A28)$$

then

$$\frac{Q_{A'} - Q_{B'}}{A_{B'}} = \frac{q_{A'} + A_{A'}S_{A'}}{A_{B'}} - \frac{q_{B'} + A_{B'}S_{B'}}{A_{B'}}$$

$$= \frac{q_{A'} - q_{B'}}{A_{B'}} + \frac{A_{A'}}{A_{B'}}(S_{A'}) - S_{B'} \tag{A29}$$

Since velocity is constant through a contact surface, so that

$$q_{A} = q_{B}$$

then equation (A29) becomes

$$\frac{Q_{A'} - Q_{B'}}{A_{B'}} = \frac{A_{A'}}{A_{B'}} S_{A'} - S_{B'}$$

Using equation (A27), this can be written

$$\frac{Q_{A'} - Q_{B'}}{A_{B'}} = \exp^{(\frac{(\gamma - 1)}{2}(S_{B'} - S_{A'}))} S_{A'} - S_{B'}$$
(A30)

Multiply each side by A_{B} , A_{B} , and since A_{B} , = A_{A} then

$$\frac{Q_{A'} - Q_{B'}}{A_{B}} = [(\exp^{(\frac{(\gamma - 1)}{2}(S_{B'} - S_{A'}))})(S_{A'}) - S_{B'}](A_{A}/A_{B})$$
(A31)

For a contact surface traveling to the left, as illustrated in Fig. A.3, the derivation is entirely similar but

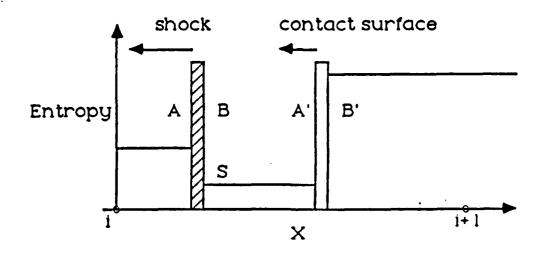


Figure A.3 Contact Surface Traveling Left Subscript Notation

using the R, extended Riemann variable with the result

$$\frac{R_{B^*} - R_{A^*}}{A_A} = [\exp^{(\frac{(\gamma - 1)}{2})(S_{A^*} - S_{B^*})}(S_{B^*}) - S_{A^*}] (\frac{A_B}{A_A})$$
 (A32)

E. DERIVATION OF OPEN BOUNDARY CONDITIONS WITH CONSTANT PRESSURE

The equation for density and temperature ratios in terms of pressure and entropy are derived below. The definition of modified entropy in non-dimensional form is

$$s = \frac{2}{\gamma - 1} - \frac{1}{\gamma (\gamma - 1)} \ln \left(\frac{P}{\rho^{\gamma}} \right)$$
 (A33)

where P and ρ are non-dimensionalized ratios. Then

$$(S - \frac{2}{\gamma - 1})(-\gamma(\gamma - 1)) = \ln(P/\rho^{\gamma})$$

or .

$$\exp \left[\left(S - \frac{2}{\gamma - 1} \right) \left(-\gamma \left(\gamma - 1 \right) \right) \right] = P/\rho^{\gamma}$$

Rearranging,

$$\rho^{\gamma} = [P[\exp \left[(s - \frac{2}{\gamma - 1}) \left(-\gamma (\gamma - 1) \right) \right]]$$

thus

$$\rho = p^{1/\gamma} (\exp^{(S - \frac{2}{\gamma - 1})(-\gamma(\gamma - 1))})^{-1/\gamma}$$

$$\rho = \{\frac{1}{p} (\exp^{(S - \frac{2}{\gamma - 1})(-\gamma(\gamma - 1))})\}^{-1/\gamma}$$
(A34)

Using the perfect gas law,

$$\rho = \left\{ \frac{1}{\rho T} (\exp^{(S - \frac{2}{\gamma - 1})(-\gamma(\gamma - 1))})^{-1/\gamma} \right\}$$

$$\rho^{-\gamma} = \frac{1}{\rho T} (\exp^{(S - \frac{2}{\gamma - 1})(-\gamma(\gamma - 1))})$$

multiply each side by T and divide by $\rho^{-\gamma}$ then

thus
$$T = \rho^{\gamma/o}(\exp^{(S - \frac{2}{\gamma - 1})(-\gamma(\gamma - 1))})$$

$$T = \rho^{\gamma - 1}[\exp^{(S - \frac{2}{\gamma - 1})(\gamma(1 - \gamma))}]$$
(A35)

APPENDIX B

OPERATION OF E1DV2 ON THE NPS VM/CMS SYSTEM

A. TERMINAL REQUIREMENTS

Terminal requirements depend on the desired output. Any terminal, such as the IBM 3278, connected into the VM/CMS system is adequate for a tabular listing or Disspla Metafile of data. The Disspla Metafile stores graphical data for display using DISSPOP commands. If output of the plots on a monitor screen is desired, an IBM 3277-TEK618 dual screen terminal must be used. Table B.I lists terminal requirements for different outputs.

TABLE B.I

TERMINAL AND OUTPUT

OUTPUT	TERMINAL
Tabular listing of data	Any terminal
Graphical data in format for VERSATEC printing	Any terminal
Graphical data plotted on screen	IBM 3277-TEK618

B. PROCEDURE

1. Editing Variables and Program Setup

To change the initial and boundary conditions, graphical output, and grid size to run the program under

different conditions, the following must be done. First, pick the appropriate terminal from Table B.I and log on. Enter the editor by issuing the command

x E1DV2 FORTRAN A

Table B.II lists the code variables that will require editing and their meaning. In addition, to these variables if graphical plots are to be outputed then enter the "BORDER" and "EXACT" subroutines and edit the lines:

"FIRST ORDER N = ???"

"DENSITY RATIO = ??? TEMP RATIO = ???"

"PRESSURE RATIO = ???"

To issue the output graphs to the screen comment out the lines "COMPRS", and use

CALL TEK618

Otherwise, if a Disspla Metafile of the graphics plot is desired, comment out the "TEK618" line, and use

CALL COMPRS

These lines are in the "Set up graphics plot of variable" loop in the main program.

To store these changes, hit the enter key, and type "file". Select the enter key once more. The program is now ready to be compiled and executed.

2. Commands

To compile and execute the E1DV2 code on the VM/CMS system perform the following commands exactly as typed:

TABLE B.II

EDITABLE VARIABLES

<u>Variable</u>	<u>Edit</u>
-----------------	-------------

variable	EGIL
DIMENSION statement for arrays A(N),, XARRAY(N)	set the dimension of the arrays equal to the number of nodes in the grid
N	set to the number of nodes in the grid
GRAPHS	set to: 0 for tabular listing of data 1 for plot of density, entropy, pressure and velocity distributions 2 for plot of exact density distribution compared to computed density distribution
SKIP	set to number of time steps between calls to output routines
JSTOP	set to maximum number of time steps
TRI	set to initial temperature ratio across diaphragm
PRI	set to initial pressure ratio across diaphragm
DRI	set to initial density ratio across diaphragm
QLI	set to initial velocity left of diaphragm
QRI	set to initial velocity right of diaphragm
LBDPRI	set to initial pressure ratio across left boundary
LBDTRI	set to initial temperature ratio across left boundary
LBDORI	set to initial density ratio across left boundary

TABLE B.II (CONTINUED)

RBDDRI	set to initial density ratio across right boundary
RBDPRI	set to initial pressure ratio across right boundary
RBDTRI	set to initial temperature ratio across right boundary
G	set to desired value of gamma
EE	<pre>set to desired error tolerance for calculation of characteristic slope (i.e., 0.1D-8)</pre>
LWPRES	<pre>set to: 2 for low pressure on right side of diaphragm 3 for low pressure on left side</pre>
LBNDRY RBNDRY	set to: 1 for closed boundary 0 for open boundary
LBDPRS RBDPRS	set to: 0 for constant pressure at left boundary 1 for pressure that adjusts at the left boundary
XINIT	set to location of diaphragm
VHEAD	set to exact velocity for head of expansion wave
VTAIL	set to exact velocity for tail of expansion wave
VCDE	set to exact velocity for contact surface
VSE	set to exact velocity for shock wave
DLCD	set to exact density behind contact surface
DLSH	set to exact density behind shock

TABLE B.II (CONTINUED)

```
set to diaphragm location (i.e.,
SIGMA(1,2)
SIGMA(2,2)
                        0.5D00)
SIGMA(3,2)
SIGMA(4,2)
Y
                        There are four cases where Y
                        appears in the program
                        edit as follows:
                        Comment out Y = (Integer#), use:
                        first, Y = (N+1)/2 if LWPRES = 2
                        second, Y = (N+3)/2
                        and
                        third, Y = (N-1)/2 if LWPRES = 3
                        fourth, Y = (N+1)/2
                        for diaphragm at 0.5
                        Comment out those above, if dia-
                        phragm at another node. Set
                        first, Y = (Integer #) of node for
                          LWPRES = 2
                        second, Y = (# + 1)
                        and
                        third, Y = (Integer # - 1) of node
                           for LWPRES = 3
                        fourth, Y = (#)
```

1) Increase the virtual memory by entering

DEFINE STORAGE 1M

2) To return to CMS environment enter

I CMS

3) To compile the program enter

FORTVS E1DV2

The screen will display messages as it compiles each routine and when finished a ready symbol appears.

4) To execute the program, enter

DISSPLA E1DV2

The message

- ...YOUR FORTRAN PROGRAM IS NOW BEING LOADED...
- ... EXECUTION WILL SOON FOLLOW...

should appear, followed by

... EXECUTION BEGINS...

If at a TEK618 terminal with GRAPHS equal to 1 or 2 then the screen on the TEK618 will begin plotting the selected graph. A

...press ENTER to continue...

message will appear on the 3277 terminal. If a copy of the plot is desired, do so now before pressing the enter key. After pressing the enter key on the 3277 terminal, the plot will be erased and the program will terminate. Proper termination will result in

END OF DISSPLAY 9.2 #### VECTORS IN 1 PLOT... appearing, followed by a ready message.

If GRAPHS was set to 0, then proper termination would be a ready message. The tabular listing of pressure, density, velocity, entropy, and Riemann variables will be in "FILE FT09F001." The exact location of the shock, contact surface, and expansion wave with elapsed time will be in "FILE FT08F001." The computed location of the shock, contact surface, and expansion wave with elapsed time will be in "FILE FT10F001."

A second method to compile and execute the program, plus provide the files with a name is to create the following EXEC file on the user's disk.

FI 9 DISK FILE09 LISTING A(PERM FI 10 DISK FILE10 LISTING A(PERM FI 8 DISK FILE08 LISTING A(PERM FORTVS &1

A possible file name and required file type would be

RUN EXEC

To compile the program and define the output files, enter ${\tt RUN\ E1DV2}$

After compiling is finished, and the ready message appears, enter

DISSPLA E1DV2

The program executes as outlined before.

APPENDIX C

FLOWCHARTS

Flowcharts for major routines in E1DV2 are shown.

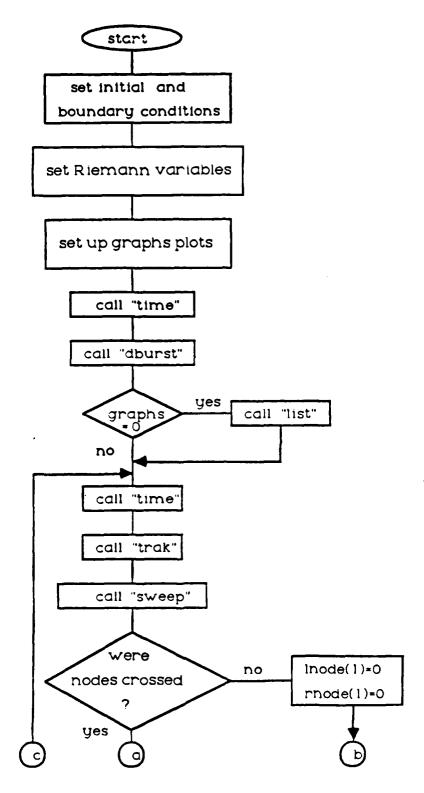


Figure C.1 Main Program Flowchart

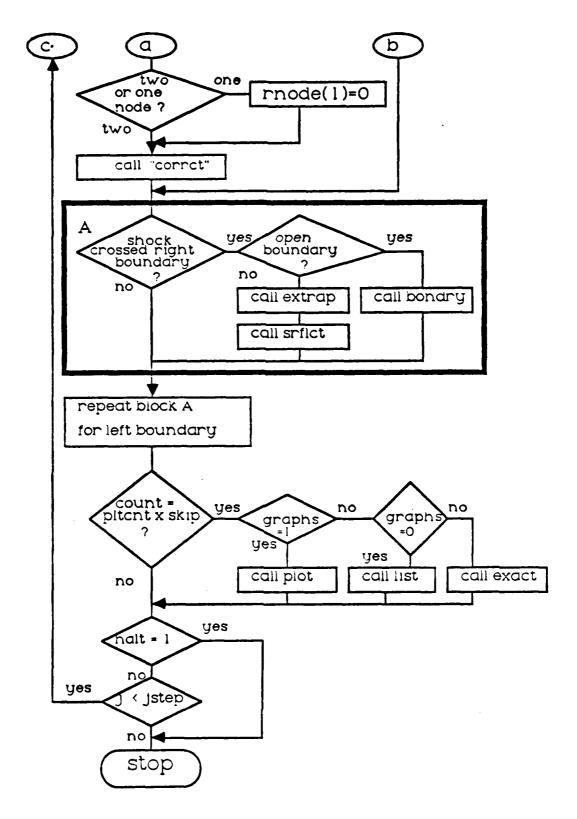


Figure C.1 (Continued)

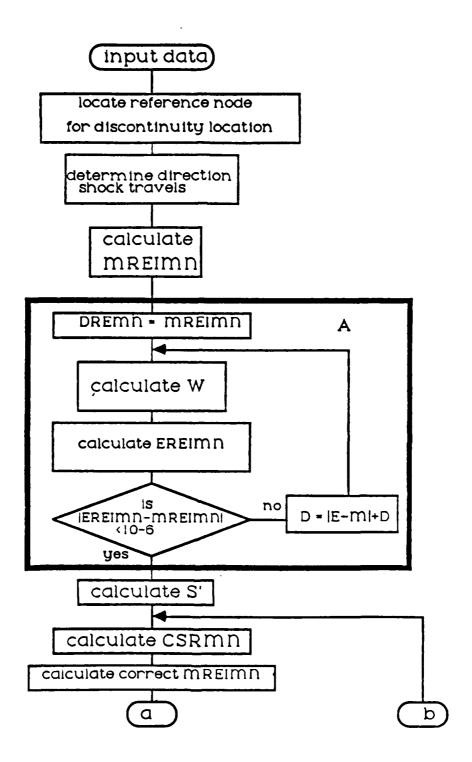


Figure C.2 "DBURST" Subroutine Flowchart.

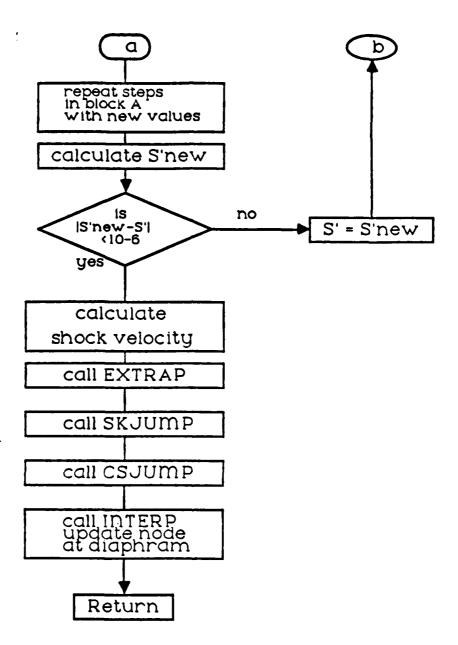


Figure C.2 (Continued)

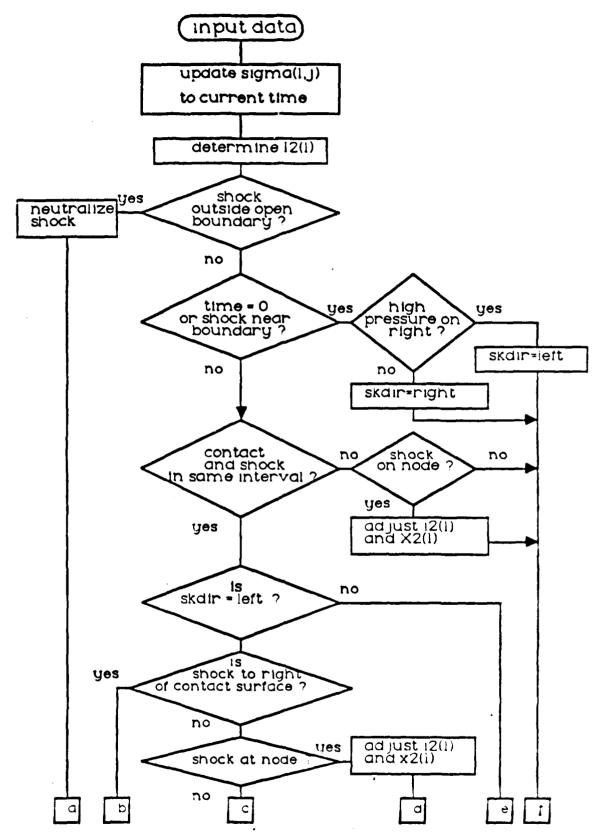


Figure C.3 "TRAK" Subroutine Flowchart

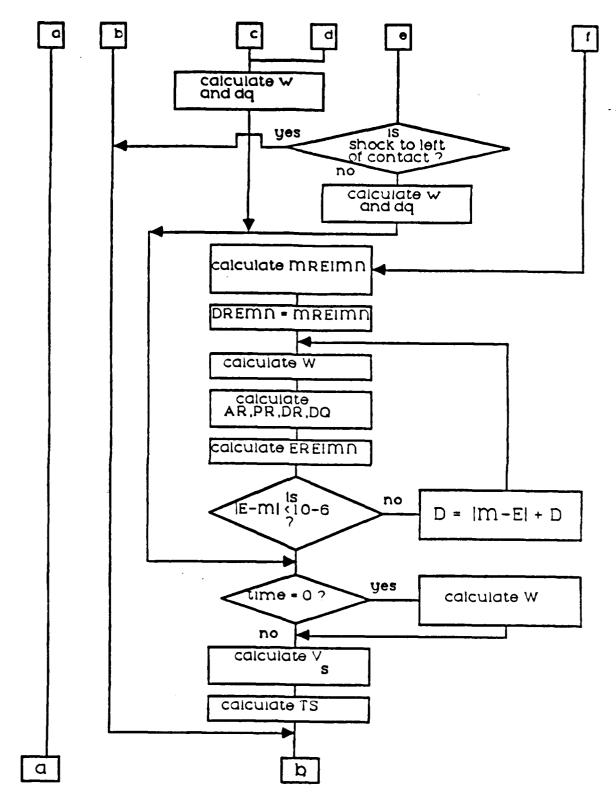


Figure C.3 (Continued)

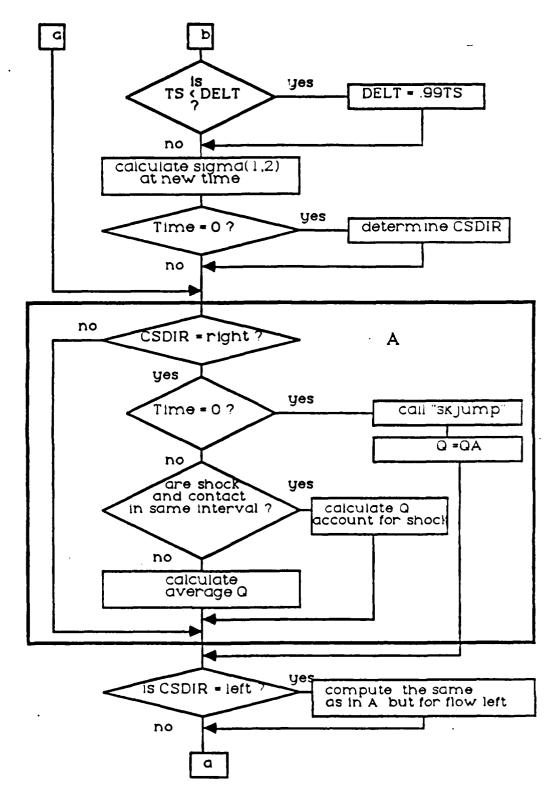


Figure C.3 (Continued)

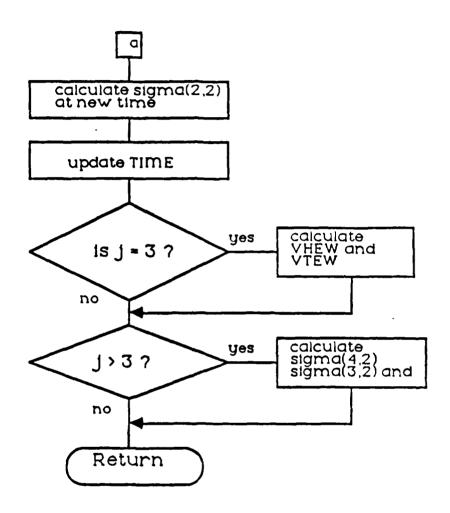
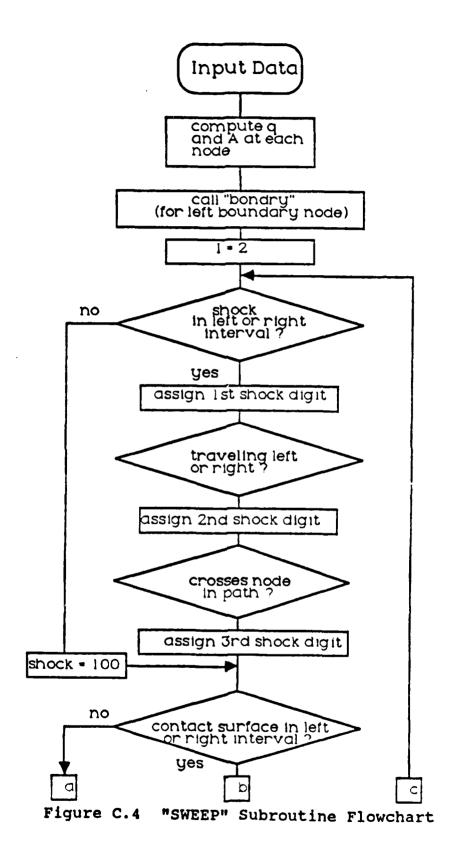
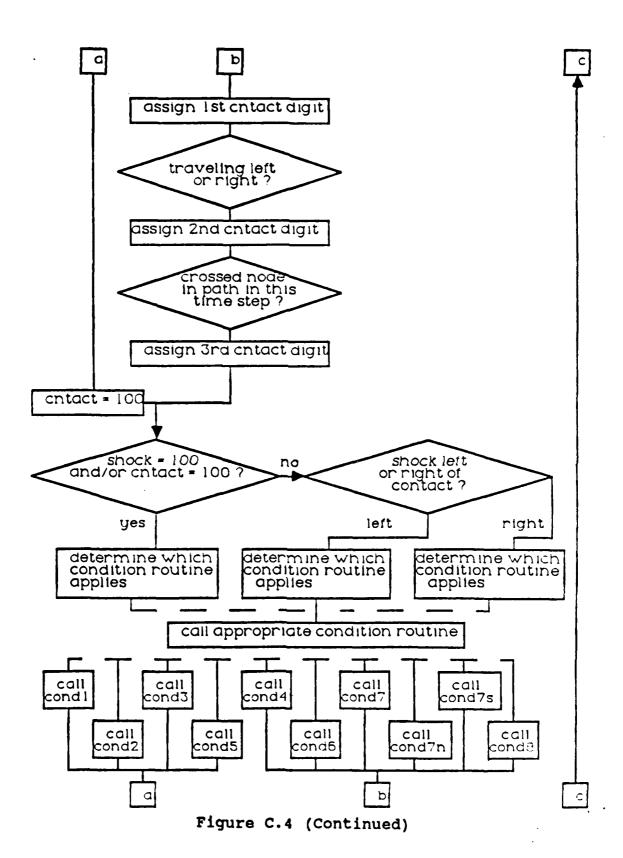


Figure C.3 (Continued)





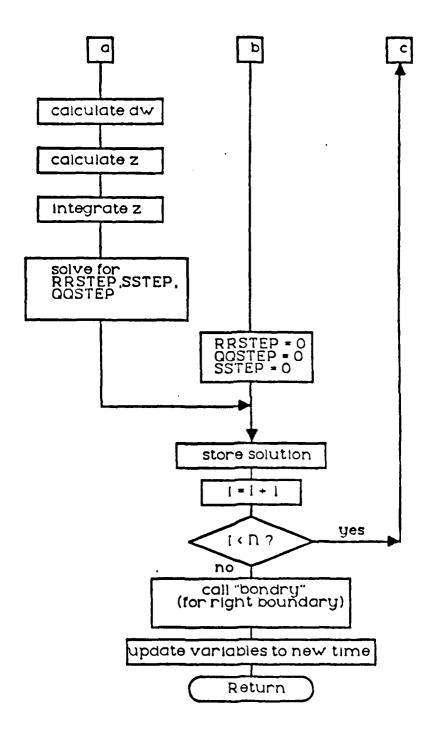


Figure C.4 (Continued)

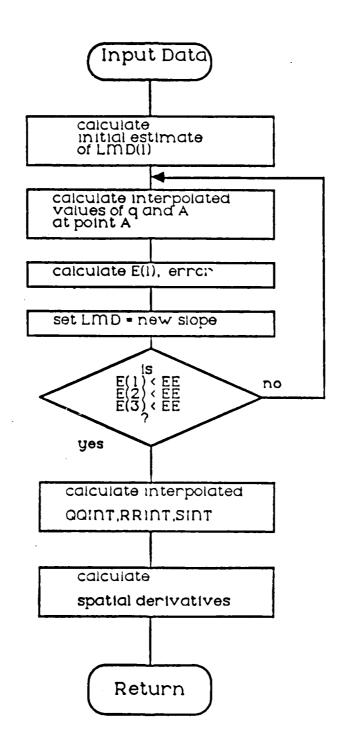


Figure C.5 General "COND1, 2, 3, and 5" Subroutine Flowchart

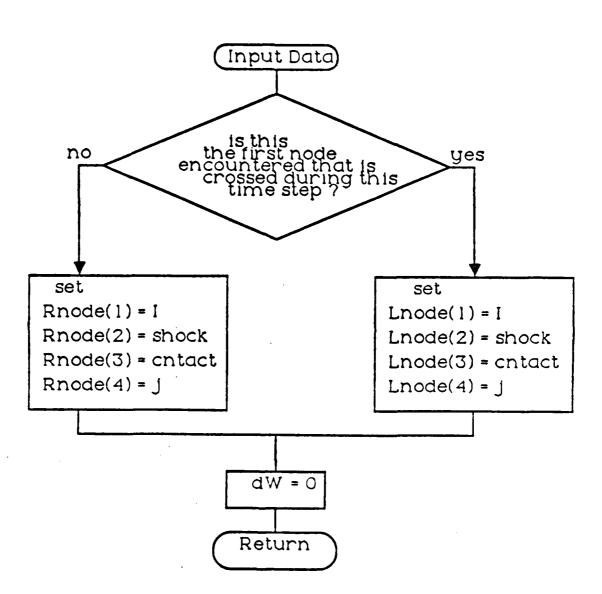


Figure C.6 "COND4" Subroutine Flowchart

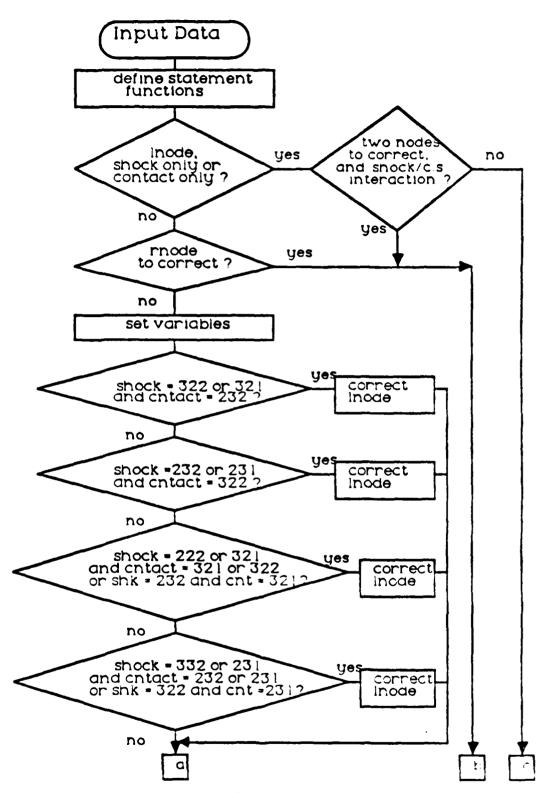


Figure C.7 "CORRCT" Subroutine Flowchart

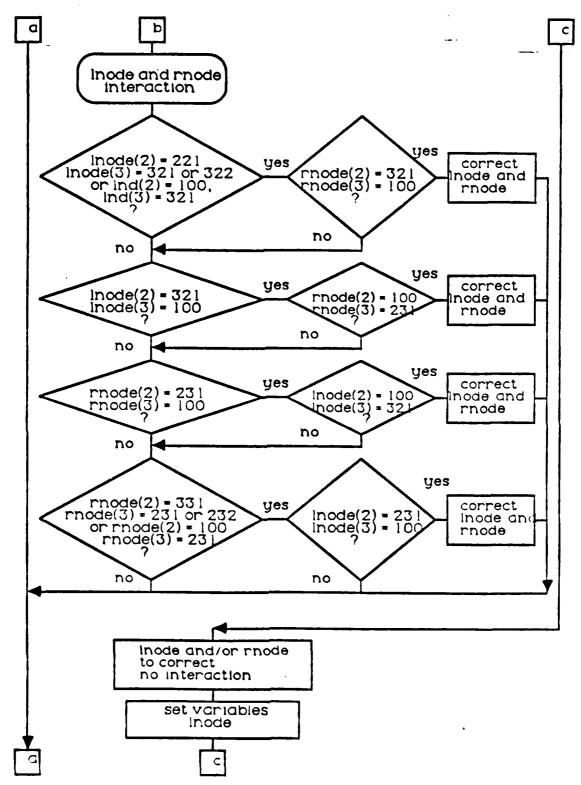


Figure C.7 (Continued)

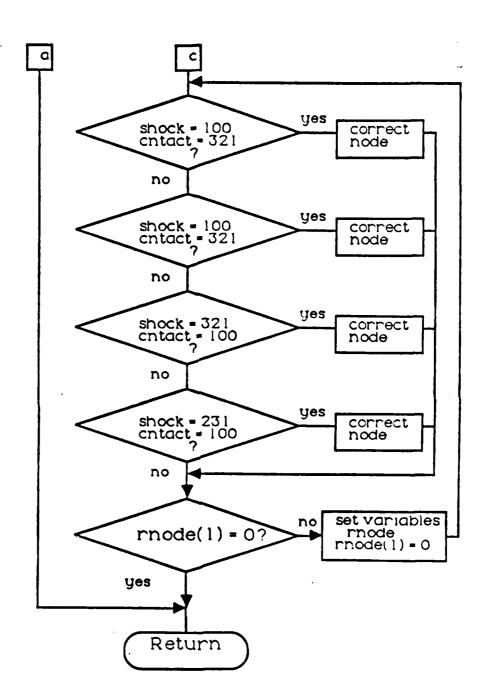


Figure C.7 (Continued)

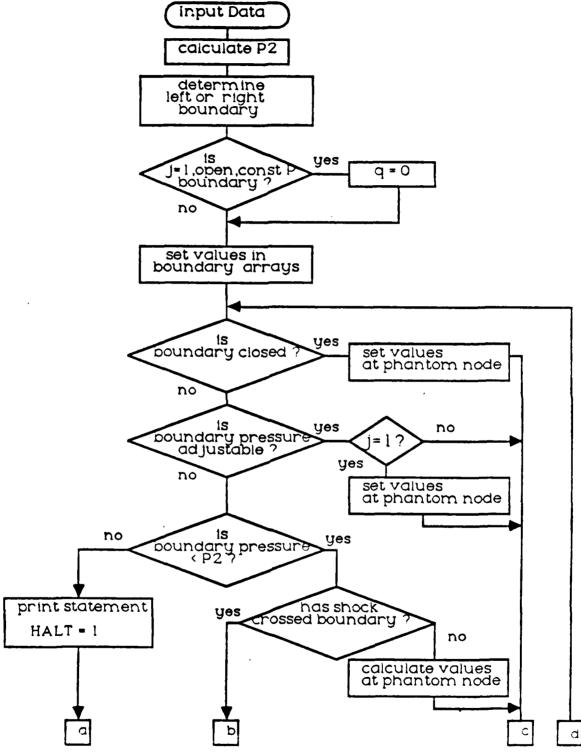
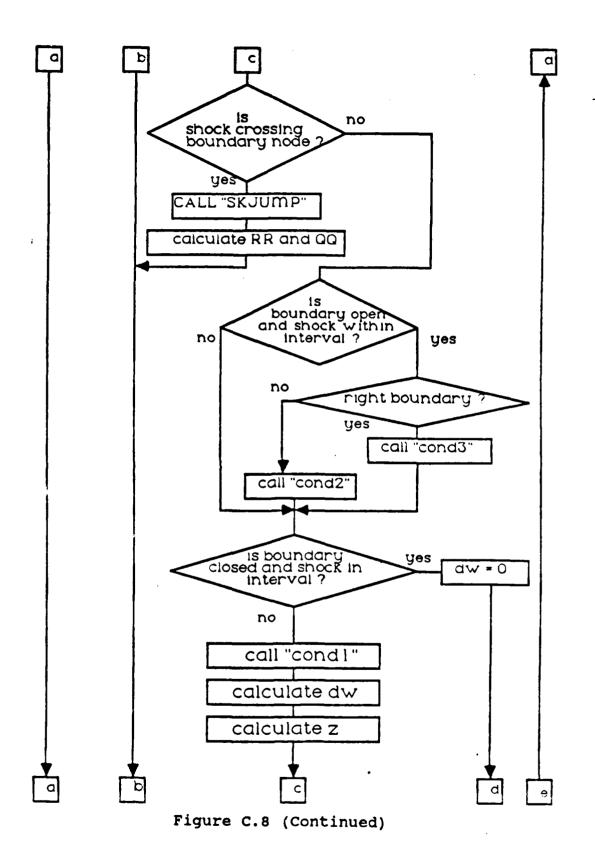


Figure C.8 "BONDRY" Subroutine Flowchart



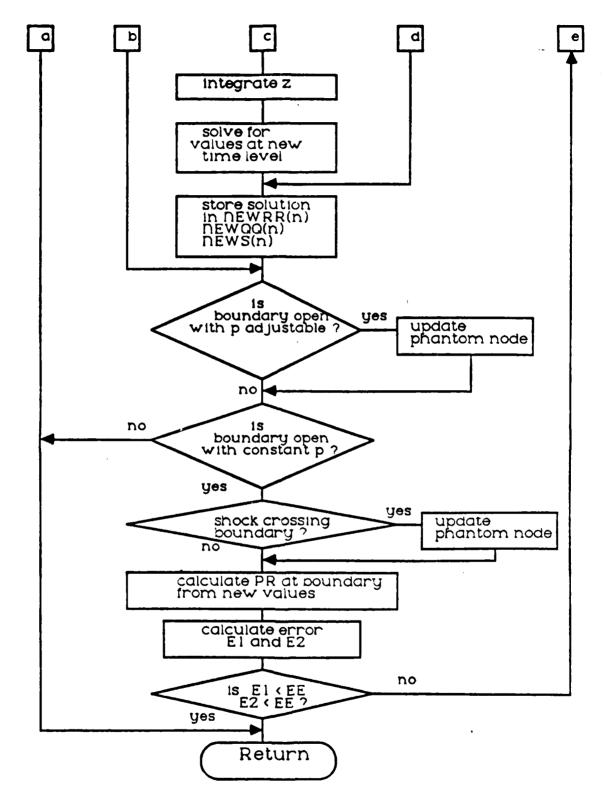


Figure C.8 (Continued)

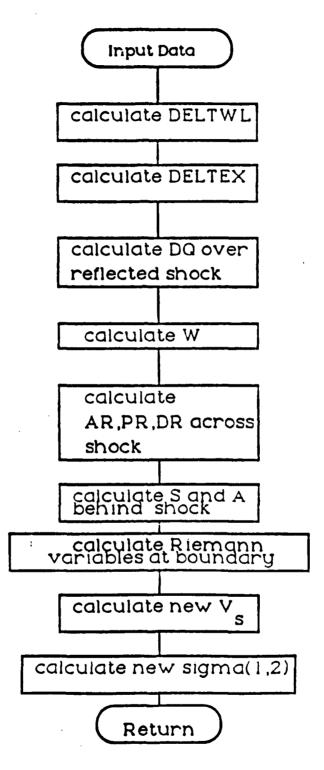


Figure C.9 "SRFLCT" Subroutine Flowchart

APPENDIX D

E1DV2 FORTRAN LISTING

```
*****
                   EULER-10
                      VERSION 2
                       (E10V2)
          THIS PROGRAM SOLVES THE EULER EQUATIONS
         EXPRESSED IN A QUAZI-ONE DIMENSIONAL
         STREAMLINE COORDINATE SYSTEM.
C
         AUTHOR - LT. D.T. JOHNSTON, FEB 1987
C
C
         BASED ON THE EULERI CODE BY
C
         T.F. SALACKA, DEC 1985
C
         FEATURES OF THIS VERSION (2)
C
          + ORDER OF SPATIAL DERIVITIVES - FIRST
C
C
         + NUMBER OF SPATIAL DIMENSIONS - ONE
C
         + DISCONTINUITIES TREATED:
C
                SHOCKS
                                        - YES
                CONTACT DISCONTINUITIES - YES
C
                EXPANSION WAVES
                                        - YES
C
          + HIGH PRESSURE SIDE
¢
                LEFT
                                        - YES
C
                 RIGHT
                                        - YES
C
C
C
Č
             CONVENTIONS
                         AND
                                DEFINITIONS
C
C
C
C
      ----- NON-DIMENSIONING CONVENTION-----
C
C
        ALL VELOCITIES NON-DIM. BY THE SOUND SPEED ON
C
            THE LOW PRESSURE SIDE OF THE DIAPHRAGM.
        ALL PRESSURES, DENSITIES, AND TEMPERATURES ARE
C
            NON-DIM. BY THEIR INITIAL VALUES ON THE LOW
            PRESSURE SIDE OF THE DIAPHRAGM.
C
        SPACIAL DISTANCE IS NON-DIM.BY OVERALL LENGTH.
        ENTROPY IS NON-DIM. BY THE GAS CONSTANT, R.
        TIME IS NON-DIM. BY (LENGTH/SOUND SPEED).
        VELOCITIES AND DISTANCES ARE DEFINED POSITIVE
C
            TO THE RIGHT.
                  SUBSCRIPT NOTATION----
        I - SPACIAL NODE 11 TO N FROM LEFT TO RIGHT)
        J - TIME LEVEL (0 IS THE INITIAL CONDITION)
        K - DENOTES WHICH CHARACTERISTIC MAVE IS BEING
            DEALT HITH:
               1 = Q+A
                          2 = Q
                                   3 = Q-A
        L - DENOTES WHICH TYPE OF DISCONTINUITY IS
            BEING DEALT WITH:
               1 = SHOCK 2 = CONTACT DISCONTINUITY
               3 = HEAD OF EXPANSION HAVE
               4 = TAIL OF EXPANSION HAVE
```

```
- SPEED OF SOUND
           - DENOTES THE VALUE OF A VARIABLE AT THE NODE
C
      ₩À
             TO THE LEFT OF A DISCONTINUITY. * CAN
             BE ANY VARIABLE NAME.
¢
           - THE RATIO OF SOUND SPEED ACROSS A
             SHOCK, A/B(SHOCK MOVING RIGHT), B/A(SHOCK MOVING LEFT)
C
           - DENOTES THE VALUE OF A VARIABLE AT THE NODE
             TO THE RIGHT OF A DISCONTINUITY.
      BORY - 3 DENOTES LEFT BOUNDARY, 2 THE RIGHT BOUNDARY
¢
      COUNT - COUNTER FOR GRAPHICS ROUTINES
C
      DARRAY - ARRAY OF DENSITY FOR PLOTTING
C
      DELT
             - TIME STEP
C
      DLCD
             - DENSITY BEHIND THE CONTACT
                DISCONTINUITY IN THE EXACT SOLUTION.
C
             - DENSITY BEHIND THE SHOCK IN THE
C
                EXACT SOLUTION.
C
           - THE JUMP IN VELOCITY ACROSS THE SHOCK
             DIVIDED BY THE SOUND SPEED AT B(RIGHT) OR A(LEFT)
C
      DRI
             - INITIAL DENSITY RATIO ACROSS THE SHOCK
C
      EE
             - DESIRED PRECISION FOR CHARACTERISTIC CALCULATIONS
C
             - GAMMA (RATIO OF SPECIFIC HEATS)
      GRAPHS - FOR GRAPHICAL OUTPUT, 0=NONE (TABULAR)
¢
                1=PLOTS ALL VARIABLES
C
                2=COMPARES DENSITY WITH EXACT SOLUTION
C
      61
             -1/(G-1)
C
      G2
             -2/(G-1)
C
             -1/(N-1)
C
      HALT - TERMINATES PROGRAM IF 1, SET BY CONDITIONS NOT CODED
          - NUMBER OF THE NODE TO THE RIGHT OF A
C
             DISCONTINUITY.
      JSTOP - NUMBER OF TIME LEVELS TO BE CALCULATED
      LBOOR - LEFT BOUNDARY DENSITY RATIO
C
      LBODRI - LEFT BOUNDARY DENSITY RATIO AT TIME ZERO
      LBDPR - LEFT BOUNDARY PRESSURE RATIO
      LBDPRI - LEFT BOUNDARY PRESSURE RATIO AT TIME ZERO
      LBDPRS - VALUE OF 0 DENOTES CONSTANT PRESSURE AT LEFT BOUNDARY
C
               ,1 DENOTES ADJUSTABLE PRESSURE AT THE LEFT BOUNDARY
      LBOTR - LEFT BOUNDARY TEMPERATURE RATIO
C
      LBOTRI - LEFT BOUNDARY TEMPERATURE RATIO AT TIME ZERO
C
      LBNDRY - DENOTES LEFT BOUNDARY CONDITION, OPEN OR CLOSED
      LNODE - ARRAY OF LEFT MOST NODE TO BE CORRECTED IN CORRCT
C
      LMPRES - DENOTES WHICH SIDE OF DIAPHRAGM HAS LOW PRESSURE
             - NUMBER OF SPACIAL NODES (ODD NUMBER)
             - DOUBLE PRECISION VALUE OF N
      NEM**(I)- STORED VALUES OF ** FOR THE NEXT TIME LEVEL
      PARRAY - ARRAY OF PRESSURES FOR PLOTTING
            - INITIAL PRESSURE RATIO ACROSS THE SHOCK
      PLTCNT - COUNTER FOR GRAPHICS ROUTINES
            - ABSOLUTE FLUID VELOCITY
      QARRAY - ARRAY OF VELOCITIES FOR PLOTTING
      QLBD - INITIAL VELOCITY AT LEFT BOUNDARY
      OLI
             - INITIAL VELOCITY LEFT OF THE DIAPHRAGM
      QRBO - INITIAL VELOCITY AT RIGHT BOUNDARY
      ORT
             - INITIAL VELOCITY RIGHT OF THE DIAPHRAGM
             - Q+A*S (EXTENDED RIEMANN VARIABLE)
      RBODR - RIGHT BOUNDARY DENSITY RATIO
      RBDDRI - INITIAL RIGHT BOUNDARY DENSITY RATIO
      RBDPR - RIGHT BOUNDARY PRESSURE RATIO
      RBOPRI - INITIAL RIGHT BOUNDARY PRESSURE RATIO
      RBOPRS - VALUE OF O DENOTES A CONSTANT PRESSURE AT RIGHT
               BOUNDARY, WHILE 1 IS FOR ADJUSTABLE PRESSURE
      RBDTR - RIGHT BOUNDARY TEMPERATURE RATIO
      RBOTRI - INITIAL RIGHT BOUNDARY TEMPERATURE RATIO
      RBNDRY - DENOTES RIGHT BOUNDARY OPEN OR CLOSED
      RNODE - ARRAY FOR RIGHT MOST NODE TO BE CORRECTED IN CORRCT
             - Q-A*S (EXTENDED RIEMANN VARIABLE)
      RR
             - ENTROPY
      SARRAY - ARRAY OF ENTROPY FOR PLOTTING
```

```
C
      SIGMA - SPATIAL LOCATION OF DISCONTINUITIES
               SIGMA(L,J) WHERE L INCICATES THE TYPE OF
¢
                 DISCONTINUITY AND J INDICATES THE
                 TIME LEVEL; 1 - CURRENT LEVEL
                 2 - LEVEL BEING CALCULATED
C
      SK - INTEGER THAT DENOTES RELATIVE LOCATION OF SHOCK NEAR
           BOUNDARIES
¢
             - VARIABLE MHICH INDICATES HOW MANY TIME STEPS BETWEEN
      SKIP
               CALLS TO OUTPUT ROUTINES
             - TIME SINCE INITIAL CONDITIONS
C
             - INITIAL TEMP. RATIO ACROSS THE SHOCK
C
      TRI
C
      VHEAD - VELOCITY OF THE HEAD OF THE EXPANSION
C
                WAVE FOR THE EXACT SOLUTION.
C
      VTAIL - VELOCITY OF THE TAIL OF THE EXPANSION
                WAVE FOR THE EXACT SOLUTION.
C
      VCDE
             - VELOCTIY OF THE CONTACT DISCONTINUITY
C
                FOR THE EXACT SOLUTION.
C
      ٧S
           - THE SHOCK SPEED(POSITIVE RIGHT, NEGATIVE LEFT)
C
      VSE
             - VELOCITY OF THE SHOCK FOR THE EXACT
C
                SOLUTION.
             - MACH NO. RELATIVE TO A STANDING SHOCK
      XARRAY - ARRAY OF SPATIAL POSITIONS FOR PLOTTING
C
C
      XEXACT - ARRAY OF SIX X VALUES FOR THE EXACT SOLUTION.
      XINIT - INITIAL POSITION OF DISCONTINUITY FOR
C
C
                EXACT SOLUTION PLOTTING.
             - LOCATION OF NODE TO RIGHT OF DISCONT.
C
C
               ALONG THE SPACIAL AXIS.
C
             - (N+1)/2
C
      YEXACT - ARRAY OF SIX DENSITY VALUES FOR THE EXACT SOLUTION.
C
      *** OTHER VARIABLES ARE DEFINED IN THE
               SUBROUTINES WHERE THEY ARE USED ****
C
C
         C
¢
                    PROBLEM SET - UP
C
C
C
C
      THE PARTICULAR PROBLEM FOR THIS VERSION IS:
¢
C
          SHOCK TUBE, SINGLE CENTERED DIAPHRAGM WITH
¢
          HIGH PRESSURE SIDE TO THE RIGHT.
C
C
          BOUNDARY CONDITIONS - LEFT END CLOSED, RIGHT END OPEN
C
C
      ----- VARIABLE DECLARATIONS -----
C
         DIMENSION 12(4), X2(4), XEXACT(6), YEXACT(6), LNODE(4), RNODE(4),
                   SIGMA(4.2)
C
C
      ++++++ USER INPUT REQUIRED HERE ++++++++++
  ---- SET THE DIMENSIONS EQUAL TO N -----
C
         DIMENSION A(101),Q(101),QQ(101),RR(101),S(101),
                   NEWRR(101), NEWS(101), NEWQQ(101),
        C
                   PARRAY(101), DARRAY(101), SARRAY(101),
                   QARRAY(101), XARRAY(101)
C
         INTEGER I, J, N, JSTOP, Y, GRAPHS, COUNT, PLTCNT, BDRY, SK, RBNDRY,
                 SKIP, I2, LWPRES, HALT, LNODE, RNODE, LBNDRY, LBDPRS, RBDPRS
         DOUBLE PRECISION TRI, PRI, QLI, QRI, DRI, G, G1, G2, SIGMA, EE, NEHQQ,
                         DELT, H, ND, X2, AR, W, DQ, VS, T, A, Q, QQ, RR, S, NEWRR, NEWS,
        C
                         LBDPRI, LBDTRI, LBDDRI, LBDPR, LBDDR, LBDTR, QLBD,
        C
                         RRA, QQA, AA, SA, QA, RRB, QQB, AB, SB, QB,
                         RBOPRI, RBOTRI, RBODRI, RBOPR, RBOOR, RBOTR, QRBO,
        C
                         QCS, VTEW, VHEW
         REAL VTAIL, VCDE, VSE, DLSH, DLCD, XINIT, VHEAD,
```

```
XEXACT, YEXACT, PARRAY, DARRAY, SARRAY, QARRAY, XARRAY
        COMMON AR, DQ, VS, H
      ---- ENTER THE APPROPRIATE VALUES BELOW -----
C
        N= 101
        GRAPHS=1
      ---- FOR GRAPH = 1 OR 2 MUST ENTER CHANGES IN SUBROUTINE ----
     ---- BORDER AND SUBROUTINE EXACT ----
      ---- LINES "FIRST ORDER N = ???"
                 "DENSITY RATIO = ???" TEMP RATIO = ???"
                 "PRESSURE RATIO = ???"
        SKIP=18
         JSTOP=101
         TRI=1.0000
         PRI=5.0000
         DRI=5.0000
         QLI=0.0000
         QRI=0.0000
         LBOPRI = 1.000
         LBOTRI = 1.000
         LBODRI = 1.DOO
         RBDDRI = 1.000
         RBDPRI = 4.000/5.000
         RBOTRI = 1.000
         G=1.4000
         EE=0.10-8
C
C ---- DENOTE LOW PRESSURE SIDE BY SETTING ----
C ---- LWPRES = 2 IF LOW PRESSURE ON RIGHT
C ---- LMPRES = 3 IF LOW PRESSURE ON LEFT
C
         LMPRES = 3
C ---- SET BOUNDARY CONDITIONS BY SPECIFING OPEN OR CLOSED ----
C ---- LBNDRY: OPEN = 0, CLOSED = 1 (FOR LEFT BOUNDARY) ----
C ---- IF OPEN SPECIFY IF PRESSURE IS TO BE MAINTAINED AT LBDPRI ----
C --- OR IF IT CAN ADJUST TO PREVENT ANY HAVES FORMING AT THE BOUNDARY -
C ---- LBOPRS: CONSTANT = 0, ADJUSTABLE = 1 ----
C ---- DO THE SAME FOR RIGHT BOUNDARY; RBNDRY, RBDPRS ----
C
         LBNDRY = 1
         LBOPRS = 1
         RBNDRY = 0
         RBDPRS = 0
         ----- EXACT SOLUTION VALUES ------
         XINIT=0.50
         VHEAD= 1.0
         VTAIL= 0.310557
         VCDE=-.574487
         VSE=-1.402346
         DLCD=2.713115
         DLSH=1.69344
         SIGMA(1,2)=0.50000001D00
         SIGMA(2,2)=0.50000001D00
         SIGMA(3,2)=0.50000001000
         SIGMA(4,2)=0.50000001000
C
      +++++++ END OF USER INPUT AREA +++++++
         SK = 0
         T=0.0000
         00 10 I=1,4
             I2(I)=0
             LNODE(I) = 0
             RNODE(I) = 0
             X2(I)=0.0D00
```

```
SIGMA(1,1)=0.0000
    10 CONTINUE
        NO=DBLE(N)
        H=1.D00/(ND-1.D00)
        00 11 I=1,N
             A(I)=0.0000
             Q(I)=0.0000
             NEHQQ( I )=0.0000
             NEWRRII)=0.0000
             NEWS(I)=0.0000
             GARRAY(I)=0.0
             PARRAY(I)=0.0
             DARRAY(I)=0.0
             SARRAY(I)=0.0
             XARRAY(I)=FLOAT(I-1)*SNGL(H)
    11 CONTINUE
         DELT=2.0000
 ----LOAD INITIAL REIMAN VALUES INTO NODE LOCATIONS, FIRST FROM NODE---
C ---- TO MIDPOINT (Y), AND THEN FROM Y TO N. NOTE IF SHOCK DOES NOT--
C ----START AT MIDPOINT THEN Y SHOULD BE SET TO NODE WHERE SHOCK -----
  ----INITIALLY IS----
C
         AR=1.0000
         DQ=0.0000
         H=1.0000
         VS=0.0000
         QCS=0.D00
         VHEW=0.DOO
         VTEM=0.000
         G1=1.D00/(G-1.D00)
         G2=2.000/(G-1.000)
  ---- FLON RIGHT ----
         IF(LWPRES.EQ.2) THEN
         LBODR = DRI * LBDDRI
         LBOPR = PRI * LBOPRI
         LBOTR = TRI * LBOTRI
         QLBD = QLI
         RBDDR = RBDDRI
         RBOPR = RBOPRI
         RBOTR = RBOTRI
         QRBD = QRI
             Y = (N+1)/2
         Y = 38
C
             DO 12 I=1,Y
                  S(I)=G2-(G1/G)*DLOG(PRI/((DRI)**G))
                  QQ(I)=QLI+OSQRT(TRI)*S(I)
                  RR(I)=QLI-OSQRT(TRI)*S(I)
           CONTINUE
     12
              Y=(N+3 1/2
         Y=39
              DO 13 I=Y,N
                  S( I )=G2
                  QQ(I)=QRI+S(I)
                  RR(I)=QRI-S(I)
           CONTINUE
         ELSE
  ---- FLOH LEFT ----
C
         LBODR = LBODRI
         LBDPR = LBDPRI
         LBOTR = LBOTRI
         GLBD = GLI
         RBODR = RBODRI * DRI
         RBOPR = RBOPRI * PRI
         RBUTR = RBOTRI * TRI
```

```
QRBO = QRI
             Y = (N-1)/2
        Y = 13
             DO 14 I=1,Y
                  S( I )=G2
                  QQ(I)=QLI+S(I)
                  RR(I)=QLI-S(I)
          CONTINUE
    14
             Y = (N+1)/2
        Y = 14
             DO 15 I=Y,N
                  S(I)=G2-(G1/G)*DLOG(PRI/((DRI)**G))
                  QQ(I)=QRI+DSQRT(TRI)*S(I)
                  RR(I)=QRI-DSQRT(TRI)*S(I)
          CONTINUE
         END IF
 ---- SET UP GRAPHICS PLOTS OF VARIABLES ----
        IF (GRAPHS.GT.0) THEN
             CALL COMPRS
         CALL TEK618
             CALL HWROT( 'AUTO')
             CALL HWSCAL( 'SCREEN')
             IF (GRAPHS.EQ.2) THEN
                CALL PAGE(11.0,8.5)
             ELSE
                CALL PAGE(8.5,11.0)
             END IF
             IF (GRAPHS.EQ.1) THEN
             CALL BORDER( JSTOP )
             END IF
         END IF
         HALT = 0
         J=1
         COUNT=1
         IF (GRAPHS.EQ.1) THEN
             CALL PLOTIJ, JSTOP, N, QQ, RR, S, H, XARRAY, PARRAY,
       #DARRAY, GARRAY, SARRAY, G, G1, G2)
         END IF
C ---- BURST DIAPHRAGM ----
         CALL TIME(N,QQ,RR,S,DELT,H)
        CALL DBURST(N,H,QQ,RR,S,G,G1,G2,DELT,I2,X2,W,AR,DQ,VS,LWPRES,
                    SIGMA,A,Q)
C
         IF (GRAPHS.EQ.O) THEN
             CALL LIST(N,SIGMA,QQ,RR,S,G,G1,G2,J,T,DELT,VS,QCS,VTEH,VHEH,
                      XINIT, VHEAD, VTAIL, VCDE, VSE)
         END IF
C ---- BEGIN CALCULATION FOR JUMP TO NEXT TIME AND CONTINUE ----
  ---- UNTIL EITHER JSTOP REACHED OR SHOCK MEETS CONTACT SURFACE ----
   16 IF (J.EQ.JSTOP) GOTO 18
         PLTCNT=J/SKIP
         CALL TIME(N,QQ,RR,S,DELT,H)
C
         CALL TRAK(N,SIGMA,H,QQ,RR,S,G,G1,G2,DELT,I2,X2,W,AR,DQ,VS,J,
                   LWPRES,QCS,VHEW,VTEW)
C
         CALL SHEEP(N,H,SIGMA,QQ,RR,S,DELT,EE,Q,A,NEWQQ,NEWRR,NEWS,12,G2,
                    J, LNODE, RNODE, HALT, LBNDRY, LBDPRS, LBDPR, LBDTR, LBDOR,
                    QLBD,G,G1,RBNDRY,RBOPRS,RBOPR,RBOTR,RBODR,QRBO,BDRY,
                    SK)
C
         IF(LNODE(4).LT.J) THEN
```

```
LN00E(1) = 0
                 RNODE(1) = 0
                 GO TO 17
         END IF
         IF(RNODE(4).LT.LNOOE(4)) THEN
               RNODE(1) = 0
         CALL CORRCT(LNODE, RNODE, N, SIGMA, H, QQ, RR, S, G, G1, G2, I2, X2, M, AR, DQ,
                     VS.A.Q)
    17 IF (SIGMA(1,2).GE.1.DOO) THEN
                 IF(RBNDRY.EQ.0) THEN
                         IF(SIGMA(1,2).NE.3.DOO) THEN
                         SK = 2
                         CALL BONDRY(Q(N),Q(N-1),QRBD,A(N),A(N-1),QQ(N),QQ(N-1),
        C
                                 RR(N), RR(N-1), S(N), S(N-1), H, EE, DELT,
        C
                                 RBNDRY, RBDPRS, RBDPR, RBDDR, RBDTR, J, NEWQQ(N),
        C
                                NEHRR(N), NEHS(N), G, G1, G2, HALT, BDRY, SK)
                         END IF
                 ELSE
                         CALL EXTRAP(RR(N-1),RR(N-2),QQ(N-1),QQ(N-2),S(N-1),
        C
                                SIN-2),H,H,RRA,QQA,SA,AA,QA)
                         CALL SRFLCT(QQA,RRA,SA,SIGMA,VS,DELT,LMPRES,
                                RR(N),QQ(N),S(N),Q(N),A(N),G,G1,G2)
                 END IF
         END IF
         IF (SIGMA(1,2).LE.O.DOO) THEN
                 IF(LBNDRY.EQ.0) THEN
                         IF(SIGMA(1,2).NE.-2.DOO) THEN
                         BDRY = 3
                         SK=2
                         CALL BONDRY(Q(1),Q(2),QLBD,A(1),A(2),QQ(1),QQ(2),
        C
                                 RR(1), RR(2), S(1), S(2), H, EE, DELT,
        C
                                 LBNDRY, LBDPRS, LBDPR, LBDDR, LBDTR, J, NEWQQ(1),
        C
                                 NEHRR(1), NEHS(1), G, G1, G2, HALT, BDRY, SK)
                         END IF
                 ELSE
                         CALL EXTRAP(RR(2), RR(3), QQ(2), QQ(3), S(2),
        C
                                 S(3),H,H,RRB,QQB,SB,AB,QB)
                         CALL SRFLCT(QGB, RRB, SB, SIGMA, VS, DELT, LMPRES,
                                 RR(1),QQ(1),S(1),Q(1),A(1),G,G1,G2)
                 END IF
         END IF
         T=T+DELT
  ---- OUTPUT DATA ----
         IF ((COUNT.EQ.PLTCNT*SKIP).AND.(GRAPHS.EQ.1))
        C
             THEN
C
      IF((J.GT.55)) THEN
              CALL PLOT(J, JSTOP, N, QQ, RR, S, H, XARRAY, PARRAY,
        CDARRAY, QARRAY, SARRAY, G, G1, G2)
      END IF
         END IF
         IF ((COUNT.EQ.PLTCNT*SKIP).AND.(GRAPHS.EQ.0))
        C
              THEN
              CALL LIST(N,SIGMA,QQ,RR,S,G,G1,G2,J,T,DELT,VS,QCS,VTEH,VHEH,
        C
                       XINIT, VHEAD, VTAIL, VCDE, VSE)
         END IF
         IF ((COUNT.EQ.PLTCNT*SKIP).AND.(GRAPHS.EQ.2))
             THEN
         IF (J.GT.50) THEN
              CALL EXACTIN, XINIT, T, VHEAD, VTAIL, VCDE, VSE, DLCD, DLSH, QQ, RR, S, H,
        CXARRAY, DARRAY, G, G1, G2, DRI)
         END IF
         END IF
```

```
IF(HALT.EQ.1) GO TO 18
        J=J+1
       COUNT=COUNT+1
       60 TO 16
  18 CALL DONEPL
       END
     Ç
C
       SUBROUTINE LIST(N,SIGMA,QQ,RR,S,G,G1,G2,J,T,DELT,VS,QCS,VTEH,
                      VHEW, XINIT, VHEAD, VTAIL, VCDE, VSE)
C
     **************
C
C
C
            TABULAR RESULTS SUBROUTINE
C
     C
C
     ----- VARIABLE DEFINITIONS -----
C
     DENS - DENSITY
C
     PRESS - PRESSURE
     TEMP - TEMPERATURE
        INTEGER I,J,N,L
        DIMENSION SIGMA(4,2),QQ(N),RR(N),S(N)
        DOUBLE PRECISION SIGMA, QQ, RR, S, PRESS, VTEM, VHEM, QCS, TEMORE,
                       TEMP, DENS, G, G1, G2, Q, T, DELT, VS, HEMXE,
                       XINIT, VHEAD, VTAIL, VCDE, VSE, SKXE, CSXE
C
                                               ELAPSED TIME IS',T
        MRITE(9,*) 'TIME LEVEL',J,'
        HRITE(9,*) 'TIME STEP IS', DELT,'
                                        SHOCK VELOCITY IS', VS
        MRITE(9,*) 'CONTACT SURFACE VELOCITY IS', QCS
        WRITE(9,#) 'HEAD EXPANSION WAVE VELOCITY IS', VHEW
        HRITE(9,#) 'TAIL EXPANSION HAVE VELOCITY IS', VTEH
        HRITE(9,#)
        HRITE(9,*) '
                                 VELOCITY
                                                 DENSITY
                     NODE
       CPRESSURE '
        MRITE(9,*) ' '
        DC 61 I=1,N
        TEMP=(QQ(I)-RR(I))*(QQ(I)-RR(I))/(4.D00*S(I)*S(I))
        DENS=((1.000/TEMP)*0EXP(G*(1.000-G)*(S(I)-G2)))**(-G1)
        PRESS=TEMP+DENS
        Q=(QQ(I)+RR(I))/2.0000
        WRITE (9,65) I,Q,DENS,PRESS
    65 FORMAT (4X,12,7X,F12.6,7X,F12.6,7X,F12.6)
    61 CONTINUE
        HRITE(9,#) ' '
        MRITE(9,#) ' '
        MRITE(9,*) '
                     NOOE
                                                      RR
       CHODIFIED S'
        HRITE(9,*) ' '
        DO 62 I=1.N
        MRITE (9,66) I,QQ(I),RR(I),S(I)
    66 FORMAT (4X,12,7X,F12.6,7X,F12.6,7X,F12.6)
    62 CONTINUE
        MRITE(9,#) ' '
        MRITE(9,#) ' '
        HRITE(9,#) '
                        DISCONTINUITY LOCATIONS AT TIME LEVEL', J
        WRITE(9,*) ' '
         MRITE(9,#) '
                          TYPE
                                      LOCATION'
        DO 63 L=1,4
            HRITE(9,#) L,'
                          ',SIGMA(L,2)
    63 CONTINUE
        WRITE! 9.#1 '
        MRITE(9,#) '----
        HRITE(9,#) ' '
```

```
MRITE(9,#) ' '
        IFIJ.EQ.1) THEN
                                     SHOCK
                                                 CONTACT
                                                             HEAD
        MRITE(10,#) '
                        TIME
      C TAIL'
        MRITE(10,*) ' '
        END IF
        MRITE(10,67) T,SIGMA(1,1),SIGMA(2,1),SIGMA(3,1),SIGMA(4,1)
    67 FORMAT (1X,F12.6,1X,F12.6,1X,F12.6,1X,F12.6,1X,F12.6)
        IF(J.EQ.1) THEN
                       EXACT VALUES'
        MRITE(8,#) '
        MRITE(8,*) '
                                    SHOCK
                                                CONTACT
                                                            HEAD
                       TIME
       C TAIL'
        HRITE(8.#)
        END IF
        SKXE=XINIT+VSE#T
        CSXE=XINIT+VCDE#T
        HENCE =XINIT+VHEAD#T
        TENCE=XINIT+VTAIL#T
        MRITE(8,68) T, SKXE, CSXE, HENCE, TENCE
    68 FORMAT (1X,F12.6,1X,F12.6,1X,F12.6,1X,F12.6)
        RETURN
        END
C
        SUBROUTINE TIME(N,QQ,RR,S,DELT,H)
C
C
      C
C
            CALCULATE TIME STEP SUBROUTINE
C
¢
     ***********************************
     -----NEM VARIABLE DEFINITIONS -----
C
     THIN - RUNNING VALUE OF THE MINIMUM TIME STEP
        INTEGER N,I
        DIMENSION QQ(N),RR(N),S(N)
        DOUBLE PRECISION H,A,QQ,RR,S,DELT,TMIN,Q
        TMIN=2.0000
        DO 21 I=1,N
            A=(QQ(I)-RR(I))/(2.D00#S(I))
             Q=(QQ(I)+RR(I))/2.0D00
            DELT=H/(DABS(DABS(Q)+A))
            IF (DELT.LT.TMIN) THEN
             TMIN=DELT
             END IF
    21 CONTINUE
        DELT=0.99D00*TMIN
        RETURN
        END
C
        SUBROUTINE TRAKIN, SIGMA, H, QQ, RR, S, G, G1, G2, DELT, I2, X2, M, AR, DQ, VS,
       #J,LMPRES,QCS,VHEH,VTEH)
C
     伊州州州州北京市政治政策的政治政治政治政治政治政治政治政治政治政治政治政治政治政治政治政治
C
C
            DISCONTINUITY TRACKING SUBROUTINE
C
C
      C
      ----- VARIABLE DEFINITIONS -----
C
C
      CSDIR - CONTACT SURFACE DIRECTION, 2 TO THE RIGHT,3 TO THE LEFT
     CSRMN - RIEMANN VARIABLE CHANGE ACROSS A CONTACT SURFACE
C
         - THE RATIO OF THE DENSITY ACROSS A
            SHOCK, B/AIRIGHT).8/AILEFT)
C
      DREMM - DUMMY VARIABLE
C
         - THE RATIO OF THE PRESSURE ACROSS A
            SHOCK, A/BIRIGHT),B/AILEFT)
```

```
MREIMN - THE MEASURED JUMP IN QQ ACROSS THE SHOCK,
               FROM A TO B.
¢
      EREIMN - THE JUMP IN QQ ACROSS THE SHOCK CALCULATED ANALYTICALLY
C
      AS A FUNCTION OF M. SAP - ENTROPY TO THE LEFT OF THE SHOCK FOR FLOWS RIGHT
C
C
C
            OR ENTROPY TO THE RIGHT OF THE C.S. FOR FLOMS LEFT
      SBP - ENTROPY TO THE RIGHT OF THE C.S. FOR FLOWS RIGHT
C
C
            OR ENTROPY TO THE LEFT OF THE SHOCK FOR FLOWS LEFT
      SHKDIR - SHOCK DIRECTION OF TRAVEL, 3 TO THE LEFT, 2 TO THE RIGHT
C
      TS - TIME FOR SHOCK TO TRAVEL ONE INTERVAL
C
C
      X - DISTANCE FROM LEFT BOUNDARY TO NODE
         INTEGER N,I,Y,I2,L,J,SHKDIR,CSDIR,LWPRES
         DIMENSION SIGMA(4,2),X2(4),RR(N),QQ(N),S(N),I2(4)
         DOUBLE PRECISION SIGMA, X2, X, H, AB, SA, SB, AA, QA, QB, QQA, QQB, RRA, RRB,
                          RR,QQ,S,TS,W,DQ,AR,PR,G,G1,G2,VS,DELT,CSRMN,
                          Q, MREIMN, DREMN, EREIMN, WH, SA1, SA2, SAP, SBP
       C
                          AM, QM, VHEM, VTEM, TIME, QCS
C
      ++++++ LOCATING THE UPSTREAM NODE ++++++++
         DO 10 L=1,4
              SIGMA(L,1)=SIGMA(L,2)
              Y=0
              X=0.000
              I=1
          IF (.NOT.(Y.EQ.0)) GOTO 10
                 IF (SIGMA(L,1).LT.X) THEN
                     X2(L)=X
                     I2(L)=I
                     Y=1
                 END IF
              X=X+H
              I=I+1
              GOTO 11
   10
        CONTINUE
C
  ---- IF SHOCK HAS LEFT AN OPEN BOUNDARY OUT OF THE TUBE THEN SET ----
C
  ---- SHOCK TO NEUTRAL -----
C
         IF (12(1).GT.N) THEN
               SIGMA(1,1) = 2.000
               SIGMA(1,2) = 3.000
               W = 1.000
               VS = 1.000
               DQ = 0.000
               AR = 0.000
               PR = 1.000
               DR = 1.000
               GO TO 150
         ELSE IF(12(1).LT.2) THEN
               SIGMA(1,1) =-1.000
               SIGMA(1,2) =-2.000
               H = 1.000
                VS =-1.000
               DQ = 0.000
                AR = 0.000
                PR = 1.000
               DR = 1.000
               GO TO 150
         END IF
C
      +++++++++ DETERMINING SHOCK SPEED +++++++
¢
           IF((J.Eq.1).OR.(I2(1).Eq.2).OR.(I2(1).Eq.N)) THEN
C ----AT TIME ZERO OR BOUNDARYS DETERMINE CORRECT SHOCK DIRECTION-----
C ----SHKDIR = 3 IS A SHOCK HEADED LEFT, AND SHKDIR = 2 IS SHOCK-----
C ----TRAVELING RIGHT----
```

```
C
                  IF(LMPRES.EQ.3) THEN
                         SHKDIR = 3
                         IF (J.EQ.1) THEN
                                 X2(1) = X2(1) - H
                                 I2(1) = I2(1) - 1
                                 X2(2) = X2(2) - H
                                 I2(2) = I2(2) - 1
                         END IF
                         GO TO 20
                  ELSE
                         SHKDIR = 2
                  END IF
                  GO TO 20
C
C ----IF SHOCK AND CONTACT SURFACE ARE NOT WITHIN THE SAME----
C ---- INTERVAL THEN NO CORRECTIONS ARE NEEDED IN CALCULATING----
C ----THE REIMAN VARIABLE JUMP ACROSS THE SHOCK----
C
          ELSE IF (12(1).NE.12(2)) THEN
                  IF((SHKDIR.EQ.3).AND.(SIGMA(1,1).EQ.(X2(1)-H))) THEN
                          X2(1) = X2(1) - H
                          I2(1) = I2(1) - 1
                  END IF
                  GO TO 20
C ----IF SHOCK AND CONTACT SURFACE ARE WITHIN THE SAME INTERVAL----
  ----THEN CORRECTIONS ARE REQUIRED TO DETERMINE SHOCK STRENGTH----
           ELSE IF(SHKDIR.EQ.3) THEN
  ----SHOCK LOCATION RELATIVE TO THE CONTACT SURFACE FOR A SHOCK----
C
  -----HEADED TO THE LEFT DETERMINES THE CORRECT VALUES FOR W AND VS--
C
                  IF(SIGMA(1,1).GT.SIGMA(2,1)) THEN
                          GO TO 111
                  ELSE IF(SIGMA(1,1).EQ.(X2(1)-H)) THEN
                          X2(1) = X2(1) - H
                          I2(1) = I2(1) - 1
                          X2(2) = X2(2) - H
                          I2(2) = I2(2) - 1
                   END IF
     15
                   RRA=RR(12(1)-1)
                          RRB=RR(12(1))
                          QQA=QQ(12(1)-1)
                          QQB=QQ(12(1))
                          SA=S(12(1)-1)
C
                          QA =(QQA+RRA)/2.000
                          QB =( QQB+RRB )/2.000
                          AA =(QQA-RRA)/(2.000*SA)
                          DQ ={QB-QA}/AA
                          H = DSQRT((DQ**2)*(0.36D00)+1.D00) - (DQ*0.6D00)
                          DQ =(-1.000)*DQ
                          GO TO 110
C -----FOR SHOCK HEADED RIGHT THE SAME PROCEDURE FOR CORRECTIONS ARE---
   ----FOLLOWED-----
C
           ELSE IF(SIGMA(1,1).LT.SIGMA(2,1)) THEN
                          GO TO 111
           ELSE
     17
                   RRA=RR(12(1)-1)
                          RRB=RR([2(1))
                          QQA=QQ(12(1)-1)
                          QQB=QQ([2(1))
                          SB=S(12(1))
                          QA =(QQA+RRA)/2.DOO
                          QB =(QQB+RRB)/2.000
```

```
AB =(QQB-RRB)/(2.D00*SB)
                         DG =(QA-QB)/AB
                         M = DSQRT((DQ**2)*(0.36D00)+1.D00) + (DQ*0.6D00)
                         GO TO 110
          END TE
C -----NITH NO SHOCK/CONTACT SURFACE INTERACTION THE JUMP IN REIMAN-----
C -----VARIABLES ARE DETERMINED HITHOUT INTERPOLATION OVER THE ----
C ----INTERVAL. MREIMN IS THE MEASURED JUMP. EREIMN IS THE ANALYTICAL--
C ----VALUE----
    20 RRA=RR(12(1)-1)
         RRB=RR(12(1))
         QQA=QQ(12(1)-1)
         QQB=QQ(I2(1))
         SA=S(I2(1)-1)
         SB=S(12(1))
    21 AB=(QQB-RRB)/(2.D00*SB)
         AA=(QQA-RRA)/(2.D00*SA)
         IF(SHKDIR.EQ.3) THEN
                MREIMN = (RRB-RRA)/AA
                DREMN = DABS(MREIMN)
         ELSE
                MREIMN = (QQA-QQ8)/AB
                DREMN = MREIMN
         END IF
C ----ITERATE FOR PROPER VALUE OF M USING THE QUADRATIC FIT OF THE----
  ----REIMAN VARIABLE CHANGE WITH W CURVE. NOTE LEFT MOVING SHOCKS----
  ----ARE USED IN THESE EQUATIONS SINCE RRB-RRA/AA=-(QQA-QQB/AB)-----
   100 HH= (3.0396408D01-((DREMN+2.7574D00)/0.286337D00))
         H=5.513294000-DSQRT(HH)
         DQ=2.D00*(W*W-1.D00)/(W*(G+1.D00))
         AR*DSQRT(2.D00*(G-1.D00)*(1.D00+((G-1.D00)*H*H/2.D00))*
                (G*G2*H*H-1.D00))/((G+1.D00)*H)
         PR=(2.D00*G/(G+1.D00))*H*H-((G-1.D00)/(G+1.D00))
         DR=((G-1.D00)*H*H+2.D00)/((G+1.D00)*H*H)
         EREIMN=DQ+(AR-1.DOO)*G2-(AR*G1/G)*DLOG(PR*(DR**G))
         IF (DABS(EREIMN-DABS(MREIMN)).LT.0.1D-5) GO TO 110
         DREMN = (DABS(MREIMN) - EREIMN) + DREMN
         GOTO 100
  ----SHOCK VELOCITY DEPENDS ON DIRECTION SHOCK IS TRAVELING ----
  ----LEFT IS < 0, AND RIGHT IS > 0 -----
   110 IF (J.EQ.1) THEN
                TIME = 0.000
                 SA1 = (G1/G)*DLOG((2.D00*G*(W**2)-G+1.D00)/(G+1.D00))
                 SA2 = G1*DLOG(((G-1.D00)*(W**2)+2)/((G+1.D00)*(W**2)))
                 IF(SHKDIR.EQ.2) THEN
                        SAP = SB - SA1 - SA2
                        SBP = SAP
                ELSE
                        SBP = SA - SA1 - SA2
                        SAP = SBP
                 END IF
   103
            IF(SHKDIR.EQ.2) THEN
                        CSRMN =((DEXP((SBP-SA)/G2))*(SA)-(SBP))*AR
                        CSRMN =((DEXP((SAP-SB)/G2))*(SB)-(SAP))*AR
                 END IF
                 IF(SHKDIR.EQ.3) THEN
                        MREIMN =((RRB-RRA)/AA)+CSRMN
                        DREMN = DABS(MREIMN)
                 ELSE
                        MREIMN #((QQA-QQB)/AB)-CSRMN
                        DREMN - MREIMN
                 END IF
```

```
101
            HH=(3.0396408001-((DREHN+2.7574000)/0.286337000))
                H=5.513294D00-DSQRT(HH)
                DQ=2.D00*(H#H-1.D00)/(H#(G+1.D00))
                AR=DSGRT(2.D00*(G-1.D00)*(1.D00+((G-1.D00)*HHH/2.D00))*
       C
                     (G+G2*H*H-1.D00))/((G+1.D00)*H)
                PR=(2,D00*G/(G+1,D00))*H*H~((G-1,D00)/(G+1,D00))
                DR=((G-1.D00)*H*H+2.D00)/((G+1.D00)*H*H)
                EREIMN=DQ+(AR-1.DOO)#G2-(AR#G1/G)*DLOG(PR*(DR**G)) .....
                IF (DABS(EREIMN-DABS(MREIMN)).LT.0.10-5) GO TO 102
                DREMN = (DABS(MREIMN) - EREIMN) + DREMN
                GOTO 101
  102
           SA1 = (G1/G)*DLOG((2.D00*G*(H**2)-G+1.D00)/(G+1.D00))
                SA2 = G1*DLOG(((G-1.D00)*(W**2)+2)/((G+1.D00)*(W**2)))
                IF(SHKDIR.EQ.2) THEN
                        SAP = SB - SA1 - SA2
                ELSE
                        SBP = SA - SA1 - SA2
                END IF
                IF (DABS(SAP-SBP).LT.0.10-5) GO TO 105
                IF(SHKDIR.EQ.2) THEN
                      SBP = (SAP-SBP) + SBP
                ELSE
                      SAP = (SBP-SAP) + SAP
                END IF
                60 TO 103
        END IF
  105 IF(SHKDIR.EQ.3) THEN
                DQ = (-1.000)*DQ
                VS = ((RRA+QQA)*0.5000) - (H*AA)
        ELSE
                VS=(QQB+RRB)*0.5000+H*AB
        END IF
        TS=H/DABS(VS)
  111 IF (TS.LT.DELT) THEN
             DELT=0.99000*TS
        END IF
        SIGMA(1,2)=VS*DELT+SIGMA(1,1)
  +++++DETERMINE CONTACT SURFACE SPEED+++++++
         IF(J.EQ.1) THEN
                CSDIR = SHKDIR
         END IF
  ---- CONTACT SURFACE TRAVELING RIGHT ----
   150 IF(CSDIR.EQ.2) THEN
  ----CONTACT SURFACE MOVING RIGHT, CHECK FOR SHOCK IN INTERVAL----
C ----AND CALCULATE SPEED OF CONTACT SURFACE AS APPROPRIATE----
                IF(J.EQ.1) THEN
                        QB =( QQB+RRB )/2.000
                        QA = DQ*AB + QB
                        CALL SKJUMP(AB, 9B, SB, AR, DQ, VS, G, G1, N, AA, QA, SA)
                        Q = QA
                        GO TO 200
                END IF
                IF(X2(2).EQ.X2(1)) THEN
                        IF(SIGMA(2,1).LE.SIGMA(1,1)) THEN
                                Q = (QQ(12(2)-1) + RR(12(2)-1)) / 2.000
                        ELSE
                                Q = (QQ(12(2)) + RR(12(2))) / 2.000
                        END IF
                FISE
                        QA = (QQ(12(2)-1) + RR(12(2)-1)) / 2.000
                        QB = (QQ(1212)) + RR([2(2))) / 2.000
                        Q = (QA + QB)/2.000
                 END IF
```

```
ELSE IF(CSDIR.EQ.3) THEN
C ---- CONTACT SURFACE TRAVELING LEFT ----
               IF(J.EQ.1) THEN
                      QA =(QQA+RRA)/2.000
                      QB = DQ#AA + QA
                      CALL SKJUMP(AA,QA,SA,AR,DQ,VS,G,G1,W,AB,QB,SB)
                      GO TO 200
               END IF
               IF(X2(2).EQ.X2(1)) THEN
                      IF(SIGMA(2,1).GE.SIGMA(1,1)) THEN
                             Q = (QQ(I2(2)) + RR(I2(2))) / 2.000
                      ELSE
                             Q = (QQ(I2(2)-1) + RR(I2(2)-1)) / 2.000
                      END IF
               ELSE IF(SIGMA(2,1).EQ.(X2(2)-H)) THEN
                      X2(2) = X2(2) - H
                      I2(2) = I2(2) - 1
                      Q = (QQ(12(2))+RR(12(2))) / 2.000
               ELSE
                      QA = (QQ(I2(2)-1) + RR(I2(2)-1)) / 2.000
                      QB = (QQ(12(2)) + RR(12(2))) / 2.000
                      Q = (QA + QB)/2.000
               END IF
        END IF
   200 SIGMA(2,2) = DELT # Q + SIGMA(2,1)
        QCS≥Q
C
C ---- CALCULATE EXPANSION WAVE SPEED -----
        TIME = TIME+DELT
        IF(J.EQ.3) THEN
               AH=(QQ((N+1)/2)-RR((N+1)/2))/(2.D00*S((N+1)/2))
               QH=Q
               IF((CSDIR).EQ.2) THEN
                       VHEN=-(AH)
                       VTEH= QH-AH
               ELSE
                       VHEW= AM
                       VTEH= QH+AM
               END IF
         END IF
         IF(J.EQ.3) THEN
                SIGMA(3,2) = SIGMA(3,1) + VHEH+TIME
               SIGMA(4,2) = SIGMA(4,1) + VTEH*TIME
         ELSE IF((CSDIR.EQ.2).AND.(SIGMA(3,1).GT.O.DOO)) THEN
               SIGMA(3,2) = SIGMA(3,1) + VHEH*DELT
               SIGMA(4,2) = SIGMA(4,1) + VTEM*DELT
         ELSE IF((CSDIR.EQ.3).AND.(SIGMA(3,1).GT.1.DOO)) THEN
               SIGMA(3,2) = SIGMA(3,1) + VHEH*DELT
                SIGMA(4,2) = SIGMA(4,1) + VTEH*DELT
         END IF
         RETURN
C
         SUBROUTINE SHEEP(N,H,SIGMA,QQ,RR,S,DELT,EE,Q,A,NEHQQ,NEHRR,NEHS,
       CI2,G2,J,LNODE,RNODE,HALT,LBNORY,LBDPRS,LBDPR,LBDTR,LBDDR,QLBD,G,
       CG1,RBNDRY,RBDPRS,RBDPR,RBDTR,RBDDR,QRBD,BDRY,SK)
      C
C
              SPACE SHEEPING SUBROUTINE
C
      ----- VARIABLE DEFINITIONS -----
c
```

```
AAVG - AVERAGE SPEED OF SOUND
      CNTACT - 3 DIGIT VARIABLE DENOTING CONTACT SURFACE
               LOCATION, DIRECTION OF TRAVEL, AND IF IT CROSSES A NODE
      DELQQH - CHANGE IN QQ FROM I TO I+1
      DELQQL - CHANGE IN QQ FROM I-1 TO I
      DELRRH - CHANGE IN RR FROM I TO I+1
      DELRRL - CHANGE IN RR FROM I-1 TO I
      DELSH - CHANGE IN S FROM I TO I+1
            - CHANGE IN S FROM I-1 TO I
      DELSL
      DELAH
            - CHANGE IN A FROM I TO I+1
C
      DELAL
            - CHANGE IN A FROM I-1 TO I
            - CHANGE IN Q FROM I TP I+1
C
      DELOH
      DELQL - CHANGE IN Q FROM I-1 TO I
C
C
      DELX
            - INTERPOLATION DISTANCE (LMD*0ELT)
      DLTA** - PREFIX WHICH INDICATES THE SPATIAL
               CHANGE IN ** FOR ONE TIME STEP.
      INTEG(K)- RESULT OF INTEGRATING Z(K)
      **INT - VALUE OF ** INTERPOLATED BETWEEN NODES
C
C
               ON THE CURRENT TIME LEVEL.
      LXX - NOOE DEFINING THE LEFT INTERVAL
C
      *PRIM(K)- SUFFIX WHICH INDICATES THE SPATIAL
C
               DERIVITIVE OF * AT THE CURRENT TIME LEVEL.
      RXX - NODE DEFINING THE RIGHT INTERVAL
C
      SAVG - AVERAGE ENTROPY
      SHOCK - 3 DIGIT VARIABLE DENOTING SHOCK
              LOCATION, DIRECTION OF TRAVEL, AND IF IT CROSSES A NODE
      **STEP - THE CHANGE IN TIME OF ** AT A NODE
               USED TO STEP UP TO THE NEXT TIME LEVEL
             - LOCATION IN SPACIAL PLANE (I-1)*H
      Z(K)
             - RIGHT SIDE OF THE K'TH EQUATION.
         INTEGER I, RXX, LXX, SHOCK, CNTACT, I2, J, LNODE, RNODE, HALT,
                N, LBNDRY, LBDPRS, RBNDRY, RBDPRS, SK, BDRY
         DIMENSION SIGMA(4,2),S(N),Q(N),A(N),I2(4),QINT(3),AINT(3),Z(3),
                   NEWGG(N), NEWRR(H), NEWS(N), INTEG(3), APRIM(3), QPRIM(3),
       C
                   LNODE(4), RNODE(4), AAVG(3), RR(N), QQ(N)
         DOUBLE PRECISION AAVG, SAVG, G2, X, H, SIGMA, QQ, RR, S, Q, A, G, G1,
                          DELQQH, DELQQL, DELRRH, DELRRL, DELSH, DELSL,
                          DELAH, DELAL, DELQH, DELQL, DELT,
       C
                          QINT, AINT, QQINT, RRINT, SINT, EE,
        C
                          NEHQQ, NEHRR, NEHS, LBDPR, LBDTR, LBDDR, QLBD,
        C
                          RRSTEP, SSTEP, INTEG, Z, DLTAGQ, QQSTEP,
        C
                          DLTARR, DLTAS, APRIM, QPRIM,
                          RBOPR, RBOTR, RBODR, QRBO
         COMMON ARIDGIVSIA
  ---- COMPUTE VELOCITY AND SPEED OF SOUND AT EACH NODE ----
         DO 10 I= 1,N
                 Q(I) = (QQ(I) + RR(I)) / 2.0000
                 A(I) = ((QQ(I) - RR(I)) / (2.0000 * S(I)))
    10 CONTINUE
C
  ---- AT, VANCE LEFT BOUNDARY TO NEW TIME STEP ----
         BDRY = 3
         IF(12(1).EQ.2) THEN
               SK = 1
         ELSE IF(SIGMA(1,2).EQ.-2.DOO) THEN
               SK = 3
               SK = 0
         END IF
         CALL BONDRY(Q(1),Q(2),QLBD,A(1),A(2),QQ(1),QQ(2),RR(1),RR(2),
                     S(1),S(2),H,EE,DELT,LBNDRY,LBOPRS,LBDPR,LBDDR,LBDTR,
                     J,NEHQQ(1),NEHRR(1),NEHS(1),G,G1,G2,HALT,BDRY,SK)
C ---- AT EACH NODE FROM 2 TO N-1 DETERMINE THE BEST ALGORITHM TO USE--
C ---- TO ADVANCE THAT NODE TO THE NEXT TIME STEP ----
```

```
I=2
    11 IF(I.EQ.N) GO TO 1200
                X=FLOAT(I-1)*H
                DELQQH = QQ(I+1) - QQ(I)
                DELQQL = QQ(I) - QQ(I-1)
                DELRRH = RR(I+1) - RR(I)
                DELRRL = RR(I) - RR(I-1)
                DELSH = S(I+1) - S(I)
                DELSL = S(I) - S(I-1)
                DELAH = A(I+1) - A(I)
                DELAL = A(I) - A(I-1)
                DELQH = Q(I+1) - Q(I)
                DELQL = Q(I) - Q(I-1)
  ---- DEFINE LEFT SECTOR AND RIGHT SECTOR WRT NODE EXAMINED----
          RXX = I + 1
          LXX = I
  ---- TEST FOR SHOCK -----
C
          IF (I2(1).EQ.RXX) THEN
                  SHOCK = 200
                  GO TO 20
          ELSE IF (12(1).EQ.LXX) THEN
                  SHOCK = 300
                  GO TO 20
          ELSE
                  SHOCK = 100
          END IF
          GO TO 30
C
  ---- DETERMINE DIRECTION SHOCK IS TRAVELING ----
    20 IF (SIGMA(1,1).LT.SIGMA(1,2)) THEN
                  SHOCK = SHOCK + 20
          ELSE
                  SHOCK = SHOCK + 30
          END IF
C ---- DETERMINE IF SHOCK CROSSES A NODE IN THIS TIME INTERVAL ----
          IF (SHOCK.EQ.220) THEN
                  IF (SIGMA(1,2).GE.(X+H)) THEN
                         SHOCK = SHOCK + 1
                  ELSE
                         SHOCK = SHOCK + 2
                  END IF
           ELSE IF (SHOCK.EQ.230) THEN
                  IF (SIGMA(1,2).LE.X) THEN
                         SHOCK = SHOCK + 1
                  ELSE
                         SHOCK = SHOCK + 2
                  END IF
          ELSE IF (SHOCK.EQ.320) THEN
                  IF (SIGMA(1,2).GE.X) THEN
                         SHOCK = SHOCK + 1
                  ELSE
                         SHOCK = SHOCK + 2
                  END IF
          ELSE IF (SHOCK.EQ.330) THEN
                  IF (SIGMA(1,2).LE.(X-H)) THEN
                         SHOCK = SHOCK + 1
                  ELSE
                         SHOCK = SHOCK + 2
                  END IF
          END IF
```

```
C ---- TEST FOR CONTACT SURFACE ----
       IF (I2(2).EQ.RXX) THEN
                  CNTACT = 200
                  GO TO 40
          ELSE IF (I2(2).EQ.LXX) THEN
                  CNTACT = 300
                  60 TO 40
          ELSE
                  CNTACT = 100
          END IF
          GO TO 50
  -----DETERMINE DIRECTION CONTACT SURFACE IS TRAVELING -----
С
    40 IF (SIGMA(2,1).LT.SIGMA(2,2)) THEN
                  CNTACT = CNTACT + 20
                  CNTACT = CNTACT + 30
          END IF
C ---- DETERMINE IF CONTACT SURFACE CROSSES A NODE DURING THIS TIME ---
C ---- INTERVAL ----
          IF (CNTACT.EQ. 220) THEN
                  IF (SIGMA(2,2).GE.(X+H)) THEN
                          CNTACT = CNTACT + 1
                         CNTACT = CNTACT + 2
                  END IF
          ELSE IF (CNTACT.EQ.230) THEN
                  IF (SIGMA(2,2).LE.X) THEN
                          CNTACT = CNTACT + 1
                  ELSE
                          CNTACT = CNTACT + 2
                  END IF
          ELSE IF (CNTACT.EQ.320) THEN
                  IF (SIGMA(2,2).GE.X) THEN
                          CNTACT = CNTACT + 1
                  ELSE
                          CNTACT = CNTACT + 2
                  END IF
          ELSE IF (CNTACT.EQ.330) THEN
                  IF (SIGMA(2,2).LE.(X-H)) THEN
                          CNTACT = CNTACT + 1
                  ELSE
                         CNTACT = CNTACT + 2
                  END IF
          END IF
C --- CHECK IF EITHER A SHOCK OR CONTACT SURFACE WITHIN H OF THIS NODE---
C --- DETERMINE PROPER ALGORITHM TO USE FOR CALCULATING EXTENDED REIMAN--
C --- VARIABLE CHANGE ALONG CHARACTERISTICS AT THIS NODE-----
    50 IF (SHOCK.EQ.100.OR.CNTACT.EQ.100) THEN
C
¢
  ---NEITHER A SHOCK NOR A CONTACT SURFACE EXIST NEAR NODE---
C
            IF (SHOCK.EQ.100.AND.CNTACT.EQ.100) THEN
 --- TEST FOR SUBSONIC OR SUPERSONIC FLOM---
C
                   IF (DABS(Q(I)).LT.A(I)) THEN
                           IF(I.EQ.(I2(1)-2)) THEN
                                   IF(J.EQ.1) THEN
                                          IF(SIGMA(1,1).LE.SIGMA(1,2)) THEN
                                                  GO TO 200
                                          END IF
```

END IF

```
END IF
                           IF(I.EQ.(I2(1)+1)) THEN
                                   IF(J.EQ.1) THEN
                                          IF(SIGMA(1,1).GE.SIGMA(1,2)) THEN
                                                  GO TO 300
                                          END IF
                                   END IF
                           END IF
                           GO TO 100
                   ELSE
                           IF (SIGMA(2,1).LE.SIGMA(2,2)) THEN
                                  GO TO 200
                           ELSE
                                   GO TO 300
                           END IF
                   END IF
            END IF
  ---SHOCK OR CONTACT SURFACE ON LEFT, HEADED RIGHT, NO NODES CROSSED--
            IF (SHOCK.EQ.322.OR.CNTACT.EQ.322) THEN
                   IF (DABS(Q(I)).LT.A(I)) THEN
                           GO TO 300
                   ELSE
                           GO TO 500
                   END IF
            END IF
C --- SHOCK OR CONTACT SURFACE ON LEFT, HEADED LEFT, NO NODES CROSSED--
          IF (SHOCK.EQ.332.OR.CNTACT.EQ.332) THEN
                  GO TO 300
  ---SHOCK OR CONTACT SURFACE ON LEFT, HEADED RIGHT, NODE IS CROSSED---
          IF (SHOCK.EQ.321.OR.CNTACT.EQ.321) THEN
                  GO TO 400
          END IF
C ---SHOCK OR CONTACT SURFACE ON LEFT, HEADED LEFT, NODE IS CROSSED---
          IF (SHOCK.EQ.331.OR.CNTACT.EQ.331) THEN
                  GO TO 300
  ---SHOCK OR CONTACT SURFACE ON RIGHT, HEADED RIGHT, NO NODES CROSSED--
C
          IF (SHOCK.EQ.222.OR.CNTACT.EQ.222) THEN
                  GO TO 200
          END IF
C ---SHOCK OR CONTACT SURFACE ON RIGHT, HEADED LEFT, NO NODES CROSSED--
          IF (SHOCK.EQ.232.OR.CNTACT.EQ.232) THEN
                  IF (DABS(Q(I)).LT.A(I)) THEN
                         GO TO 200
                  ELSE
                          GO TO 500
                  END IF
  ---SHOCK OR CONTACT SURFACE ON RIGHT, HEADED RIGHT, NODE CROSSED---
          IF (SHOCK.EQ.221.OR.CNTACT.EQ.221) THEN
                  GO TO 200
          END IF
C --- SHOCK OR CONTACT SURFACE ON RIGHT, HEADED LEFT, JUMPS NODE---
```

```
C
          CO TO 400
          END IF
C --- BRANCH HERE IF SHOCK TO RIGHT OF CONTACT SURFACE----
C --- DETERMINE PROPER ALGORITHM TO USE FOR CALCULATING EXTENDED REIMAN--
C --- VARIABLE CHANGE ALONG CHARACTERISTICS AT THIS NODE-----
          IF (SIGMA(1,1).GT.SIGMA(2,1)) THEN
  --- SHOCK ON LEFT, HEADED RIGHT, NO NODE JUMPED---
C
           IF (SHOCK.EQ.322) THEN
                  IF (CNTACT.EQ.322) THEN
                          IF (DABS(Q(I)).LT.A(I)) THEN
                                 GO TO 300
                          ELSE
                                  GO TO 500
                          END IF
                  ELSE IF (CNTACT.EQ.332) THEN
                          GO TO 800
                  ELSE IF (CNTACT.EQ.331) THEN
                          GO TO 800
                  ELSE
                          GO TO 900
                  END IF
           END IF
  --- SHOCK ON LEFT, HEADED LEFT, NO NODE JUMPED---
           IF (SHOCK.EQ.332) THEN
                  IF (CNTACT.EQ.322) THEN
                          GO TO 300
                  ELSE IF (CNTACT.EQ.332) THEN
                          GO TO 600
                  ELSE IF (CNTACT.EQ.331) THEN
                          GO TO 600
                  ELSE IF (CNTACT.EQ.321) THEN
                          GO TO 700
                   ELSE
                          GO TO 900
                   END IF
           END IF
  --- SHOCK ON LEFT, HEADED RIGHT, JUMPS NODE---
C
           IF (SHOCK.EQ.321) THEN
                  IF (CNTACT.EQ.322.OR.CNTACT.EQ.321) THEN
                          GO TO 400
                   ELSE IF (CNTACT.EQ.332.OR.CNTACT.EQ.331) THEN
                          GO TO 800
                   ELSE
                          CO TO 900
                   END IF
           END IF
  --- SHOCK ON LEFT, HEADED LEFT, JUMPS NODE---
C
           IF (SHOCK.EQ.331) THEN
                   IF (CNTACT.EQ.322.OR.CNTACT.EQ.321) THEN
                          GO TO 700
                   ELSE IF (CNTACT.EQ.332.OR.CNTACT.EQ.331) THEN
                          GO TO 600
                   ELSE
                          GO TO 900
                   END IF
           END IF
C --- SHOCK ON RIGHT, HEADED RIGHT, NO NODE JUMPED---
```

```
IF (SHOCK.EQ.222) THEN
                  IF (CNTACT.EQ.222) THEN
                          GO TO 200
                  ELSE IF (CNTACT.EQ.232.OR.CNTACT.EQ.231) THEN
                         GO TO 800
                  ELSE IF (CNTACT.EQ.321.OR.CNTACT.EQ.322) THEN
                          GO TO 400
                  ELSE IF (CNTACT.EQ.332.OR.CNTACT.EQ.331) THEN
                          GO TO 800
                  ELSE
                          GO TO 900
                  END IF
          END IF
C --- SHOCK ON RIGHT, HEADED LEFT, NO NODE JUMPED---
          IF (SHOCK.EQ.232) THEN
                  IF (CNTACT.EQ.222) THEN
                          IF (SIGMA(1,2).LT.SIGMA(2,2)) THEN
                                 GO TO 700
                          ELSE
                                 GO TO 200
                          END IF
                  ELSE IF (CNTACT.EQ.231.OR.CNTACT.EQ.232) THEN
                          GO TO 600
                  ELSE IF (CNTACT.EQ.221) THEN
                          GO TO 700
                  ELSE IF (CNTACT.EQ.322) THEN
                          GO TO 400
                  ELSE IF (CNTACT.EQ.332.OR.CNTACT.EQ.331) THEN
                          GO TO 600
                  ELSE IF (SIGMA(1,2).LT.SIGMA(2,2)) THEN
                          GO TO 710
                  ELSE
                          GO TO 400
                  END IF
          END IF
  ---SHOCK ON RIGHT, HEADED RIGHT, JUMPS NODE---
          IF (SHOCK.EQ.221) THEN
                  IF (CNTACT.EQ.221.OR.CNTACT.EQ.222) THEN
                          GO TO 200
                  ELSE IF (CNTACT.EQ.231.OR.CNTACT.EQ.232) THEN
                          GO TO 300
                  ELSE IF (CNTACT.EQ.321.OR.CNTACT.EQ.322) THEN
                          GO TO 400
                  ELSE
                          GO TO 800
                  END IF
          END IF
  --- SHOCK ON RIGHT, HEADED LEFT, JUMPS NODE---
C
          IF (CNTACT.EQ.221.OR.CNTACT.EQ.222) THEN
                  GO TO 700
          ELSE IF (CNTACT.EQ.231.OR.CNTACT.EQ.232) THEN
                  GO TO 600
          ELSE IF (CNTACT.EQ.322) THEN
                  IF (SIGMA(1,2).LT.SIGMA(2,2)) THEN
                          GO TO 710
                  ELSE
                          GO TO 400
                  END IF
           ELSE IF (CNTACT.EQ.321) THEN
                  GO TO 710
           ELSE IF (DABS(Q(I)).LT.A(I)) THEN
                  GO TO 600
```

```
ELSE
                  GO TO 800
          END IF
C
C --- BRANCH HERE IF SHOCK IS TO LEFT OF CONTACT SURFACE----
C --- DETERMINE PROPER ALGORITHM TO USE FOR CALCULATING EXTENDED REIMAN--
  --- VARIABLE CHANGE ALONG CHARACTERISTICS AT THIS NODE----
          ELSE IF (SIGMA(1,1).LT.SIGMA(2,1)) THEN
C
  --- SHOCK ON LEFT, HEADED RIGHT, NO NODE CROSSED---
           IF (SHOCK.EQ.322) THEN
                  IFICNTACT.EQ.322.OR.CNTACT.EQ.321) THEN
                          GO TO 600
                  ELSE IF (CNTACT.EQ.332) THEN
                          IF (SIGMA(1,2).GT.SIGMA(2,2)) THEN
                                 GO TO 700
                          ELSE
                                 GO TO 300
                          END IF
                  ELSE IF (CNTACT.EQ.331) THEN
                          GO TO 700
                  ELSE IF (CNTACT.EQ.222.OR.CNTACT.EQ.221) THEN
                          GO TO 600
                  ELSE IF (CNTACT.EQ.232) THEN
                          GO TO 400
                  ELSE IF (SIGMA(1,2).GT.SIGMA(2,2)) THEN
                          GO TO 710
                  ELSE
                          GO TO 400
                  ENO IF
  --- SHOCK ON LEFT, HEADED LEFT, NO NODE CROSSED---
           IF (SHOCK.EQ.332) THEN
                  IF (CNTACT.EQ.322) THEN
                          GO TO 800
                  ELSE IF (CNTACT.EQ.332) THEN
                          GO TO 300
                  ELSE IF (CNTACT.EQ.321) THEN
                          GO TO 800
                  ELSE IF (CNTACT.EQ.222.QR.CNTACT.EQ.221) THEN
                          GO TO 800
                  ELSE IF (CNTACT.EQ.231.OR.CNTACT.EQ.232) THEN
                          GO TO 400
                  ELSE
                          GO TO 900
                  END IF
           END IF
  --- SHOCK ON LEFT, HEADED RIGHT, JUMPS NODE---
           IF (SHOCK.EQ.321) THEN
                  IF (CNTACT.EQ.322.OR.CNTACT.EQ.321) THEN
                          GO TO 600
                  ELSE IF (CNTACT.EQ.332.OR.CNTACT.EQ.331) THEN
                          GO TO 710
                  ELSE IF (CNTACT.EQ.222.OR, CNTACT.EQ.221) THEN
                          GO TO 600
                  ELSE IF (CNTACT.EQ.231) THEN
                          GO TO 710
                   ELSE IF (SIGMA(1,2).GT.SIGMA(2,2)) THEN
                          GO TO 710
                   ELSE
                          GO TO 400
                  END IF
           END IF
```

```
--- SHOCK ON LEFT, HEADED LEFT, JUMPS HODE---
          IF (SHOCK.EQ.331) THEN
                  IF (CNTACT.EQ.322.OR.CNTACT.EQ.321) THEN
                          GO TO 800
                  ELSE IF (CNTACT.EQ.331.OR.CNTACT.EQ.332) THEN
                          GO TO 300
                  ELSE IF (CNTACT.EQ.221.OR.CNTACT.EQ.222) THEN
                          90 TO 800
                  ELSE
                          90 TO 400
                  END IF
          END IF
 --- SHOCK ON RIGHT, HEADED RIGHT, NO NODE CROSSED---
          IF (SHOCK.EQ.222) THEN
                  IF (CNTACT.EQ.222.OR.CNTACT.EQ.221) THEN
                          60 TO +00
                  ELSE IF (CNTACT.EQ.231) THEN
                          GO TO 710
                  ELSE IF (CNTACT.EQ. 232) THEN
                          IF (SIGNA(1,2).GT.SIGNA(2,2)) THEN
                                  90 TO 700
                          ELSE
                                  00 TO 200
                          END IF
                  ELSE
                          90 TO 900
                  END IF
           END IF
C --- SHOCK ON RIGHT, HEADED LEFT, NO NODES CROSSED---
           IF (SHOCK . EQ. 232) THEN
                  IF (CNTACT.E9.222.OR.CNTACT.E9.221) THEN
                          00 TO 600
                  ELSE IF (CNTACT EQ. 232) THEN
                          IF (DABS(Q(I)).LT,A(I)) THEN
                                  GO TO 200
                          ELSE
                                  30 TO 500
                          END IF
                  ELSE
                          GO TO 900
                  END IF
           END IF
C
C --- SHOCK ON RIGHT, HEADED RIGHT, JUMPS HODE ---
           IF (SHOCK.EQ.221) THEN
                  IF (CNTACT, EQ. 221. OR, CNTACT, EQ. 222) THEN
                          GO TO +00
                   ELSE IF (CNTACT EQ. 231) THEN
                          90 TO 710
                   ELSE IF (CNTACT.EQ.232) THEN
                          GO TO 700
                   ELSE
                          90 TO 900
                  END IF
           END IF
C
  --- SHOCK ON RIGHT, HEADED LEFT, JUMPS NODE---
           IF "CNTAC" EQ 221.08.CNTAC" EQ.222 THEN
                  GO TO 800
           ELSE IF (CNTACT EQ.231.OR.CNTACT.EQ.232) THEN
                  90 TO 400
```

```
ELSE
                   90 TO 900
  --- SHOCK AND CONTACT SURFACE ARE AT THE SAME LOCATION AFTER TIME---
  ---ZERO---
           ELSE IF ((SHOCK.EQ.222).AND.(CNTACT.EQ.222))THEN
                   SHOCK = 321
                   CHTACT = 321
                   GO TO 400
           ELSE IFI(SHOCK.EQ.322).AND.(CNTACT.EQ.322))THEN
                   IFIDABSIGITILLT. ALTIT THEN
                           GO TO 300
                   ELSE
                           GO TO 500
                   END IF
           ELSE IF ((SHOCK.EQ.332).AND.(CNTACT.EQ.332)) THEN
                   SHOCK = 231
                   CNTACT = 231
                   GO TO 400
           ELSE IFI (SHOCK . EQ. 232) . AND . (CNTACT . EQ. 232)) THEN
                   IFIDABSIQ(I)).LT.A(I)) THEN
                           GO TO 200
                   ELSE
                           GO TO 500
                   END IF
           ELSE
                   GO TO 720
           END IF
C --- CALL CONDITION SUBROUTINE MHICH CONTAINS ALGORITHM THAT IS---
  --- MUMERICALLY BEST SUITED FOR THE SITUATION AT NOOE I---
   100 CALL COMO1(Q(I),Q(I+1),A(I),A(I+1),RR(I),QQ(I),S(I),DELQQL,
                     DELRRH, DELSH, DELSL, DELQH, DELAH, DELQL, DELAL, H, EE,
                     DELT, QQINT, RRINT, SINT, QPRIM, APRIM, AINT, Q(I-1), A(I-1))
         60 TO 1000
C
   200 CALL COND2(Q(I),Q(I-1),A(I),A(I-1),RR(I),QQ(I),S(I),DELQQL,
                     DELRRL DELSE DELGE DELAL DELT , H, EE , GGINT , RRINT , SINT ,
                     SPRIM.APRIM.AINT I
         90 TO 1000
C
   300 CALL COND3(G(I),G(I+1),A(I),A(I+1),RR(I),GG(I),S(I),DELGGH.
                     DELRRH, DELSH, DELQH, DELAH, DELT, H, EE, QQINT, RRINT, SINT,
                     QPRIM, APRIM, AINT 1
         60 TO 1000
   400 CALL COND4/I.SHOCK.CNTACT.J.LNDDE.RNDDE.QQSTEP.RRSTEP.SSTEP:
         90 TO 1100
   500 CALL CONDS(Q(I),Q(I-1),Q(I+1),A(I),A(I-1),A(I+1),RR(I),QQ(I),
                     SITI . DEL GOL . DEL GOM . DEL RRL . DEL RRH . DEL SL . DEL SH . DEL GL ,
        c
                     DELGH, DELAL, DELAH, H, EE, DELT, QQINT, RRINT, SINT, AIMT,
                     GPRIM, APRIM, SHOCK, CHTACT I
          90 TO 1000
   600 CALL CONDA! SHOCK, CHTACT, HALT)
         995TEP=0 00
         RRSTEP=0 DO
         SSTEP+0 DO
         90 TO 1100
    TOO SALE SONO?! SHOCK CONTACT DELT, SIGMA . IZ . I . H . HALT . Q ( I . )
         9651EP=1 00
         RRSTEP=0 DO
         SSTEP-0 DO
         90 10 1100
```

```
710 CALL COND 7N(SHOCK, CNTACT, DELT, SIGMA, IZ, I, H, HALT, Q(I), X)
         QQSTEP=0.DO
        RRSTEP=0.DO
          SSTEP=0.DO
        90 TO 1100
   720 CALL COND7S(SIGMA, HALT, SHOCK, CNTACT)
         QQSTEP=0.DO
         RRSTEP=0.DO
          SSTEP=0.DO
         60 TO 1100
   800 CALL CONDS(SHOCK, CNTACT, HALT)
         OGSTEP=0.DO
         RRSTEP=0.00
          SSTEP=0.DO
         60 TO 1100
   900 PRINT # ,'AN IMPOSSIBLE SITUATION EXISTS - ERROR'
         QQSTEP=0.DO
         RRSTEP=0.00
          SSTEP=0.00
         HALT = 1
         COTO 1100
C
C
      ----- CALCULATE DLTA QQ, DLTA RR & DLTA S
 1000
        DLTAQQ=QQINT-QQ(I)
            OLTARR=RRINT-RR(I)
           DLTAS=SINT-S(I)
¢
C
        ----- CALCULATE Z(K)'S -----
C
¢
            AAVG(1)=(AINT(1)+A(1))/2.0000
            AAVG(3)=(AINT(3)+A(I))/2.0000
            AAVG1 2 1=0.0000
            SAVG = (SINT+S(I))/2.000
            Z(1)=-(1.0000/G2)#AAVG(1)#(SAVG-G2)#(QPRIM(1)-G2#APRIM(1))
            Z(3)=(1.0000/G2)#AAVG(3)#(SAVG-G2)#(QPRIM(3)+G2#APRIM(3))
            Z(2)=0.0000
        ---- INTEGRATE THE Z(K)'S -----
C
            INTEG( 2 1=0.0000
            INTEG(1)=Z(1)#DELT
            INTEG(3)=Z(3)*DELT
¢
        ----- SOLVE THE EQUATION -----
C
¢
            QQSTEP=DLTAQQ+INTEG(1)
            RRSTEP=DLTARR+INTEG(3)
            SSTEP=DLTAS+INTEG(2)
C
        ----- STORE THE SOLUTION -----
C
Ç
 1100
        NEMQQ(I)=QQ(I)+QQSTEP
            NEWRR(I)=RR(I)+RRSTEP
            NEHS(I)=S(I)+SSTEP
C
        ----- GO TO NEXT NOOE -----
C
            I=I+1
         GOTO 11
 1200 CONTINUE
         BORY = 2
         IF(IZ(1).EQ.N) THEN
```

SK = 1

```
ELSE IF(SIGMA(1,2).EQ.3.DOO) THEN
              SK = 0
        END IF
        CALL SONDRY(Q(N),Q(N-1),QRSO,A(N),A(N-1),QQ(N),QQ(N-1),RR(N),
            RR(N-1),S(N),S(N-1),H,EE,DELT,RBNDRY,RBDPRS,RBDPR,RBDDR,
             RBOTR, J, NEWQQ(N), NEWR(N), NEWS(N), G, G1, G2, HALT, BORY, SK)
      ----- UPDATE THE VARIABLES -----
 1210 IF (I.EQ.N+1) GOTO 1220
           RR(I)=NEWRR(I)
           QQ(I)=NEHQQ(I)
           S(I)=NEWS(I)
        I=I+1
        GOTO 1210
 1220 CONTINUE
        RETURN
        END
        <del>刘昊就就就就是刘昊就是我们的,我们就是我们的,我们就是我们就是我们就是我们的,我们就是我们的,我们是是我们的,我们就是我们的,我们就是我们的人们的人们是是我们的人们</del>
C
C
                     CONDITION SUBROUTINES 1-8
C
C
        SUBROUTINE CONDICAL, GIPI, AI, AIPI, RR, QQ, S, DELQQL, DELRRH, DELSH,
                        DELSL, DELQH, DELAH, DELQL, DELAL, H, EE, DELT, QQINT,
                        RRINT, SINT, QPRIM, APRIM, AINT, QIM1, AIM1)
        C
                        SUBROUTINE CONDITION 1
C
C
        C
C ---- USED WHEN NO CONTACT SURFACES NOR SHOCKS MITHIN H OF NODE-----
 ---- AND FLOW IS SUBSONIC----
C ---- CALCULATES QQINT, RRINT, SINT, QPRIM, APRIM----
C ---- USES FORMARD AND BACKMARD DIFFERENCE SCHEMES----
C
C
      ----- VARIABLE DEFINITIONS . -----
C
C
     AI - A(I)
     AIM1 - ALI-1)
     AIP1 _ A(I+1)
C
           - ACTUAL ERROR IN CHARACTERISTIC SLOPE CALCULATION.
     E(K)
     LMO
            - SLOPE OF THE CHARACTERISTICS (Q+A,Q,Q-A)
     QI - Q(I)
     QIM1 - Q(I-1)
C
C
     QIP1 - Q(I+1)
C
        DIMENSION LMD(3),DELX(3),QINT(3),AINT(3),E(3),QPRIM(3),APRIM(3)
        INTEGER K
        DOUBLE PRECISION QI,QIP1,AI,AIP1.RR.QQ,S,AIM1,QIM1,
                        DELQQL, DELRRH, DELSH, DELSL, DELQH, DELAH, DELQL,
       C
                        DELAL, H, EE, DELT, LMD, DELX, QINT, AINT, E,
                        QQINT, RRINT, SINT, QPRIM, APRIM
C
    ----INITIAL ESTIMATE OF CHARACTERISTIC SLOPES----
C
        LMD(1) = QIM1 + AIM1
        LMD(2) = QI
        LMD(3) = QIP1 - AIP1
     ----CALCULATE LINEARLY INTERPOLATED VALUES OF Q AND A----
```

```
10 K = 1
    20 IF (K.LT.4) THEN
                DELX(K) = DELT * LMD(K)
                IF (LMD(K).LT.0.0000) THEN
                       QINT(K) = QI - (DELX(K) + DELQH / H)
                       AINT(K) = AI - (DELX(K) * DELAH / H)
                ELSE
                       QINT(K) = QI - (DELX(K) * DELQL / H)
                       AINT(K) = AI - (DELX(K) * DELAL / H)
                END IF
                K = K + 1
                GO TO 20
        END IF
    ----CALCULATE ERROR BETHEEN ESTIMATED SLOPE AND NEW SLOPE----
¢
    ----FROM NEW INTERPOLATED VALUES----
         E(1) = DABS(LMO(1) - (QINT(1) + AINT(1)))
         E(2) = DABS(LMO(2) - (QINT(2)))
        E(3) = DABS(LMD(3) - (QINT(3) - AINT(3)))
         LMD(1) = QINT(1) + AINT(1)
         LMD(2) = QINT(2)
         LMD(3) = QINT(3) - AINT(3)
    ---- COMPARE ERROR TO ERROR TOLERANCE LEVEL, ITERATE TIL MET----
Ç
         IF ((E(1).GT.EE).OR.(E(2).GT.EE).OR.(E(3).GT.EE)) GO TO 10
    ---- CALCULATE LINEARLY INTERPOLATED VALUES OF REIMAN----
    ---- VARIABLES AND MODIFIED ENTROPY AT POINT A----
         991NT = 99 - (DELX(1) + (DEL99L / H))
         IF (LMD(2).LE.0.0000) THEN
                SINT = S - (DELX(2) * (DELSH / H))
                SINT = S - (DELX(2) + (DELSL / H))
         END IF
         RRINT = RR - (DELX(3) # (DELRRH / H))
C --- CALCULATE SPATIAL DERIVATIVES ---
         QPRIM(1) = (QI-QIM1)/H
         QPRIM(2) = 0.000
         QPRIM(3) = (QIP1-QI)/H
         APRIM(1) = (AI-AIM1)/H
         APRIM(2) . 0.000
         APRIM(3) = (AIP1-AI)/H
         RETURN
         END
C
         SUBROUTINE COND2(QI,QIM1,AI,AIM1,RR,QQ,S,DELQQL,DELRRL,DELSL,
                         DELGL.DELAL.DELT.H.EE, QQINT.RRINT.SINT, QPRIM,
                         APRIM, AINT I
C
             你你你你你你我们的我们的我们的我们的我们的我们的我们的我们的我们的我们的我们的我们的我们的
¢
¢
                         SUBROUTINE CONDITION 2
C
            ********
C --- BACKMARD DIFFERENCE ALGORITHM FOR CALCULATING ---
C --- RRINT, QQINT, SINT, APRIM, QPRIM, AINT ---
         DIMENSION LMD(3).DELX(3).QINT(3).AINT(3).E(3).QPRIM(3).APRIM(3)
         INTEGER K
         DOUBLE PRECISION QI,QIMI,AI,AIMI,RR,QQ.S,DELQQL,DELRRL,DELSL,
```

DELQL, DELAL, DELT, H, EE, AINT, QINT, LMD, DELX, E,

```
C
                        QQINT, RRINT, SINT, QPRIM, APRIM
C
C
      --- INITIAL ESTIMATE OF CHARACTERISTIC SLOPES----
C
        LMB(1) = QIM1 + AIM1
        TMD(S) = dI
        LMD(3) = QI - AI
C
      ----CALCULATE LINEARLY INTERPOLATED VALUES OF Q AND A-----
    10 K = 1
    20 IF (K.LT.4) THEN
                DELX(K) = DELT # LMO(K)
                QINT(K) = QI - (DELX(K) = DELQL / H)
                AINT(K) = AI - (DELX(K) * DELAL / H)
                K = K + 1
                60 TO 20
        END IF
    ----CALCULATE ERROR BETHEEN ESTIMATED SLOPE AND NEW SLOPE----
C
C
    ----FROM NEW INTERPOLATED VALUES----
c
        E(1) = DABS(LHD(1) - (QINT(1) + AINT(1)))
        E(2) = DABS(LMD(2) - GINT(2))
        E(3) = DABS(LMO(3) - (QINT(3) - AINT(3)))
C
        LMD(1) = QINT(1) + AINT(1)
        LMD(2) = QINT(2)
         LMD(3) = QINT(3) - AINT(3)
C
    -----COMPARE ERROR TO ERROR TOLERANCE LEVEL, ITERATE TIL MET----
C
C
         IF ((E(1).GT.EE).OR.(E(2).GT.EE).OR.(E(3).GT.EE)) GO TO 10
    ----CALCULATE LINEARLY INTERPOLATED VALUES OF REIMAN----
    ---- VARIABLES AND MODIFIED ENTROPY AT POINT A----
c
         QQINT = QQ - (DELX(1) # (DELQQL / H))
        SINT = S - (DELX(2) + (DELSL / H))
         RRINT = RR - (DELX(3) * (DELRRL / H))
  --- CALCULATE SPATIAL DERIVATIVES ---
         QPRIM(1) = (QI-QIM1)/H
         QPRIM(2) = 0.000
         GPRIM(3) = (GI-GIM1)/H
         APRIM(1) = (AI-AIM1)/H
         APRIM(2) = 0.000
         APRIM(3) = (AI-AIM1)/H
         RETURN
         END
C
        SUBROUTINE COND3(QI,QIP1,AI,AIP1,RR,QQ,S,DELQQH,DELRRH,DELSH,
       C
                         DELQH.DELAH, DELT, H, EE, QQINT, RRINT, SINT, QPRIM,
                         APRIM, AINT I
C
             .......................
C
C
                         SUBROUTINE CONDITION 3
C
         C --- FORMARD DIFFERENCE ALGORITHM FOR CALCULATING ---
  --- RRINT, QQINT, SINT, APRIM, QPRIM, AINT ---
         DIMENSION .MD(3).DELX(3).QINT(3).AINT(3).E(3),QPRIM(3),APRIM(3)
         INTEGER K
         DOUBLE PRECISION QI,QIP1,AI,AIP1,RR,QQ,S,
                         DELQGH, DELRRH, DELSH, DELQH, DELAH,
```

Control of the Contro

```
C
                        DELT.H.EE,AINT.GINT.LMD.DELX.E,
                        QQINT, RRINT, SINT, QPRIM, APRIM
    ----INITIAL ESTIMATE OF CHARACTERISTIC SLOPES----
        LHD(1) = QI + AI
        LMD(2) = QI
        LMD(3) = QIP1 - AIP1
   ---- CALCULATE LINEARLY INTERPOLATED VALUES OF Q AND A----
    10 K = 1
    20 IF (K.LT.4) THEN
              DELX(K) = DELT + LMD(K)
              QINT(K) = QI - (DELX(K) + DELQH / H)
              AINT(K) = AI - (DELX(K) # DELAH / H)
              K = K + 1
              60 TO 20
        END IF
    ---- CALCULATE ERROR BETHEEN ESTIMATED SLOPE AND NEW SLOPE----
¢
C
    ----FROM NEW INTERPOLATED VALUES----
C
        E(1) = DABS(LMD(1) - (QINT(1) + AINT(1)))
        E(2) = DABS(LMO(2) - QINT(2))
        E(3) = DABS(LMO(3) - (QINT(3) - AINT(3)))
        LHO(1) = QINT(1) + AINT(1)
        LMD(2) = QINT(2)
        LMD(3) = QINT(3) - AINT(3)
    -----COMPARE ERROR TO ERROR TOLERANCE LEVEL, ITERATE TIL MET----
C
        IF((E(1).GT.EE).OR.(E(2).GT.EE).OR.(E(3).GT.EE)) GO TO 10
C
    ---- CALCULATE LINEARLY INTERPOLATED VALUES OF REIMAN----
C
    ---- VARIABLES AND MODIFIED ENTROPY AT POINT A----
        QQINT = QQ - (DELX(1) # DELQQH / H)
        SINT = S - (DELX(2) = DELSH / H)
        RRINT = RR - (DELX(3) * DELRRH / H)
C
C --- CALCULATE SPATIAL DERIVATIVES ---
        QPRIM(1) = (QIP1-QI I/H
        GPRIM(2) = 0.000
        QPRIM(3) = (QIP1-QI)/M
        APRIM(1) = (AIP1-AI)/H
         APRIM(2) = 0.000
         APRIM(3) = (AIP1-AI)/M
         RETURN
        END
C
        SUBROUTINE COND411, SHOCK, CNTACT, J, LNODE, RNODE, 99STEP, RRSTEP,
C
C
         *********************************
C
¢
                         SUBROLITINE CONDITION 4
         C --- A SITUATION EXISTS AT NODE I THAT MILL BE CORRECTED IN ---
C --- SUBROUTINE CORRCT. PHODE ARRAYS ARE GIVEN INFORMATION ---
C --- ON NODE LOCATION AND SHOCK/CONTACT SURFACE PICTURE ----
C
      ----- VARIABLE DEFINITIONS -----
C
      CDATRK - DENOTES HOW MANY MODES NEED TO BE CORRECTED
```

```
THIS TIME STEP
         DIMENSION LNOOE(4), RNOOE(4)
         INTEGER LNODE, RNODE, I, SHOCK, CNTACT, J, CD4TRK
         DOUBLE PRECISION QUSTEP, RRSTEP, SSTEP
C -----ASSIGN FIRST NODE ENCOUNTERED DURING THE NEW TIME STEP TO ----
  ----LNOOE ----
         IF(LNODE(4).LT.J) THEN
             CD4TRK = 1
         END IF
         IF(CD4TRK.EQ.1) THEN
                 LNODE(1) = I
                 LNODE(2) . SHOCK
                 LNODE(3) = CNTACT
                 LNODE(4) = J
C ----IF A SECOND NODE MITH CONDITION 4 IS ENCOUNTERED IN THE -----
C ---- SHEEP, THIS NODE IS ASSIGNED TO RNODE ----
C
         ELSE
                 RNODE(1) = I
                 RNODE(2) = SHOCK
                 RNODE(3) = CNTACT
                 RNODE(4) = J
C -----LNODE AND RNODE MILL BE "JUMPED" OVER DURING SHEEP THUS-----
C ----THEIR WHSTEP VALUES ARE SET TO 0----
         QQSTEP = 0.000
         RRSTEP . 0.DOO
           SSTEP = 0.DOO
         IF(CD4TRK.EQ.1) THEN
                 CD4TRK = CD4TRK + 1
         ELSE
                 CD4TRK = 1
         END IF
         RETURN
         END
         SUBROUTINE CONDSIGI, QIM1, QIP1, AI, AIM1, AIP1, RR, QQ, S, DELQQL,
        C
                          DELQQH, DELRRL, DELRRH, DELSL, DELSH, DELQL, DELQH,
                          DELAL, DELAH, H. EE, DELT, QQINT, RRINT, SINT, AINT,
                          QPRIH, APRIM, SHOCK, CNTACT )
        C
C
         <del>**********************************</del>
C
C
                           SUBROUTINE CONDITION 5
C
C
          **************************
C
  --- FOR SUPERSONIC FLOW WITH A DISCONTINUITY ON ONE SIDE OF THE NODE-
C
  --- CALCULATES QQINT, RRINT, SINT, APRIM, QPRIM, AINT ---
         DIMENSION LMD(3), DELX(3), QINT(3), AINT(3), E(3), QPRIM(3), APRIM(3)
          INTEGER K, SHOCK, CNTACT
          DOUBLE PRECISION QI,AI,RR,QQ,S,QIM1,QIP1,AIM1,AIP1,
                          EE, DELT, LMD, DELX, QINT, AINT, E, DELQL, DELQH, DELAL,
                          QQINT.SINT, RRINT, QPRIM, APRIM, DELAH, H,
                          DELQQL, DELQQH, DELRRL, DELRRH, DELSL, DELSH
C
  --- DISCONTINUITY ON LEFT, HEADED RIGHT, NOT CROSSING NODE ---
C
          IFIISHOCK.EQ.3221.OR.ICNTACT.EQ.32211 THEN
C
    ----INITIAL ESTIMATE OF CHARACTERISTIC SLOPES----
```

```
LMD(1) = QI + AI
         LMD(2) = QI
         LMO(3) = QIP1 - AIP1
C
    ---- CALCULATE LINEARLY INTERPOLATED VALUES OF Q AND A----
    10 K = 1
    20 IF (K.LT.4) THEN
               DELX(K) = DELT * LMD(K)
               QINT(K) = QI - (DELX(K) * DELQH / H)
               AINT(K) = AI - (DELX(K) * DELAH / H)
               K = K + 1
               GO TO 20
         END IF
C
    ---- CALCULATE ERROR BETWEEN ESTIMATED SLOPE AND NEW SLOPE----
C
    ----FROM NEW INTERPOLATED VALUES----
         E(1) = DABS(LMD(1) - (QINT(1) + AINT(1)))
         E(2) = DABS(LMD(2) - QINT(2))
         E(3) = DABS(LMD(3) - (QINT(3) - AINT(3)))
C
         LMD(1) = QINT(1) + AINT(1)
         LMD(2) = QINT(2)
         LMD(3) = QINT(3) - AINT(3)
C
    -----COMPARE ERROR TO ERROR TOLERANCE LEVEL, ITERATE TO MEET----
C
         IF((E(1).GT.EE).OR.(E(2).GT.EE).OR.(E(3).GT.EE)) GO TO 10
C
C
    ----CALCULATE LINEARLY INTERPOLATED VALUES OF REIMAN----
C
    ----VARIABLES AND MODIFIED ENTROPY AT POINT A----
         QQINT = QQ - (DELX(1) * DELQQH / H)
         SINT = S - (DELX(2) * DELSH / H)
         RRINT = RR - (DELX(3) + DELRRH / H)
C
C --- CALCULATE SPATIAL DERIVATIVES ---
         QPRIM(1) = (QIP1-QI)/H
         GPRIM(2) = 0.000
         QPRIM(3) = (QIPI-QI)/H
         APRIM(1) = (AIP1-AI)/H
         APRIM(2) = 0.000
         APRIM(3) = (AIP1-AI)/H
         END IF
C --- DISCONTINUITY ON RIGHT, HEADED LEFT, NOT CROSSING NODE ---
C
         IF((SHOCK.EQ.232).OR.(CNTACT.EQ.232)) THEN
C
    ----INITIAL ESTIMATE OF CHARACTERISTIC SLOPES----
C
         LMD(1) = QIM1 + AIM1
         LMD(2) = QI
         LMD(3) = QI - AI
C
    ----CALCULATE LINEARLY INTERPOLATED VALUES OF Q AND A----
    30 K = 1
    40 IF (K.LT.4) THEN
                 DELX(K) = DELT + LMD(K)
                 GINT(K) = GI - (DELX(K) # DELGL / H)
                 AINT(K) = AI - (DELX(K) # DELAL / H)
                 K = K + 1
                 GO TO 40
         END IF
    ----CALCULATE ERROR BETHEEN ESTIMATED SLOPE AND NEW SLOPE----
```

```
----FROM NEW INTERPOLATED VALUES----
        E(1) = DABS(LMD(1) - (QINT(1) + AINT(1)))
        E(2) = DABS(LMD(2) - QINT(2))
        E(3) = DABS(LMD(3) - (QINT(3) - AINT(3)))
C
        LMD(1) = QINT(1) + AINT(1)
        LMD(2) = QINT(2)
        LMD(3) = QINT(3) - AINT(3)
   ----COMPARE ERROR TO ERROR TOLERANCE LEVEL, ITERATE TO MEET----
C
        IF {{E(1).GT.EE).OR.(E(2).GT.EE).OR.(E(3).GT.EE)} GO TO 30
   ----CALCULATE LINEARLY INTERPOLATED VALUES OF REIMAN----
    ----VARIABLES AND MODIFIED ENTROPY AT POINT A----
C
        QQINT = QQ - (DELX(1) * (DELQQL / H))
        SINT = S - (DELX(2) * (DELSL / H))
        RRINT = RR - (DELX(3) * (DELRRL / H))
 --- CALCULATE SPATIAL DERIVATIVES ---
        QPRIM(1) = (QI-QIM1)/H
        QPRIM(2) = 0.000
        QPRIM(3) = (QI-QIM1)/H
        APRIM(1) = (AI-AIM1)/H
        APRIM(2) = 0.000
        APRIM(3) = (AI-AIM1)/H
        END IF
        RETURN
        END
C
        SUBROUTINE COND6(SHOCK, CNTACT, HALT)
C
        휈췙퉑눑궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦궦
                        SUBROUTINE CONDITION 6
C
        INTEGER SHOCK CONTACT HALT
        PRINT # , 'THE SITUATION FOR CONDITION 6 HITH THE CONTACT SURFACE '
        PRINT # ,'TO THE RIGHT OF A SHOCK BOTH HEADED RIGHT OR THE
        PRINT # , CONTACT SURFACE TO THE LEFT OF A SHOCK BOTH HEADED LEFT'
        PRINT # ,'ADDITIONAL LOGIC IS REQUIRED TO PROCEED'
        PRINT * , 'SHOCK =', SHOCK,' CONTACT SURFACE ='.CNTACT
        HALT = 1
        RETURN
        ENO
¢
        SUBROUTINE COND7(SHOCK, CNTACT, DELT, SIGMA, 12, 1, H, HALT, 0)
C
        **************
C
                        SUBROUTINE CONDITION 7
C
C
        C
C
        DIMENSION SIGNA(4,2),12(4)
        INTEGER HALT, SHOCK, CNTACT, 12, I
        DOUBLE PRECISION DELT, SIGMA, H, Q
        PRINT # , 'CONDITION 7 REQUIRES THAT THE CONTACT SURFACE AND
        PRINT # , 'SHOCK(HOVING IN OPPOSITE DIRECTIONS) HEET AND CROSS.
        PRINT # , 'MMEN THEY INTERSECT, THE RESULT IS A FUNCTION OF EXIST-'
```

```
PRINT * ,'ING CONDITIONS AROUND THEM. BOTH THE ORIGINAL SHOCK
        PRINT # 5'AND CONTACT SURFACE WILL EXPERIENCE VELOCITY CHANGES .'
        PRINT # , THIS SUBROUTINE HOULD HAVE TO CALCULATE WHEN AND WHERE'
        PRINT * , 'MITHIN THE TIME/SPACE ITERVAL THE SHOCK AND CONTACT
        PRINT * , SURFACE INTERSECT. THIS IS BASED ON KNOWN SPEED AND
        PRINT * , THEIR RESPECTIVE LOCATIONS. THIS NEW TIME, DELT(NEW) '
        PRINT * , 'THEN COULD BE USED TO RERUN "SHEEP", MITH CONDITION 75'
        PRINT # , 'EXISTING AT TIME = T + DELT(NEW). ADDITIONAL LOGIC IS'
        PRINT * , 'REQUIRED TO CONTINUE.'
        PRINT * ,'SHOCK =',SHOCK,' CONTACT SURFACE =',CNTACT
        PRINT * ,'SIGMA(1,1) =',SIGMA(1,1),' SIGMA(1,2) =',SIGMA(1,2)
        PRINT * ,'SIGMA(2,1) =',SIGMA(2,1),' SIGMA(2,2) =',SIGMA(2,2)
        PRINT * , 'CONTACT SURFACE VELOCITY =',Q
        PRINT * , 'NODE I *', I
        HALT # 1
        RETURN
        END
C
        SUBROUTINE CONDITHING SHOCK, CHTACT, DELT, SIGMA, 12, 1, H, HALT, Q, X1
        C
C
                         SUBROUTINE CONDITION 7N
C
        *******************
C
        DIMENSION SIGNA(4,2),12(4)
        INTEGER HALT, SHOCK, CNTACT, 12, I
        DOUBLE PRECISION DELT, SIGMA, H, Q, X
¢
        PRINT # , CONDITION 7N REQUIRES THAT WHEN EITHER A SHOCK OR
        PRINT # , 'CONTACT SURFACE JUMPS A NODE (AS DETERMINED BY
        PRINT . COMPARING SIGNA(L,1) TO SIGNA(L,2)) A CONTACT SURFACE
         PRINT # , 'OR SHOCK HOULD BE MET AND CROSSED DURING THE JUMP.
         PRINT . THE RESULT WHEN THEY INTERSECT IS A FUNCTION OF
         PRINT # , EXISTING CONDITIONS AROUND THEM. BOTH THE ORIGINAL
         PRINT # , SHOCK AND THE CONTACT SURFACE HILL EXPERIENCE VELOCITY
        PRINT . CHANGES. THIS SUBROUTINE HOULD HAVE TO CALCULATE WHEN'
        PRINT # , HITHIN THE TIME INTERVAL AND MHERE SPACIALLY THE
        PRINT . 'INTERSECTION OCCURS. THIS IS BASED ON KNOWN SPEED AND'
         PRINT . THE RESPECTIVE LOCATIONS OF THE SHOCK AND CONTACT
         PRINT # , SURFACE. THE NEW TIME, DELT(NEW), COULD THEN BE USED
         PRINT # , TO RERUN "SHEEP" WITH CONDITION 4 AT THIS NODE, AND
         PRINT # , 'SIGMA(2,2) = SIGMA(1,2) SO THAT CONDITION 75 HOULD
         PRINT . RESULT IN THE NEXT TIME INTERVAL.
         PRINT * , SHOCK = ', SHOCK, 'CONTACT SURFACE = ', CNTACT
        PRINT # ,'SIGMA(1,1) =',SIGMA(1,1),' SIGMA(1,2) =',SIGMA(1,2)
PRINT # ,'SIGMA(2,1) =',SIGMA(2,1),' SIGMA(2,2) =',SIGMA(2,2)
         PRINT # , 'CONTACT SURFACE VELOCITY :',Q
         PRINT # , 'NODE I #', I, ' LOCATION AT X #', X
         HALT = 1
         RETURN
         END
C
         SUBROUTINE COND7S(SIGMA, HALT, SHOCK, CHTACT)
¢
         C
C
                         SUBROLITINE CONDITION 75
C
C
         *************************************
C
         DIMENSION SIGNA(4,2)
         INTEGER SHOCK CHTACT HALT
         DOUBLE PRECISION SIGMA
C
         PRINT . CONDITION 75 HAS BEEN HET. THIS MEANS THAT THE SHOCK
         PRINT . 'AND CONTACT SURFACE ARE LOCATED AT THE SAME X AT A
```

```
PRINT # , 'TIME OTHER THAN ZERO. THIS SUBROUTINE MOULD HAVE TO '
        PRINT # , DETERMINE THE RESULT OF THE INTERSECTION BASED ON THE '
        PRINT # , CONDITIONS TO THE LEFT AND RIGHT. ADDITIONAL LOGIC IS
        PRINT # ,'REQUIRED TO PROCEED.'
        PRINT # , 'SHOCK =', SHOCK,' CONTACT SURFACE =', CNTACT
        PRINT * , 'SIGMA(1,1) =',SIGMA(1,1),' SIGMA(2,1) =',SIGMA(2,1)
        HALT - 1
        RETURN
        END
C
        SUBROUTINE COND&(SHOCK, CHTACT, HALT)
C
        C
                         SUBROUTINE CONDITION 8
C
C
        ******************************
        INTEGER HALT, SHOCK, CHTACT
        PRINT # , CONDITION & COULD RESULT ONLY AFTER THE ORIGINAL SHOCK
        PRINT + , 'HAS CROSSED THE CONTACT SURFACE, AND THE SUBSEQUENT
        PRINT . CONDITIONS DETERMINED. ADDITIONAL LOGIC IS REQUIRED TO
        PRINT + , 'CONTINUE.'
        PRINT # , 'SHOCK =', SHOCK,' CONTACT SURFACE =', CNTACT
        HALT = 1
        RETURN
        END
C
        SUBROUTINE CORRCT! LNDDE ,RNDDE ,N.SIGMA,H,GQ,RR,S.G.GI,GZ.IZ.XZ.H.
                         AR.DQ.VS.A.QI
C
C
        ¢
                   DISCONTINUITY CORRECTION SUBROUTINE
C
c
      ----- VARIABLE DEFINITIONS -----
C
     ENTRPY - MODIFIED ENTROPY
     SNOSPO - SONIC VELOCITY
      JA - MELOCITY RELATIVE TO THE SHOCK, LEFT SIDE
      UB - VELOCITY RELATIVE TO THE SHOCK, RIGHT SIDE
      /LCTY - VELOCITY
        INTEGER LNDGE . RHOSE . N. 12 . HOSE . SHOCK . CHTACT . K
        DIMENSION LNODE:41.RNODE:41.SIGNA:4.21.QQ:N1.RR:N1.S:N3.IZ:43.
                 WZ141.AIN1.QIN1.XA141.WE4
        DOUBLE PRECISION SIGMA. 39 . RR. 3 . A . J.
                        H.G.G1.G2.K2.M.AR.OQ./S.
       C
                        RRA . RRB . 994 . 998 . AA . AB . QA . GB . SA . SB .
       C
                        SALISAZIVECTY ISMOSPO LENTRPY IQQUALCIRRUALCI
                         MS.XA
C
  ---- DEFINE STATEMENT FUNCTIONS----
         SOCALCIVECTY SNOSPO ENTRPY . . VECTY . INDSPONENTRPY
        RRCALC: VLCT+ .SHOSPO .ENTRPY : + VLCT+ - SHOSPO+ENTRP+
C
  -----SET INITIAL VALUES OF VARIABLES TO ZERO-
        BRA . 0 000
         PRB . 7 D00
         204 . 1 300
         108 ·
          AA + 3 000
          AB . 0 DOO
```

BA . 0 DOO

```
■ 0.D00
          SA = 0.000
          SB = 0.000
          DO 15 K=1,4
                  XA1K )=0.00
                  XB(K)=0.00
    15 CONTINUE
   -----DETERMINE IF ONLY ONE NOOE NEEDS TO BE CORRECTED OR THO----
C
   -----NODES. ALSO, IF SHOCK AND CONTACT SURFACES ARE CLOSE----
C
   ----ENOUGH(HITH IN 2H) TO INTERACT----
         IF((!NODE(2).EQ.100).OR.(LNODE(3).EQ.100)) THEN
                IF((LNOOE(1).GE.(RNODE(1)-2)).AND.(RNODE(1).GT.0)) THEN
                        GO TO 20
                ELSE
                        GO TO 30
                 ENO IF
         ELSE IF(RNODE(1).GT.0) THEN
                 GO TO 20
         ELSE
                 GO TO 10
         END IF
C
C -----BRANCH HERE IF ONLY ONE NODE TO BE CORRECTED (LNODE) AND,-----
C ----SHOCK/CONTACT SURFACE INTERACTION----
    10 SHOCK = LNODE(2)
         CHTACT = LNODE(3)
C
C ---SHOCK ON LEFT, HEADED RIGHT, JUMPS OR NOTICONTACT SURFACE ON-----
C --- RIGHT, HEADED LEFT, DOESN'T CROSS NODE ---
         IFI(SHOCK.EQ.322.OR.SHOCK.EQ.321).AND.(CNTACT.EQ.232)) THEN
  -----DETERMINE NODE TO RIGHT OF SHOCK AND CONTACT SURFACE----
C
C
                 I2(1) = LNODE(1) + 1
                 12(2) = LNODE(1) + 1
                 CALL DELTAXIIZ,SIGMA,XB,XA,H)
  ----EXTRAPOLATE TO RIGHT FACE OF CONTACT SURFACE----
                 IF (12(2), EQ.N) THEN
                        CALL BBDRY(RRINI,QQ(N),S(N),RRB,QQB,SB,AB,QB)
                 ELSE
                 CALL EXTRAP(RR(12(2)), RR(12(2)+1), QQ(12(2)), QQ(12(2)+1),
        C
                          S(I2(2)),S(I2(2)+1),XB(2),H,RRB,QQB,S8,AB,QB)
                 FNO IF
  -----CALCULATE /ARIABLE CHANGE ACROSS CONTACT SURFACE----
                 SA = S(12(2)-1)
                 CALL CSJUMP(AB.QB.SB.SA,G2,QA,AA)
  ----IF SHOCK INTERACTS CALCULATE CHANGE IN VARIABLES ACROSS SHOCK----
                 IFISHOCK . EQ. 321) THEN
                        QB = QA
                         AR = AA
                         SB . SA
                        CALL SKUUMP! AB, QB, SB, AR, DQ, VS, G, G1, A, AA, QA, SA I
                        QQA = QQCALCIQA,AA,SA1
                        RRA = RRCALC(QA,AA,SA)
   ----- INTERPOLATE TO MODE(IZ!1)-1: AND ASSIGN CORRECTED VALUES----
                        IF (12(1).EQ.2) THEN
                                CALL BBDRY(RRA,QQA,SA,RR(I2(1)-1),QQ(I2(1)-1),
```

```
C
                                  S(I2(1)-1),A(I2(1)-1),Q(I2(1)-1))
                        ELSE
                        CALL INTERP(RRA, RR(12(1)-2), QQA, QQ(12(1)-2), SA,
                               S(12(1)-2),XA(1),(XA(1)+H),RR(12(1)-1),
                               QQ(I2(1)-1),S(I2(1)-1),A(I2(1)-1),
                               Q(12(1)-1))
                        END IF
                ELSE
                        QQ(12(2)-1) = QQCALC(QA,AA,SA)
                        RR(12(2)-1) = RRCALC(QA,AA,SA)
                         S(12(2)-1) = SA
                          A(12(2)-1) = AA
                          Q(12(2)-1) = QA
                 END IF
C ---SHOCK ON RIGHT, HEADED LEFT, CROSSES NODE OR NOT; CONTACT SURFACE-
  --- ON LEFT, HEADED RIGHT, DOES'NT CROSS NODE---
C
C
         ELSE IF((SHOCK.EQ.232.OR.SHOCK.EQ.231).AND.(CNTACT.EQ.322)) THEN
C
C
  ----DETERMINE NODE TO RIGHT TO SHOCK AND CONTACT SURFACE----
C
                I2(1) = LNODE(1)
                 I2(2) = LNODE(1)
                CALL DELTAX(12,SIGMA,XB,XA,H)
  ----EXTRAPOLATE TO LEFT FACE OF CONTACT SURFACE----
C
                 IF (12(2).EQ.2) THEN
                        CALL BBDRY(RR(1),QQ(1),S(1),RRA,QQA,SA,AA,QA)
                 CALL EXTRAP(RR(12(2)-1),RR(12(2)-2),QQ(12(2)-1),QQ(12(2)-2),
       C
                          S(12(2)-1),S(12(2)-2),XA(2),H,RRA,QQA,SA,AA,QA)
                 END IF
C ----CALCULATE VARIABLE CHANGE ACROSS CONTACT SURFACE----
                 SA = S(12(2))
                 CALL CSJUMP(AA,QA,SA,SB,G2,QB,AB)
C ----IF SHOCK INTERACTS CALCULATE CHANGE IN VARIABLES ACROSS SHOCK----
                 IF(SHOCK.EQ.231) THEN
                        QA = QB
                        AA = AB
                        SA = SB
                        CALL SKJUMP(AA,QA,SA,AR,DQ,VS,G,G1,H,AB,QB,SB)
                        QQB = QQCALC(QB,AB,SB)
                        RRB = RRCALC(QB,AB,SB)
C
   ----INTERPOLATE TO NODE(12(1)) AND ASSIGN CORRECTED VALUES----
                        IF (12(1).EQ.N) THEN
                              CALL BBDRY(RRB,QQB,SB,RR([2(1)],QQ([2(1)],S([2(1)],
       C
                                  A(12(1)),Q(12(1)))
                        CALL INTERP(RRB,RR(12(1)+1),QQB,QQ(12(1)+1),SB,
                               S(I2(1)+1), XB(1), (XB(1)+H), RR(I2(1)),
                               QQ([2(1)),S([2(1)),A([2(1)),Q([2(1)))
                        END IF
                 ELSE
                        QQ(12(2)) = QQCALC(QB,AB,SB)
                        RR(12(2)) = RRCALC(QB,AB,SB)
                          S(12(2)) = S8
                          A(12(2)) = AB
                          3(12(2)) = Q6
                 END IF
```

SMOCK ON RIGHT, MEADED RIGHT, DOESN'T CROSS OR ON LEFT, HEADED ---

```
C --- RIGHT, DOES CROSS; AND CONTACT ON LEFT, HEADED RIGHT, CROSSES---
C --- OR NOT: OR SHOCK ON RIGHT, HEADED LEFT, DOESN'T CROSS NODE ---
C --- MITH CONTACT ON LEFT, NEADED RIGHT, AND CROSSED NOOE ---
           ELSE IFILISHOCK.EG.222.GR.SHOCK.EG.3211.AND.(CNTACT.EG.321.GR.
       c
                  CNTACT.EQ.322)).OR.(SHOCK.EQ.232.AND.CNTACT.EQ.321))
  -----DETERMINE NODE TO RIGHT OF SHOCK AND CONTACT SURFACE----
                 12(1) = LNO0E(1) + 1
                 12(2) = LNODE(1' + 1
                 CALL DELTAXIIZ, SIGMA, XB, XA, HI
    ---EXTRAPOLATE TO RIGHT FACE OF SHOCK----
                 IF (12(1).EQ.N) THEN
                        CALL BBDRY(RR(N),QQ(N),S(N),RRB,QQB,SB,AB,QB)
                 CALL EXTRAP(RR(12(1)),RR(12(1)+1),QQ(12(1)),QQ(12(1)+1).
       C
                          $(12(1)),$(12(1)+1),XB(1),H,RRB,QQB,SB,AB,QB)
                 END IF
C
  ----CALCULATE CHANGE IN VARIABLES ACROSS SHOCK----
                 IF(SHOCK.EQ.232) THEN
                        AA = AB/AR
                        3A1 = (G1/G)*DLOG((2.D00*G*(H**2)-G+1.D00) / (G+1.D00))
                        SA2 = G1*DLOG(((G-1.D00)*(N**2)+2.D00) / ((G+1.D00)*
                                  (Mw#2111
                        SA = SB+SA1+SAZ
                        UB = Q8 - VS
                        UA = UB -AAHDQ
                        QA = UA + VS
                 ELSE
                        CALL SKJUMPIAB, QB, SB, AR, DQ, VS, G, G1, M, AA, QA, SA)
                 END IF
C
  ---- CALCULATE CHANGE IN VARIABLES ACROSS CONTACT SURFACE----
                 IF(CNTACT.EQ.322) THEN
                         QQ(I2(1)-1) = QQCALC(QA,AA,SA)
                         RR([2(1)-1) = RRCALC(QA.AA.SA)
                          S(12(1)-1) = SA
                          A(12(1)-1) = AA
                          Q(12(1)-1) = QA
                 ELSE
                         QB = QA
                         AB = AA
                        SB = SA
                        SA = S(12(2)-2)
                        CALL CSJUMP(AB,QB,SB,SA,G2,QA,AA)
                        QQA = QQCALC(QA,AA,SA)
                        RRA = RRCALC(QA,AA,SA)
  ----INTERPOLATE TO NODE(12(2)-1) AND ASSIGN CORRECTED VALUES----
                        IF (12(2).EQ.2) THEN
                                CALL BBDRY(RRA,QQA,SA,RR(I2(2)-1),QQ(I2(2)-1),
       C
                                  S(12(2)-1),A(12(2)-1),Q(12(2)-1))
                        CALL INTERPIRRA, RR(12(2)-2), QQA, QQ(12(2)-2), SA,
                               S(12(2)-2), XA(2), (XA(2)+H), RR(12(2)-1),
                               QQ(12(2)-1),S(12(2)-1),A(12(2)-1),
                               Q(12(2)-1))
                        ENO IF
                 END IF
  ---SHOCK ON LEFT, HEADED LEFT, DOESN'T CROSS NODE, OR ON RIGHT,---
```

```
C --- HEADED LEFT, CROSSED MODE; AND CONTACT ON RIGHT, MEADED LEFT,---
C --- CROSSES NODE OR NOT: OR SHOCK ON LEFT, HEADED RIGHT, DOESN'T---
C --- CROSS NOSE, AND CONTACT ON RIGHT, HEADED LEFT, CROSSED NODE---
                    ELSE IF(((SHOCK.E9.332.OR.SHOCK.E9.231).AND.(CNTACT.E9.232.OR.
                                          CNTACT.EQ.231)).OR.(SHOCK.EQ.322.AND.CNTACT.EQ.231))
     ----- DETERMINE MODE TO RIGHT OF SHOCK AND CONTACT SURFACE----
                                      12(1) = LNO0E(1)
                                      12(2) = LNODE(1)
                                      CALL DELTAXIIZ.SIGHA,XB.XA,HI
     ----EXTRAPOLATE TO LEFT FACE OF SHOCK----
                                      IF (12(1).EQ.2) THEN
                                                      CALL BBDRY(RR(1),QQ(1),S(1),RRA,QQA,SA,AA,QA)
                                      CALL EXTRAP(RR([21])-1), RR([21])-2), QQ([2(])-1), QQ([2(])-2),
                                                          S(12(1)-1), S(12(1)-2), XA(1), H, RRA, QQA, SA, AA, QA)
C ----CALCULATE CHANGE IN VARIABLES ACROSS SHOCK-----
                                      IF(SHOCK.EQ.322) THEN
                                                       AB = AA/AR
                                                       SA1 = (G1/G) = (G1/G) = (G+1.000) / (G+1
                                                       SAZ = G1#0L0G((1G-1.000)#(H##Z)+Z.000) / (1G+1.000)#
                 C
                                                                            114992111
                                                       S8 = SA+SA1+SA2
                                                       UA = QA - VS
                                                       UB = UA - A8#09
                                                       Q8 = U8 + VS
                                      ELSE
                                                       CALL SKJUMP(AA,QA,SA,AR,DQ,VS,G,G1,M,AB,QB,S8)
                                      FNO TE
C ---- CALCULATE CHANGE IN VARIABLES ACROSS CONTACT SURFACE----
                                      IFICHTACT . EQ. 2321 THEN
                                                       QQ(I2(1)) = QQCALC(QB,AB.SB)
                                                       RR(IZ(1)) = RRCALC(QB,AB,CB)
                                                          S(12(1)) = S8
                                                           A(12(1)) = AB
                                                          Q(12(1)) = Q8
                                      ELSE
                                                       9A - 98
                                                       AA = AB
                                                       SA . SB
                                                       S8 = S(12(2)+1)
                                                       CALL CSJUMPIAA, QA, SA, SB, GZ, QB, AB)
                                                       QQ8 = QQCALC(Q8,A8,S8)
                                                       RRB = RRCALCIGB, AB, SB )
 C ----INTERPOLATE TO NODE(12(2)) AND ASSIGN CORRECTED VALUES----
                                                       IF (12:2).EQ.N) THEN
                                                                     CALL BBDRY(RRB, QQB, SB, RR([2(2)), QQ([2(2)], S([2(2)),
                                                                             A(12(2)),Q(12(2)))
                  C
                                                       ELSE
                                                       CALL INTERP(RRB, RR(I2(2)+1), QQB, QQ(I2(2)+1), SB,
                  C
                                                                      S(12(2)+1), XB(2), (XB(2)+H), RR(12(2)),
                  C
                                                                      QQ(12(2)),S(12(2)),A(12(2)),Q(12(2)))
                                                       END IF
                                      ENO IF
                     END IF
                     GO TO 40
 C
```

```
C ----BRANCH HERE IF LNODE AND RNODE ARE CLOSE ENOUGH FOR SHOCK----
C ---- AND CONTACT SURFACE INTERACTION----
C LEFT NODE:
C --- SHOCK ON RIGHT, HEADED RIGHT, JUMPS NODE WITH CONTACT ON LEFT---
C --- NEADED RIGHT, JUMPS NOOE OR NOT; OR NO SHOCK HITH CONTACT ON ---
  --- LEFT, HEADED RIGHT, JUMPS NODE---
C RIGHT NODE:
C
  ---SHOCK ON LEFT, HEADED RIGHT, JUMPS NODE HITH NO CONTACT SURFACE---
    20 IF((!LNODE(2).EQ.221).AND.(LNODE(3).EQ.321.OR.LNODE(3).EQ.322))
       C .OR.(LNODE(2).EQ.100.AND.LNODE(3).EQ.321)) THEN
                 IF((RNODE(2),EQ.321),AND.(RNODE(3),EQ.100)) THEN
  ---- DETERMINE NODE TO RIGHT OF SHOCK AND CONTACT SURFACE----
С
                        12(1) = RNODE(1) + 1
                        IF(LNODE(2).EQ.322) THEN
                                12(2) = LNODE(1)
                                I2(2) = LNODE(1) + 1
                        END IF
                        CALL DELTAX(12,SIGMA,XB,XA,H)
  ----EXTRAPOLATE TO RIGHT FACE OF SHOCK----
                 IF (12(1).EQ.N) THEN
                        CALL BBDRY(RR(N), QQ(N), S(N), RRB, QQB, SB, AB, QB)
                 CALL EXTRAP(RR(12(1)), RR(12(1)+1), QQ(12(1)), QQ(12(1)+1),
                          S(12(1)),S(12(1)+1), X8(1), H, RRB, QQB, S8, AB, QB)
                 END IF
C
  ----CALCULATE VARIABLE CHANGE ACROSS SHOCK----
                 CALL SKJUMPIAB, QB, SB, AR, DQ, VS, G, G1, M, AA, QA, SA)
C
C
  ----DETERMINE CORRECTED VALUES AT NODE(12(1)-1) AND ASSIGN THEM----
                 IFILNODE(2).EQ.100) THEN
                         QQA . QQCALC(QA,AA,SA)
                         RRA = RRCALCIGA,AA,SAI
  ----INTERPOLATE TO NODE(12(1)-1) AND ASSIGN CORRECTED VALUES----
                         IF (12(1).EQ.2) THEN
                                CALL BBDRY(RRA, QQA, SA, RR([2(1)-1), QQ([2(1)-1],
       C
                                  S([2(1)-1],A([2(1)-1),Q([2(1)-1)]
                         ELSE
                         CALL INTERPIRRA, RRII2111-21, QQA, QQII2(1)-21, SA,
       C
                               S([2(1)-2), XA(1), (XA(1)+H), RR([2(1)-1),
                               QQ(12(1)-1),S(12(1)-1),A(12(1)-1),
       C
                               Q(12(1)-1))
                        END IF
  ----EXTRAPOLATE TO RIGHT FACE OF CONTACT SURFACE----
C
                         IF (1212).EQ.N) THEN
                                CALL BBORY(RR(N),QQ(N),S(N),RRB,QQB,SB,AB,QB)
                         CALL EXTRAP(RR(1212)), RR(12(2)+1), QQ(12(2)), QQ(12(2)+1),
        C
                              $(12(2)),$(12(2)+1),XB(2),H,RRB,QQB,$8,AB,QB(
                         END IF
                 ELSE
                         QQ(I2(1)-1) = QQCALC(QA,AA,SA)
                         RR(I2(1)-1) = RRCALC(QA,AA,SA)
                          S(12(1)-1) = SA
                          A(12(1)-1) = AA
                          Q(12(1)-1) = QA
```

```
IF(LNOOE(3).EQ.322) THEN
                                QQ(I2(2)) = QQ(I2(1)-1)
                                RR(12(2)) = RR(12(1)-1)
                                 S(12(2)) = S(12(1)-1)
                                 A(12(2)) = A(12(1)-1)
                                 Q(12(2)) = Q(12(1)-1)
                                 90 TO 40
                        ELSE
                                AA = AA
                                AB = AA
                                SB = SA
                        END IF
                 ENO IF
                        SA = S(12(2)-2)
                        CALL CSJUMP! AB. QB. SB. SA. GZ. QA. AA I
                        QQA = QQCALC(QA,AA,SA)
                        RRA = RRCALC(QA,AA,SA)
  ----INTERPOLATE TO NODE(IZ(2)-1) AND ASSIGN CORRECTED VALUES----
                        IF (12(2).EQ.2) THEN
                                CALL BBORY(RRA, QQA, SA, RR([2(2)-1), QQ([2(2)-1],
       C
                                  S(12(2)-1),A(12(2)-1),Q(12(2)-1))
                        ELSE
                        CALL INTERP(RRA, RR(12(2)-2), QQA, QQ(12(2)-2), SA,
       C
                               $(12(2)-2',XA(2),(XA(2)+H),RR(12(2)-1),
                               99(12(2)-1),S(12(2)-1),A(12(2)-1),
       C
                               Q(12(2)-1))
                        END IF
                 END IF
C LEFT NODE:
C ---SHOCK ON LEFT, HEADED RIGHT, JUMPS NODE WITH NO CONTACT---
C RIGHT NODE:
C --- NO SHOCK, MITH CONTACT ON RIGHT, HEADED LEFT, JUMPS NODE---
         ELSE IF ((LNODE(2).EQ.321).AND.(LNODE(3).EQ.100)) THEN
                 IF((RNODE(2).EQ.100).AND.(RNODE(3).EQ.231)) THEN
  ----DETERMINE NODE TO RIGHT OF SHOCK AND CONTACT SURFACE----
                        12(1) = LNODE(1) + 1
                        12(2) = RNODE(1)
                        CALL DELTAXIIZ, SIGHA, XB, XA, H)
  ----CALCULATE JUMP THROUGH CONTACT SURFACE THEN SHOCK----
                        IF(I2(1).EQ.(I2(2)-1)) THEN
                                AA = A(12(1))
                                QA = Q([2(]))
                                SA = S(12(1))
                                SB = $(12(2)+1)
                                CALL CSJUMP(AA,QA,SA,SB,G2,QB,AB)
                                QQB = QQCALC(QB,AB,SB)
                                RRB = RRCALC(QB,AB,SB)
C ----INTERPOLATE TO NODE(12(2)) AND ASSIGN CORRECTED VALUES----
                                IF (I212).EQ.N) THEN
                               CALL BBDRY(RRB,QQB,SB,RR(12(2)),QQ(12(2)),S(12(2)),
        C
                                  A(12(2)),Q(12(2)))
                                ELSE
                                CALL INTERP(RRB,RR(I2(2)+1),QQB,QQ(I2(2)+1),SB,
        C
                                   S(12(2)+1), XB(2), (XB(2)+H), RR(12(2)),
                                   QQ(12(2)),S(12(2)),A(12(2)),Q(12(2)))
                                END IF
                                AB = A(12(1))
                                98 = Q(I2(1))
                                SB = S(12(1))
```

```
CALL SKJAPPIAB, 08, 38, AR, DQ, V3, 8, 61, M, AA, QA, SA I
                                 QQA = QQCALC(QA,AA,SA)
RRA = RRCALC(QA,AA,SA)
  -----INTERPOLATE TO MODE(12(1)-1) AND ASSIGN CORRECTED VALUES-----
                                 IF (12(1).EQ.2) THEN
                                 CALL BBDRY(RRA, QQA, SA, RR(I2(1)-1), QQ(I2(1)-1),
        C
                                   $(12(1)-1).A(12(1)-1).@(12(1)-1))
                                 F1 95
                                 CALL INTERPIREA, RR(12(1)-2), QQA, QQ(12(1)-2), SA,
        c
                                    SITZ(1)-2), XA(1), (XA(1)+H), RR(TZ(1)-1),
        C
                                    QQ( 12( 1)-1).S( 12( 1)-1).A( 12( 1)-1).
                                    Q(12(1)-1))
                                 END IF
                         ELSE
                                 MR(12(1)-1) = RR(12(1)-2)
                                 QQ([2(1)-1] = QQ([2(1)-2]
                                   S(12(1)-1) = S(12(1)-2)
                                   A(12(1)-1) = A(12(1)-2)
                                   Q(12(1)-1) = Q(12(1)-2)
                                 RR(12(2)) = RR(12(2)+1)
                                 QQ(12(2)) . QQ(12(2)+1)
                                   S(12(2)) = S(12(2)+1)
                                   A(12(2)) = A(12(2)+1)
                                   Q(12(2)) - Q(12(2)+1)
                         END IF
                 END IF
C RIGHT NODE:
C --- SHOCK ON RIGHT, HEADED LEFT, JURES NODE HITH NO CONTACT---
C LEFT NODE:
C --- NO SHOCK, MITH CONTACT ON LEFT, HEADED RIGHT, JUMPS NOCE---
C
         ELSE IF ((RNODE(2), EQ. 231), AND. (RNODE(3), EQ. 100)) THEN
                 IF((LNODE(2).EQ.100).AND.(LNDDE(3).EQ.321)) THEN
C
  ----- DETERMINE NODE TO RIGHT TO SHOCK AND CONTACT SURFACE----
                         I2(1) = RNODE(1)
                         12(2) = LNO0E(1) + 1
                         CALL DELTAX(12.SIGMA.XB.XA.H)
C -----CALCULATE JUMP THROUGH CONTACT SURFACE THEN SHOCK-----
                         IF(12(2).EQ.(12(1)-1)) THEN
                                 IISISIIA = BA
                                 Q8 - 01 12(2))
                                 S8 . S(12(2))
                                 SA . SI 12(2)-2)
                                 CALL CSJUMPIAB.QB.SB.SA.GZ.QA.AAI
                                 QQA = QQCALC(QA,AA,SA)
                                 RRA . RRCALCIGA,AA,SA)
C
      --INTERPOLATE TO MODE(12(2)-1) AND ASSIGN CORRECTED VALUES----
                         IF (12(2).EQ.2) THEN
                                 CALL 880RY(RRA, QQA, SA, RR([212]-1], QQ([2(2]-1],
        C
                                   $(12(2)-1),A(12(2)-1),Q(12(2)-1))
                         ELSE
                         CALL INTERPERRA, RR(12(2)-2), QQA, QQ(12(2)-2), SA,
        C
                                $112(21-21, A62), (XA(2)+H).RR(12(2)-1),
        C
                                99(12(2)-1),S(12(2)-1),A(12(2)-1),
        C
                                Q(12(2)-1))
                         END IF
                                 1151511A . AA
                                 41 = Q1 12121)
                                 SA = S(12(2))
                                 CALL SKJUPP(AA,QA,SA,AR,DQ,VS,G,G1,H,AB,QB,SB)
```

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B . GCCALCIGS.48.98)
                                   B . MCALCIGS,46,261
  ----- INTERPOLATE TO MODE(12(1)) AND ASSIGN CORRECTED VALUES----
                                 IF (12(1).69.M) THEN
                               CALL GOORY(RRS.GGS.SS.RR(I2(1)).GG(I2(1)).S(I2(1)).
        ¢
                                   A(12(1)), @(12(1));
                                 ELSE
                                 CALL INTERP(RRS,RR(I2(1)+1),QGS,QQ(I2(1)+1),SS,
        C
                                    $(12(1)+1), x$(1),(x$(1)+M),RR(12(1)),
                                    00(12(1)),S(12(1)),A(12(1)),Q(12(1)))
                                 END IF
                         ELSE
                                 RR(12(2)-1) = RR(12(2)-2)
                                 99(12(2)-1) = QQ(12(2)-2)
                                  S(12(2)-1) = S(12(2)-2)
                                  A(12(2)-1) - A(12(2)-2)
                                  Q(12(2)-1) = Q(12(2)-2)
                                 ##(IZ(1)) = ##(IZ(1)+1)
                                 00(12(1)) . 00(12(1)+1)
                                  31121111 - 3112111+11
                                  A(12(1)) = A(12(1)+1)
                                  Q(12(1)) . Q(12(1)+1)
                         ENG IF
                 END IF
C RIGHT HODE:
C --- SHOCK ON LEFT, HEADED LEFT, JUMPS HODE HITH CONTACT ON RIGHT---
C --- MEADED LEFT, DOES NOT CROSS NODE OR NO SHOCK HITH CONTACT ON---
C --- AIGHT, HEADED LEFT, CROSSED HODE---
C LEFT NOOE:
  --- SHOCK ON RIGHT, HEADED LEFT, JUMPS NOOE HITH NO CONTACT---
         ELSE IF: ( | RNODE(21, Eq. 351) AND. (RNODE(3), Eq. 251, OR. RNODE(3), Eq.
                   232 F1. OR . ( RNDDE( 21, EQ. 100 , AND , RNDDE( 31, EQ. 231 F) THEN
                 IF((LNO0E(2).EQ.231).AND.(LNO0E(3).EQ.100)) THEN
C ----DETERMINE NODE TO RIGHT OF SHOCK AND CONTACT SURFACE----
                         12(1) . LND06(1)
                         IFI MIDDE! 3 | . EQ . 232 | THEN
                                 12(2) * ********** 1
                         ELSE
                                 IZIZI . RNODE: 11
                         END IF
                         CALL DELTAXIIE, SIGNA, XB, XA, HI
C ---- EXTRAPOLATE TO LEFT FACE OF SHOCK----
                 IF (12(1).EQ.2) THEN
                         CALL 860RY1RR(1),QQ(1),S(1),RRA,QQA,SA,AA,QA)
                 # L S.F
                 CALL EXTRAP(RR: 12(1)-1).RR(12(1)-2).QQ(12(1)-1).QQ(12(1)-2).
        c
                          $112(1)-1).$(12(1)-2).XA(1),M,RRA,QQA,SA,AA,QA)
                 END IF
  -----CALCULATE /ARIABLE CHANGE ACROSS SHOCK----
                 CALL SKJUPP(AA,QA,SA,AR,DQ,VS,G,G1,M,AB,QB,SB)
  -----DETERMINE CORRECTED VALUES AT MODE(12(1)) AND ASSIGN THEM-----
C
                 IFIRNODE(2), EQ. 1001 THEN
                         998 . GCALCIGE.AB.SBI
                         RRS . RRCALCIQS.AS.JS:
C -----INTERPOLATE TO MODELIZIALL AND ASSIGN CORRECTED VALUES-----
```

```
IF (12(1).89.N) THEN
                              CALL BOORY(RRS.com.SB.RR(I2(1)).00(12(1)).S(I2(1)),
                                 A(12(1)).4(12(1)))
                                ELSE
                               CALL INTERPIRES, RR(12(1)+1), 008, 00(12(1)+1), SS,
                                  $(12(1)+1),X$(1),(X$(1)+N),RR(12(1)),
                                   QQ(18(1)),8(12(1)),A(12(1)),Q(12(1)))
 ---- EXTRAPOLATE TO LEFT FACE OF CONTACT SURFACE----
                IF (12(2), 20.2) THEN
                        CALL BBORY(RR(1), QQ(1), S(1), RRA, QQA, SA, AA, QA)
                ELSE
                CALL EXTRAP(RRIIZ(2)-1), RR([2]2)-2), QQ([2]2)-1), QQ([2]2)-2),
                         $(12(2)-1).$(12(2)-2),XA(2).H,RRA,QQA.SA.AA.QA)
                END IF
                ELSE
                        QQ([2(1)] - QQCALC(QB,AB.SB)
                        RRITZ(1)) . RRCALC(98.A8.S8)
                         $(12(1)) = S&
                          ALIZIAN . AB
                          @(12(1)) * Q8
                        IF(RNO0E(3).EQ.232) THEN
                                RR(12(1)+1) = RR(12(1))
                                QQ([2(1)+1) = QQ([2(1))
                                 S(12(1)+1) = S(12(1))
                                 A(12(1)+1) = A(12(1))
                                 Q(12(1)+1) = Q(12(1))
                                 00 TO 40
                        ELSE
                                AA - AR
                                SA . SB
                        ENG IF
                 END IF
                        SB . SITZIZ1+1)
  ---- CALCULATE VARIABLE CHANGE ACROSS CONTACT SURFACE----
                        CALL CSJUMPIAA,QA,SA,SB,GZ,QB,AB;
                        998 . 39CALC198.48.581
                        RRS # RRCALCIGS,AB,SBI
  ----INTERPOLATE TO NODELIZEZI) AND ASSIGN CORRECTED VALUES----
                                IF (IZ(Z).EQ.N) THEN
                              CALL BBDRY(RRB, QGB, SB, RR([2(2)], QQ([2(2)], S([2(2)],
       ¢
                                  A1 121211, Q1 1212111
                                CALL INTERPIRES.RRI [2121+1].QQB,QQ([2(2)+1].SB,
       C
                                   $(12(2)+1),XB(2),(XB(2)+H),RR(12(2)),
                                   QQ(12(2)),S(12(2)),A(12(2)),Q(12(2)))
                                END IF
                 END IF
         END IF
         QQ TQ 40
C --- BRANCH HERE IF THERE ARE ONE OR THO NODES TO CORRECT, BUT THEY ---
C --- ARE SEPERATED BY MORE THAN 2H. CHECK FOR SHOCK/CONTACT SURFACE---
C --- INTERACTION, AND CORRECT APPROPRIATELY ---
    30 NOOE = LNOOE(1)
         SHOCK . LNOOE(2)
         CNTACT . LNODE(3)
C --- NO SHOCK, CONTACT SURFACE ON LEFT, HEADED RIGHT, JUMPS NODE ---
    35 IF((SHOCK.EQ.100).AND.(CNTACT.EQ.321)) THEN
```

```
I2(2) = NOOE + 1
                CALL DELTAX(IZ,SIGMA,XB,XA,H)
  ----CHECK FOR A SHOCK INTERACTING MITH CONTACT SURFACE AT HODE----
                IF((SIGMA(1,2).LT.(X2(2)+H)).AND.
                 (SIGMA(1,2).GT.(X2(2))))THEN
                        AB = ALIZIZII
                        C = Q(12(2))
                        SB = S(12(2))
                 ELSE
  ---- EXTRAPOLATE TO RIGHT FACE OF CONTACT SURFACE----
C
                        IF (12(2).EQ.N) THEN
                                CALL BBORY(RRIN),QQ(N),S(N),RRB,QQB,SB,AB,QB)
                        CALL EXTRAP(RR(12(2)), RR(12(2)+1), QQ(12(2)), QQ(12(2)+1),
                              $(12(2)),$(12(2)+1),XB(2),H,RRB,QGB,$8,A8,GB)
       C
                 END IF
                 SA = SIZ(2)-2)
    - CALCULATE VARIABLE CHANGE OVER CONTACT SURFACE ---
                 CALL CSJUMP(AB,QB,SB,SA,G2,QA,AA)
                 QQA = QQCALC(QA,AA,SA)
                 RRA = RRCALC(QA,AA,SA)
  -----INTERPOLATE TO NODE(12(2)-1) AND ASSIGN CORRECTED VALUES-----
                 IF (12(2).EQ.2) THEN
                        CALL BBDRY(RRA.QQA.SA.RR(I2(2)-1).QQ(I2(2)-1).
                             S(12(2)-1),A(12(2)-1),Q(12(2)-1))
        ¢
                 ELSE
                 CALL INTERPIREA, RRIIZIZI-ZI, QQA, QQIIZIZI-ZI, SA,
                          $(12(2)-2), XA(2), (XA(2)+H), RR(12(2)-1).
        C
                          QQ(12(2)-1),S(12(2)-1),A(12(2)-1),
        c
                          Q( 12( 2)-1))
                 END IF
  --- NO SHOCK, CONTACT SURFACE ON LEFT, HEADED LEFT, JUMPS NODE ---
C
         ELSE IF ((SHOCK.EQ.100).AND.(CNTACT.EQ.231)) THEN
                 12121 - NOOE
                 CALL DELTAX(IZ,SIGMA,XB,XA,H)
   ----CHECK FOR A SHOCK INTERACTING HITH CONTACT SURFACE AT MODE----
                 IF!(SIGMA(1,2).GT.(X2(2)-(2.D004H))).AND.(SIGMA(1,2).LT.
        C
                  (X2(2)-H1)) THEN
                         AA = A(12(2)-1)
                         QA = Q(12(2)-1)
                         SA = S(12(2)-1)
                 ELS#
   ---- EXTRAPOLATE TO LEFT FACE OF CONTACT SURFACE----
                 IF (12(2).EQ.2) THEN
                         CALL BBDKY(RR(1),QQ(1),S(1),RRA,QQA,SA,AA,QA)
                  ELSE
                 CALL EXTRAP(RR(12(2)-1),RR(12(2)-2),QQ(12(2)-1),QQ(12(2)-2),
                           $(12(2)-1),$(12(2)-2),XA(2),H,RRA,QQA,$A,AA,QA)
        C
                 END IF
                  END IF
                  SB = S(12(2)+1)
                  CALL CSJUMPIAA,QA,SA,SB,G2,QB,AB)
                  QQB = QQCALC(QB,AB,SB)
                  RRB = RRCALC(QB,AB,SB)
```

```
---INTERPOLATE TO MODE(IS(2)) AND ASSIGN CORRECTED VALUES----
                 IF (12(2).EQ.M) THEN
                       CALL BBORY(RRB, QGB,SB, RR([2(2)],QQ([2(2)],S([2(2)),
       C
                            A(12(2)),Q(12(2)))
                ELSE
                       CALL INTERP(RRB, RR(I2(2)+1), QQB, QQ(I2(2)+1),SB,
                             $(12(2)+1),XB(2),(XB(2)+H),RR(12(2)),
       C
                             QQ(12(2)),S(12(2)),A(12(2)),Q(12(2)))
                 END IF
 --- SHOCK ON LEFT, HEADED RIGHT, JUMPS NODE HITH NO CONTACT ---
                ELSE IFIISHOCK.EQ.321).AND.(CNTACT.EQ.100)) THEN
                 I2(1) = NODE + 1
                 CALL DELTAX(IZ,SIGMA,XB,XA,H)
  ----CHECK FOR A CONTACT SURFACE INTERACTING MITH SHOCK AT NODE-----
                 IF((SIGMA(2,2).LT.(X2(1)+H)).AND.
       C
                  (SIGMA(2,2).GT.(X2(1)))) THEN
                        AB . A(12(1))
                         Q8 = Q(12(1))
                        S8 = S(I2(1))
                 ELSE
  ---- EXTRAPOLATE TO RIGHT FACE OF SHOCK----
                        IF (12(1), EQ.N) THEN
                                CALL BBDRY(RR(N), 99(N), S(N), RRB, 998, S8, A8, 98)
                        CALL EXTRAP(RR[I2(1)], RR[I2(1)+1], QQ(I2(1)), QQ(I2(1)+1),
       ¢
                              $(12(1)),$(12(1)+1),X8(1),H.RRB,QQB,$8,AB,QB)
                 END IF
C --- CALCULATE VARIABLE CHANGE ACROSS SHOCK ---
                 CALL SKJUMP(AB, QB, SB, AR, DQ, VS, G, G1, H, AA, QA, SA)
                 QQA = QQCALCIQA.AA,SAI
                 RRA = RRCALCIGA.AA,SAI
  ----INTERPOLATE TO NODE(IZ(1)-1) AND ASSIGN CORRECTED VALUES----
                 IF (12(1).EQ.2) THEN
                        CALL BBDRY(RRA, QQA, SA, RR([2(1)-1), QQ([2(1)-1),
       C
                             S(12(1)-1),A(12(1)-1),Q(12(1)-1))
                 ELSE
                 CALL INTERP(RRA, RR(12(1)-2), QQA, QQ(12(1)-2), SA.
       Ç
                          S(12(1)-2), XA(1), (XA(1)+H), RR(12(1)-1),
                          QQ([2(1)-1),S([2(1)-1),A([2(1)-1),
                          Q(12(1)-1))
                 END IF
  --- SHOCK ON RIGHT, HEADED LEFT, JUMPS NODE HITH NO CONTACT SURFACE--
         ELSE IF ((SHOCK.EG.231).AND.(CNTACT.EG.100)) THEN
                 I2(1) = NODE
                 CALL DELTAX(12,SIGMA,XB,XA,H)
                 IF((SIGNA(2,2).GT.(X2(1)-(2.D00#H))).AND.(SIGNA(2,2).LT.
       c
                 (X2(1)-H))) THEN
                        AA = A(12(1)-1)
                        QA = Q(12(1)-1)
                         SA = S(12(1)-1)
                 ELSE
  ----EXTRAPOLATE TO LEFT FACE OF CONTACT SURFACE----
```

```
IF (12(1).EQ.2) THEN
                      CALL $80RY(RR(1), QQ(1), S(1), RRA, QQA, SA, AA, QA)
               CALL EXTRAP(RR(I2(1)-1), RR(I2(1)-2), QQ(I2(1)-1), QQ(I2(1)-2),
       C
                        $(12(1)-1),$(12(1)-2),XA(1),H,RRA,QQA,SA,AA,QA)
               ENO IF
               END IF
   -- CALCULATE VARIABLE CHANGE OVER SHOCK ---
        IF(12(1).EQ.N-1) THEN
        END IF
               CALL SKJUMPIAA,QA,SA,AR,DQ,VS,G,G1,M,AB,QB,SBI
C ---- DETERMINE CORRECTED VALUES AT NODE(12(1)) AND ASSIGN THEM----
        IF(12(1).EQ.N-1) THEN
        END IF
                QQB = QQCALC(QB,AB,SB)
                RRB = RRCALC(QB,AB,SB)
  ----INTERPOLATE TO NODE(12(1)) AND ASSIGN CORRECTED VALUES----
C
               IF (IZ(1).EQ.N) THEN
                     CALL BBDRY(RRB, QQB, SB, RR([2(1)), QQ([2(1)), S([2(1)),
       C
                          A(12(1)),Q(12(1)))
               ELSE
                CALL INTERPIRES, RR([2(1)+1), QQB, QQ([2(1)+1),SB,
                        $(12(1)+1),XB(1),(XB(1)+H),RR(12(1)),
                        QQ(12(1)),$(12(1)),A(12(1)),Q(12(1)))
                END IF
        END IF
C --- CHECK IF SECOND NODE NEEDS CORRECTING IF SO LOOP BACK AROUND ---
        IF(RNODE(1).EQ.0) GO TO 40
                NODE = RNODE(1)
                SHOCK = RNODE(2)
                CHTACT = RNODE(3)
                RNODE(1) = 0
                GO TO 35
    40 RETURN
        END
¢
         SUBROUTINE DELTAX(I2,SIGMA,XB,XA,H)
C
C
         C
C
            LOCATE DISCONTINUITY WITHIN INTERVAL SUBROUTINE
C
C
         DIMENSION 12(4), SIGMA(4,2), XB(4), XA(4), X2(4)
         INTEGER 12
        DOUBLE PRECISION SIGMA, XB, XA, H, X2
        X2131=0.000
        X2(4)=0.000
C
C -----CALCULATE DISTANCE NODE TO RIGHT OF DISCONTINUITY IS FROM LEFT. --
C ----BOUNDARY OF TUBE THEN DETERMINE DISTANCE FROM THIS NODE 12(#)----
C ----TO DISCONTINUITY AND DISTANCE FROM NODE TO LEFT OF DISCONTINUITY-
C ----TO THAT DISCONTINUITY----
        X2(1) = DBLE(I2(1)-1) * H
         MB(1) = (X2(1)-SIGMA(1,2))
         XA(1) = (H-XB(1))
  ---- CALCULATE SAME VALUES FOR CONTACT SURFACE----
```

```
X2(2) - DBLE(12(2)-1) + N
       XB(2) = (X2(2)-SIQMA(2,2))
       XA(2) = (H-)G(2))
        RETURN
       END
C
       SUBSCUTINE SKULPPIADN, CON. SON. ARATIO, DELTAG, VSHOCK, G, 61, M,
                       AUP, QUP, SUP)
C
            C
C
                     SHOCK JUMP SUBROUTINE
C
C
        ¢
     ----- VARIABLE DEFINITIONS -----
C
¢
C
     #ON - VARIABLE DOMNSTREAM OF SHOCK
     ARATIO - SPEED OF SOUND RATIO
C
C
     DELTAG - VELOCITY JUMP ACROSS SHOCK
     WUP - VARIABLE UPSTREAM OF SHOCK
C
C
     VSHOCK - SHOCK VELOCITY
       DOUBLE PRECISION ADN. GON, SDN, ARATIO, DELTAG, VSHOCK, G, G1, M,
                      AUP, QUP, SUP, SA1, SA2, UDN, UUP
C
 ----CALCULATE THE SPEED OF SOUND CHANGE THRU SHOCK----
C
        AUP = ADNHARATIO
C
 ----CALCULATE THE ENTROPY CHANGE THRU SHOCK----
C
C
        SA1 = (G1/G)*DLOG((2.D00*G*(W**2)-G+1.D00)/(G+1.D00))
        SA2 = G1*DLOG(((G-1.D00)*(N**2)+2)/((G+1.D00)*(N**2)))
        SUP * SDN - SA1 - SA2
C
 ----CALCULATE THE VELOCITY CHANGE ACROSS SHOCK----
       UDN = QON - VSHOCK
       UUP = UDN + ADN#DELTAG
        QUP = UUP + VSHOCK
        RETURN
        END
C
        SUBROUTINE CSJUMP(ADN, QON, SDN, SUP, G2, QUP, AUP)
C
        ********************************
C
              CONTACT SURFACE JUMP SUBROUTINE
C
C
        *************************
C
C
        DOUBLE PRECISION QUP, QON, AUP, ADN, SUP, SDN, G2
C
C ----CALCULATE THE SPEED OF SOUND CHANGE ACROSS THE CONTACT SURFACE---
C ----NOTE: THE VELOCITY IS CONTINUOUS ACROSS A C.S.----
C
        QUP = QDN
        AUP = ADN * DEXP((SDN-SUP)/G2)
        RETURN
        END
C
        SUBROUTINE EXTRAPIRRL, RRR, QQL, QQR, SL, SR, DX, DH, RRINT, QQINT, SINT,
                       ( THID, THIA
¢
        C
                    EXTRAPOLATION SUBROUTINE
C
```

```
SOLDLE PRECISION AND ARE GOL GOR SL SR SA SH ARINT GOINT SINT
                        THIP. THIA
 -----REIMAN VARIABLES ARE EXTRAPOLATED, AND THE CORRESPONDING-----
C ----VALUES FOR VELOCITY AND SPEED OF SQUAD ARE CALCULATED----
        RRINT . RRL - (DX . (RRR-RRL)/DH)
        992NT - 99L - (BX - 199R-99L1/DH)
          SINT - SL - (DX + (SR-SL)/DH)
          AINT = (GGINT-RRINT)/(2.DOG=SINT)
          GINT . (GGINT+RRINT)/(2.000)
        RETURN
        END
C
        SUBMOUTINE INTERPIREL, RRR, QQL, QQR, SL, SR, DX, DH, RRINT, QQINT, SINT,
                         AINT, GINT
C
                        ******
C
C
                     INTERPOLATION SUBROUTINE
C
            C
C
        DOUBLE PRECISION RRL, RRR, QQL, QQR, SL, SR, DX, DH, RRINT, QQINT, SINT,
                        AINT .GINT
C ----REIMAN VARIABLES ARE INTERPOLATED, AND THEIR CORRESPONDING----
C ----VALUES OF VELOCITY AND SPEED OF SOUND ARE CALCULATED----
        RRINT = RRL - (DX + (RRL-RRR)/DH)
        QQINT = QQL - (DX * (QQL-QQR)/DH)
          SINT = SL - (DX + (SL-SR)/DH)
          AINT = (QQINT-RRINT)/(2.000*SINT)
          QINT = (QQINT+RRINT)/2.000
        RETURN
        END
C
        SUBROUTINE DBURST(N,H,QQ,RR,S,G,G1,G2,DELT,I2,X2,H,AR,DQ,VS,
       #LMPRES.SIGMA.A.Q)
C
      C
C
            DIAPHRAM BURSTING SUBROUTINE
C
C
      *******************************
        INTEGER N,I,Y,I2,L,SHKDIR,CSDIR,LMPRES
        DIMENSION X2(4),RR(N),QQ(N),S(N),I2(4),SIGMA(4,2),A(N),Q(N)
        DOUBLE PRECISION X2,X,H,AB,SA,SB,AA,QA,QB,QQA,QQB,RRA,RRB,SIGMA,
       C
                        RR,QQ,S,TS.W,DQ,AR,PR.G,G1,G2,VS,DELT,CSRMN,A,
                        Q,MREIMN, DREMN, EREIMN, WH, SA1, SA2, SAP, SBP, XB, XA
      ++++++ LOCATING THE NODE TO THE RIGHT ++++++++
C
        DO 10 L=1,4
            SIGMA(L,1)=SIGMA(L,2)
             V=O
            X=H
            I=2
   11
         IF (.NOT.(Y.EQ.0)) GOTO 10
               IF (SIGMA(L,1).LT.X) THEN
                    X2(L)=X
                    I2(L)=I
                    Y=1
               END IF
             X=X+H
             I=I+1
             GOTO 11
       CONTINUE
   10
```

```
C
C
         +++++++ CORRECT FOR DIAPHRAM BURSTING ++++++++++
C ----AT TIME ZERO DETERMINE CORRECT SHOCK DIRECTION-----
C -----SHKDIR = 3 IS A SHOCK HEADED LEFT, AND SHKDIR = 2 IS SHOCK-----
C ----TRAVELING RIGHT----
                  IF(LMPRES.EQ.3) THEN
                         SHKDIR = 3
                         X2(1) = X2(1) - H
                         I2(1) = I2(1) - 1
                         X2(2) = X2(2) - H
                         I2(2) = I2(2) - 1
                         GO TO 20
                  ELSE
                         SHKDIR = 2
                  END IF
    20 RRA=RR([2(1)-1]
         RRB=RR(12(1))
         QQA=QQ([2(1)-1)
         QQ8=QQ([2(1)]
         SA=S(12(1)-1)
         SB=S([2(1))
    21 AB=(QQB-RRB)/(2.D00*SB)
         AA=(QQA-RRA)/(2.D00*SA)
         IF(SHKDIR.EQ.3) THEN
                MREIMN = (RRB-RRA)/AA
                 DREMN = DABS(MREIMN)
         ELSE
                MREINN = (QQA-QQB)/AB
                 DREMN = MREIMN
         END IF
С
C ----ITERATE FOR PROPER VALUE OF W USING THE QUADRATIC FIT OF THE----
C -----REIMAN VARIABLE CHANGE WITH V CURVE. NOTE LEFT MOVING SHOCKS----
  ----ARE USED IN THESE EQUATIONS SINCE RRB-RRA/AA=-(QQA-QQB/AB)----
   100 HM=(3.0396408D01-((DREMN+2.7574D00)/0.286337D00))
         H=5.513294000-U3QRT(WH)
         DQ=2.D00*(H*H-1.D00)/(H*(G+1.D00))
         AR=DSQRT(2.000*(G-1.000)*(1.000+((G-1.000)*H*M/2.000))*
               (G*G2*H*H-1.D00))/((G+1.D00)*H)
       C
         PR=(2.D00*G/(G+1.D00))*H*H-((G-1.D00)/(G+1.D00))
         DR=((G-1.D00)*H*H+2.D00)/((G+1.D00)*H*H)
         EREIMN=DQ+(AR-1.D00)*G2-(AR*G1/G)*DLOG(PR*(DR**G))
         IF (DABS(EREIMN-DABS(MREIMN)).LT.0,10-5) GO TO 110
         DREMN = (DABS(MREIMN) - EREIMN) + DREMN
         GOTO 100
C ----DETERMINE S BEHIND SHOCK AND THEN CALCULATE THE RIEMANN-----
  ----VARIABLE CHANGE ACROSS THE CONTACT SURFACE----
C
   110
            SA1 = (G1/G)*DLOG((2.D00*G*(N**2)-G+1.D00)/(G+1.D00))
                SA2 = G1*DLOG(((G-1.D00)*(N**2)+2)/((G+1.D00)*(N**2)))
                 IF(SHKDIR.EQ.2) THEN
                        SAP = SB - SA1 - SA2
                        SBP = SAP
                 ELSE
                        SBP = SA - SA1 - SA2
                        SAP = SBP
                END IF
   103
            IF(SHKDIR.EQ.2) THEN
                        CSRMN #11DEXP(1SBP-SA1/G21)#1SA1- SBP 18AR
                 ELSE
                        CSRMN #11DEXPLISAP-SB 1/G2 | 14158 - SAP | ** AR
                 END IF
                 IF(SHKDIR.EQ.3) THEN
```